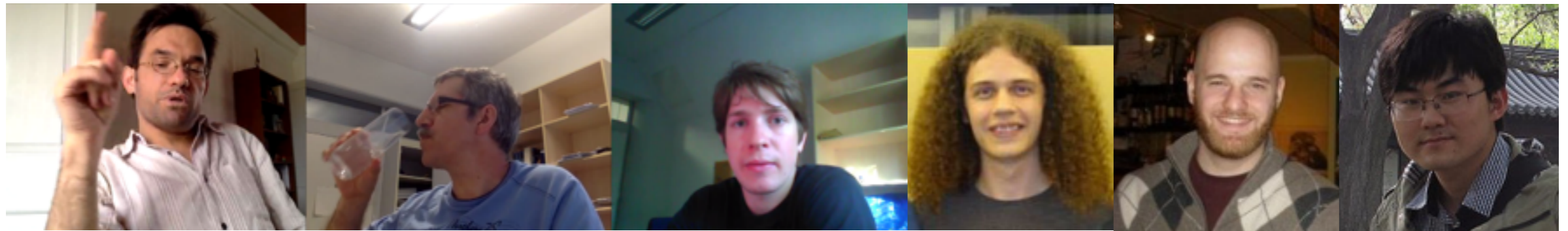


Viscosity, Conduction, Dynamo, and Convection in a Weakly Collisional Magnetized Plasma



Schekochihin

Churazov

Komarov

Melville

St-Onge

Xu

Xu & Kunz, *JPP* (2016)

Komarov, Churazov, Kunz, & Schekochihin, *MNRAS* (2016)

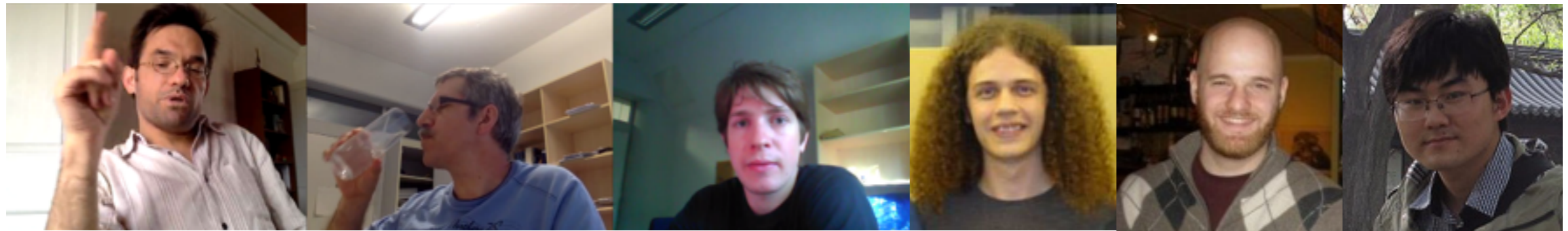
Melville, Schekochihin, & Kunz, *MNRAS* (2016)

Kunz, Schekochihin, & Stone, *PRL* (2014)

Matthew Kunz
Princeton University



or, *What is the response of a plasma in which the long-wavelength (“fluid”) and small-wavelength (“kinetic”) scales are simultaneously driven unstable by the same free-energy source?*



Schekochihin

Churazov

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Melville

St-Onge

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Xu & Kunz, *JPP* (2016)

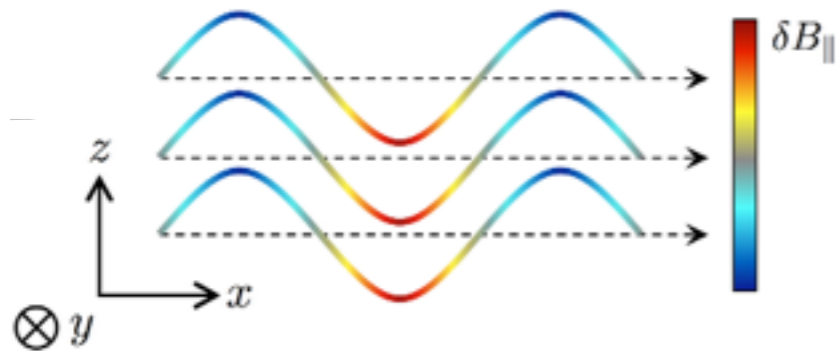
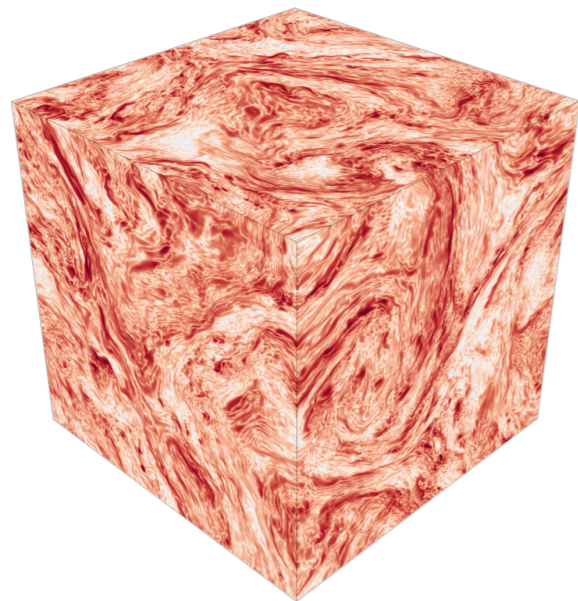
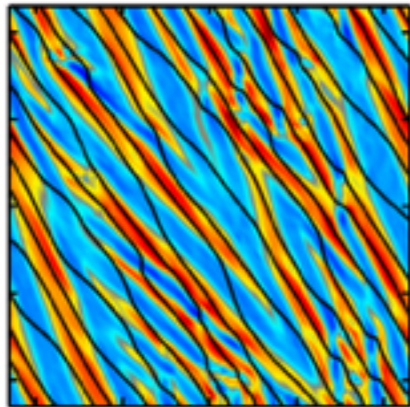
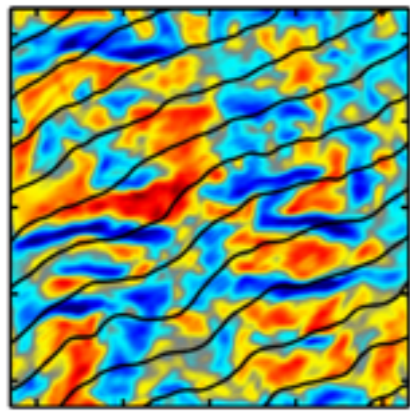
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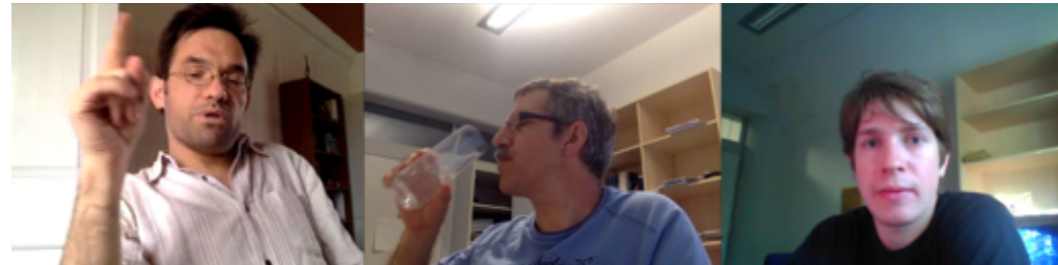




1) regulation of viscous transport by ion-Larmor-scale kinetic instabilities



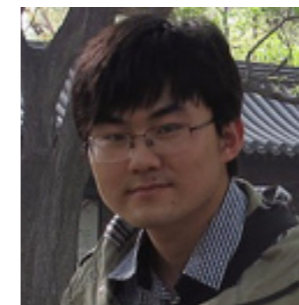
2) efficacy of electron heat transport in ion-Larmor-scale magnetic mirrors



3) turbulent dynamo in a collisionless plasma



4) linear theory of convective stability in a collisionless plasma

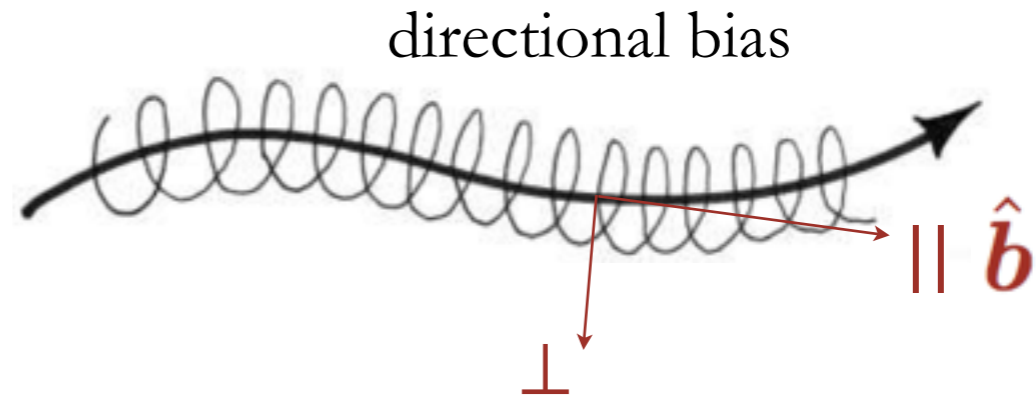


$\text{Kn} \doteq \frac{\lambda_{\text{mfp}}}{H}$ expansion parameter in Chapman-Enskog

In ICM, $\frac{\lambda_{\text{mfp}}}{H} \sim 0.001 - 0.1$, with ~ 0.01 being typical.

$\implies \left| \frac{f}{f_{\text{Maxw}}} - 1 \right| \sim 0.01$ deviations from isotropic Maxwell distribution function are allowed, at levels that are (*deceivingly*) small

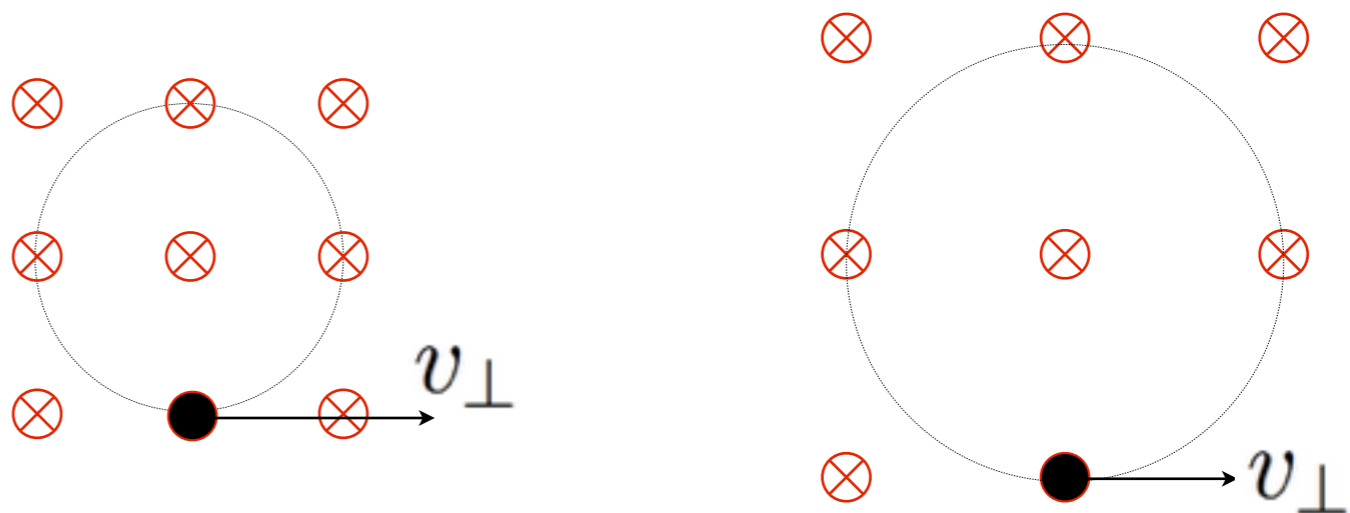
ICM is magnetized;
magnetic-field direction
biases anisotropy
(cross-field transport stifled)



change $B \implies$ produce pressure anisotropy $p_{\perp} \neq p_{\parallel}$

$$\mu = \frac{mv_{\perp}^2}{2B}$$

Kruskal (1958)



anisotropies in the distribution function produce “viscous” stresses,
which also serve as free-energy source for kinetic instabilities

$\sim 1\%$ deviations are enough, since $\beta \sim 100$ or more

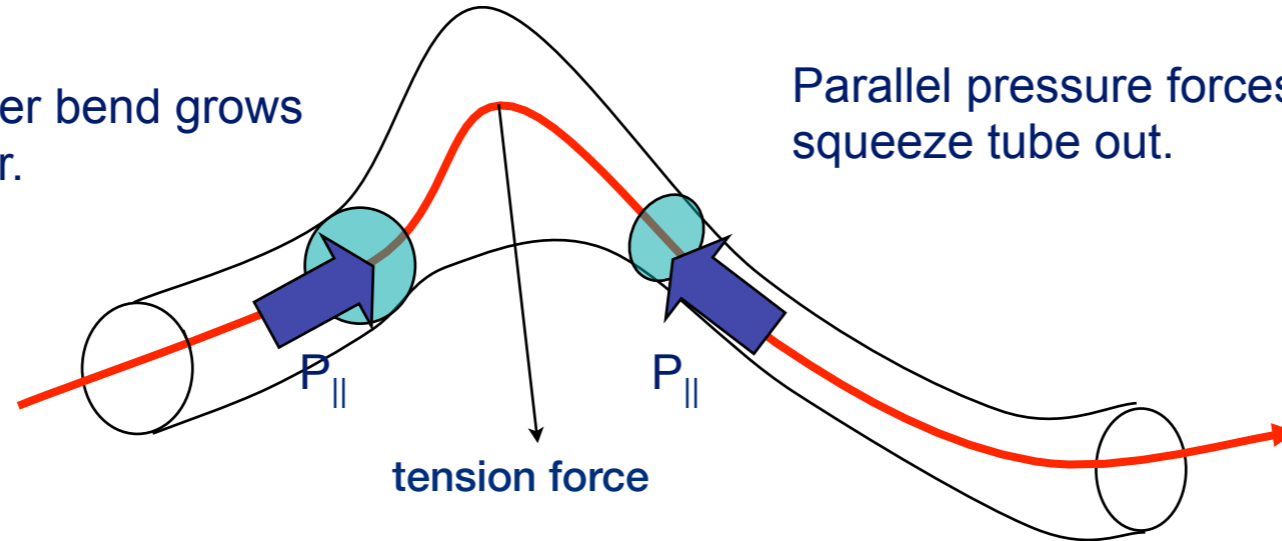
...when you try to propagate an Alfvén wave in a pressure-anisotropic plasma

firehose instability

$$p_{\parallel} - p_{\perp} \gtrsim \frac{B^2}{4\pi}$$

Tighter bend grows faster.

Parallel pressure forces squeeze tube out.



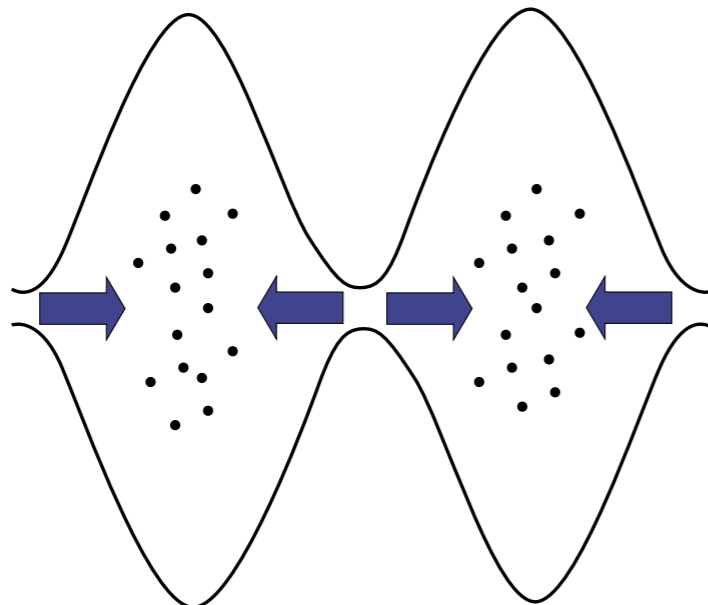
Rosenbluth 1956
Parker 1958

...when you try to Barnes-damp a slow mode in a pressure-anisotropic plasma

mirror instability

$$p_{\perp} - p_{\parallel} \gtrsim \frac{B^2}{8\pi}$$

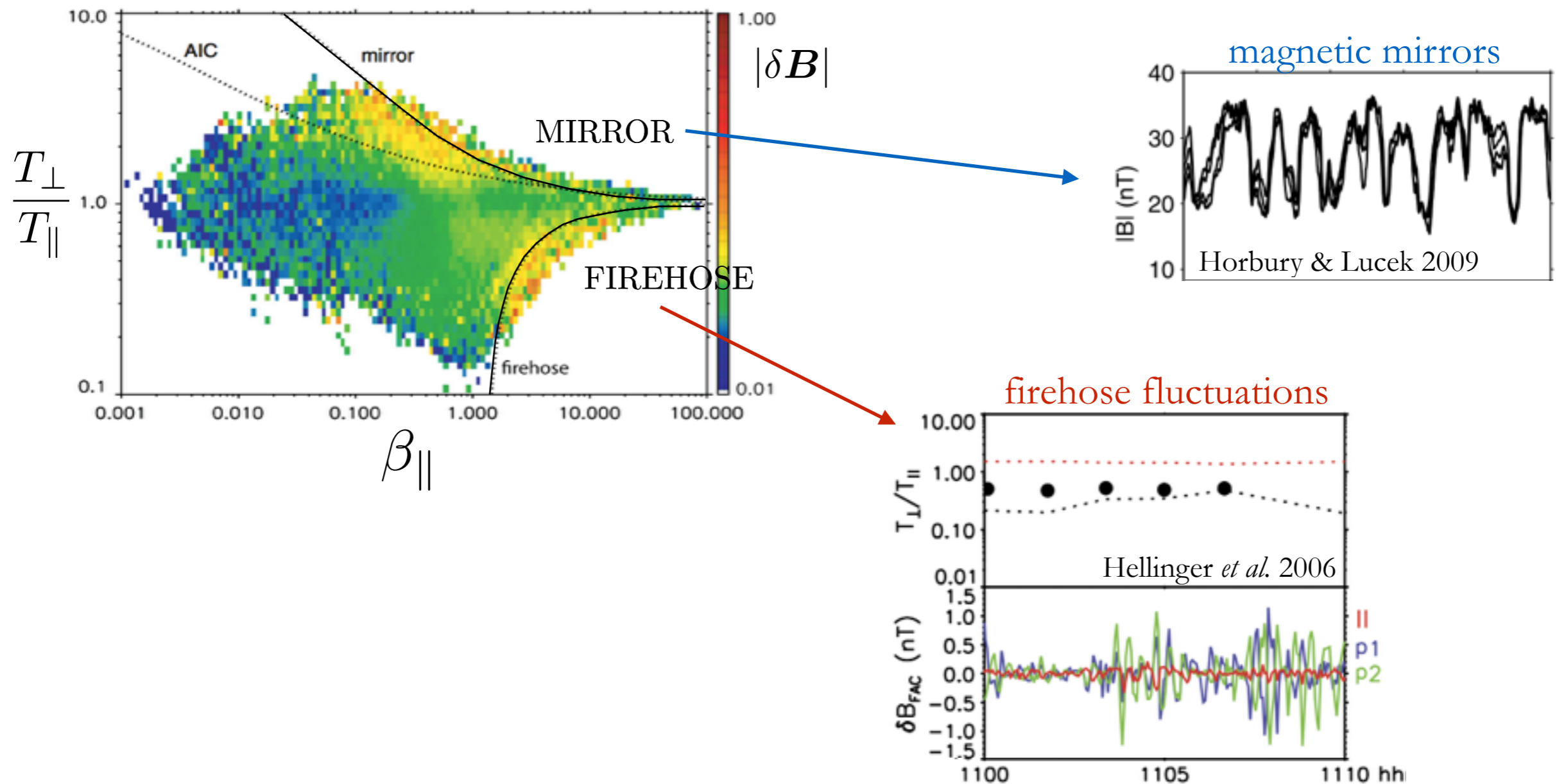
Perpendicular pressure forces blow out field lines.



$$-\hat{\mathbf{b}} (p_{\perp} - p_{\parallel}) \nabla_{\parallel} \delta B_{\parallel}$$

Rudakov and Sagdeev 1961
Southwood & Kivelson 1993

These limit pressure anisotropies, as seen in solar wind:

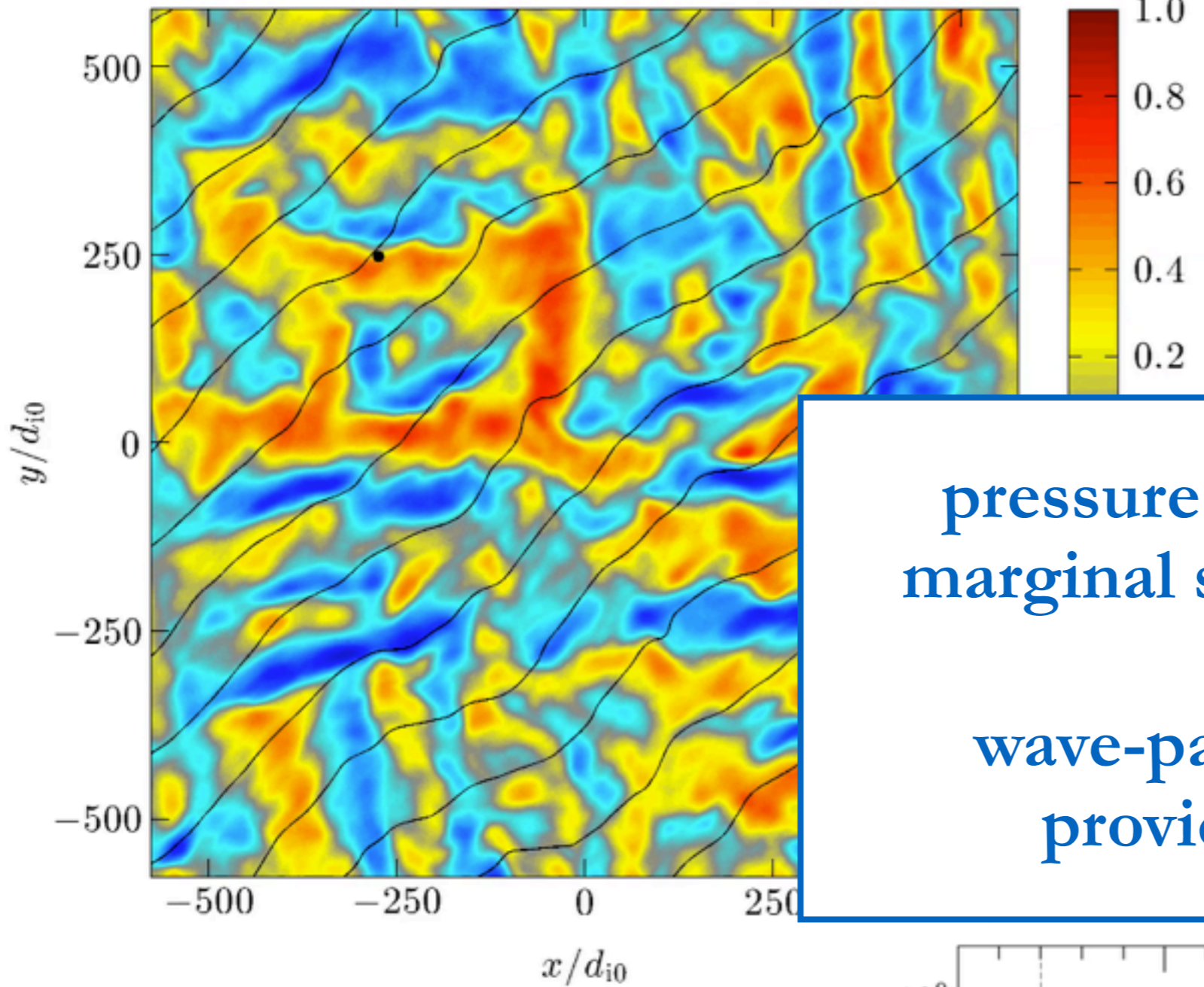


and as seen in kinetic simulations

(Hellinger & Trávníček 2008, 2015; Kunz *et al.* 2014; Riquelme *et al.* 2015; Sironi & Narayan 2015; Melville *et al.* 2016)

FIREHOSE

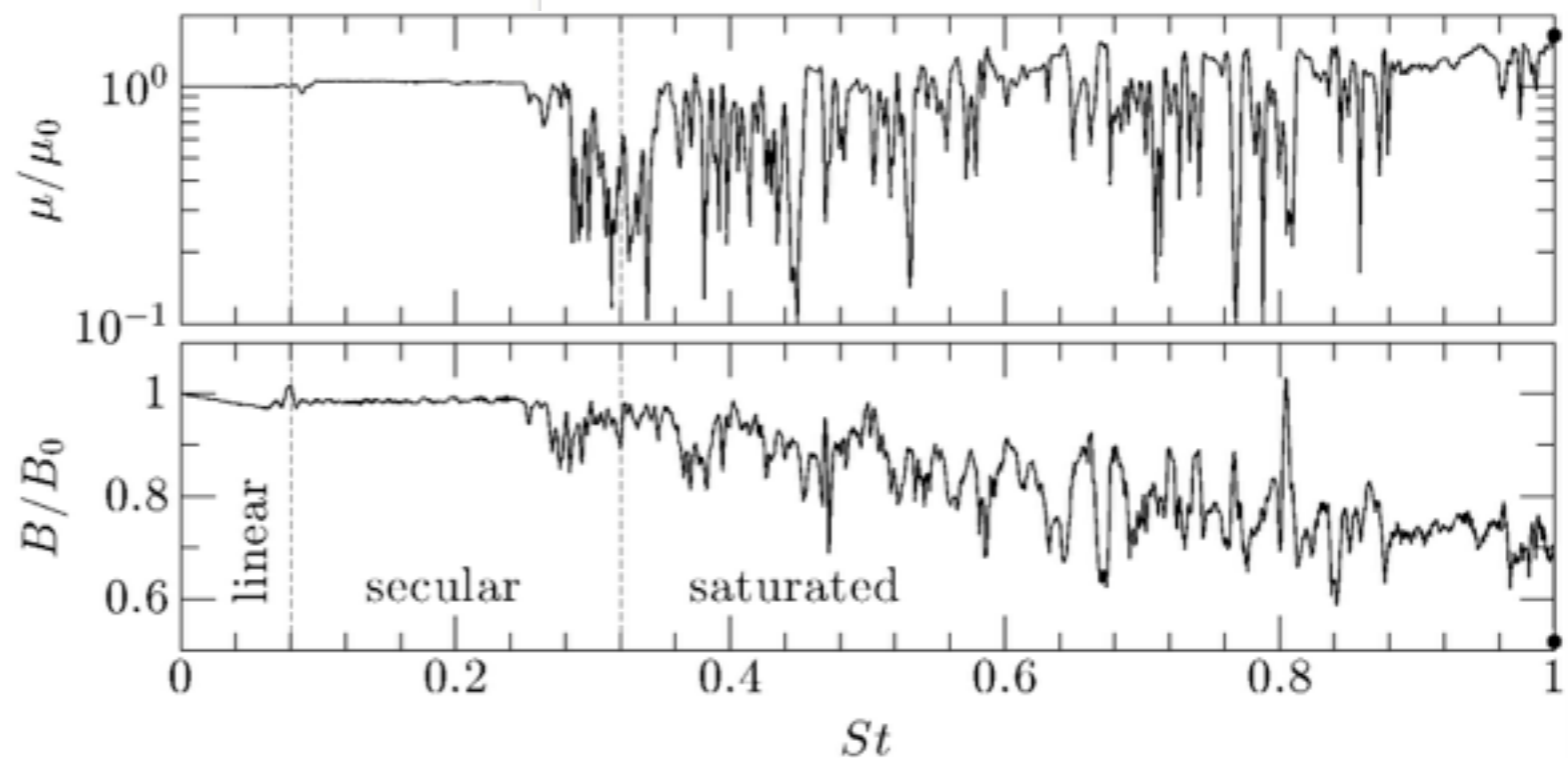
○ initial Larmor radius



pressure anisotropy pinned at marginal stability by breaking μ

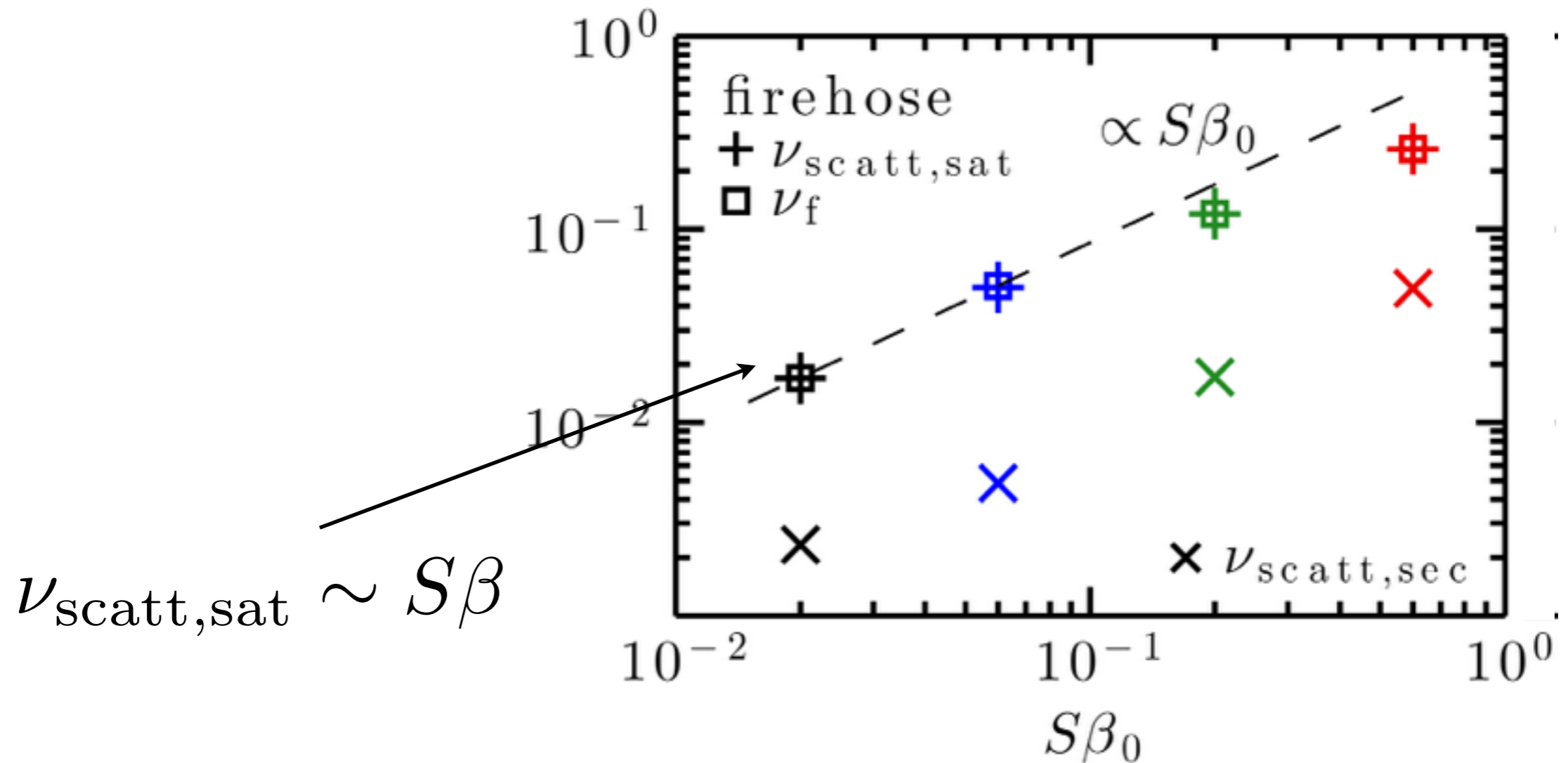
wave-particle interactions provide “collisionality”

magnetic moment of particle:



field strength at particle position:

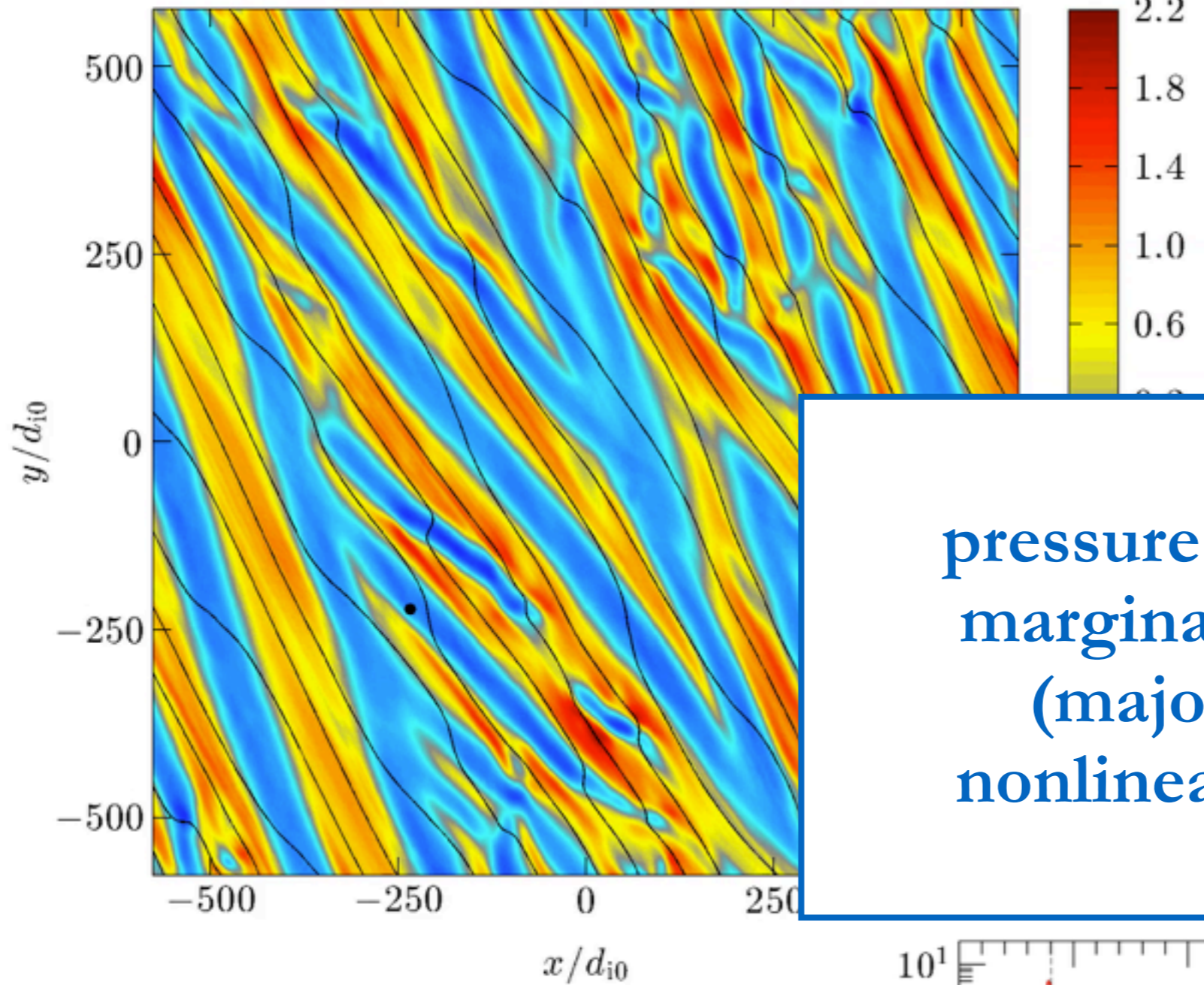
small-amplitude firehose turbulence scatters particles and thereby regulates departures from Maxwellian



Try to decrease field strength, trigger firehose, and nearly instantaneously create an effective viscosity $\sim v_A^2 / S$.

MIRROR

○ initial Larmor radius

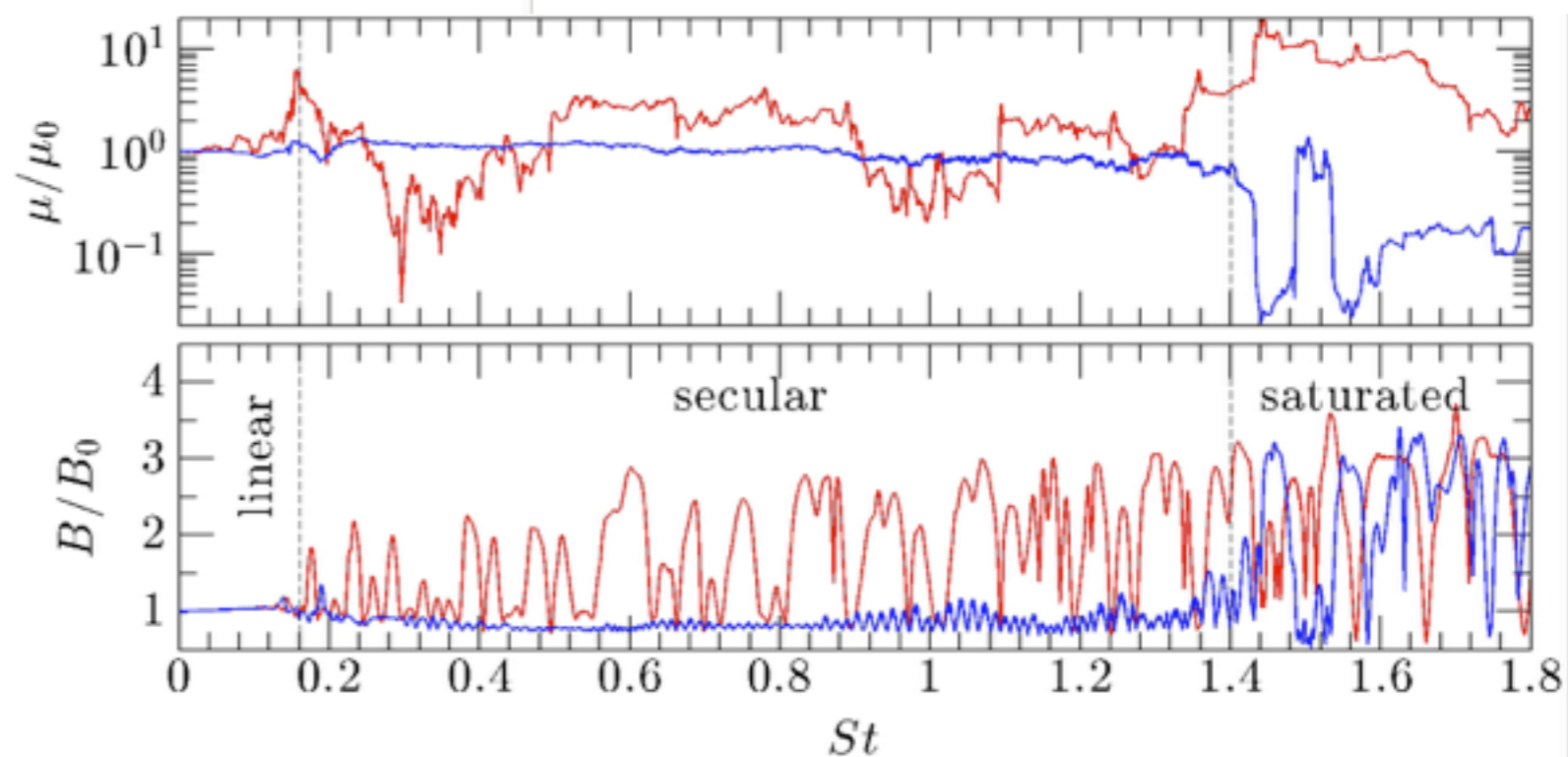


pressure anisotropy pinned at marginal stability by cooling (majority) population of nonlinearly trapped particles

magnetic moment of particle:

passing trapped

field strength at particle position:

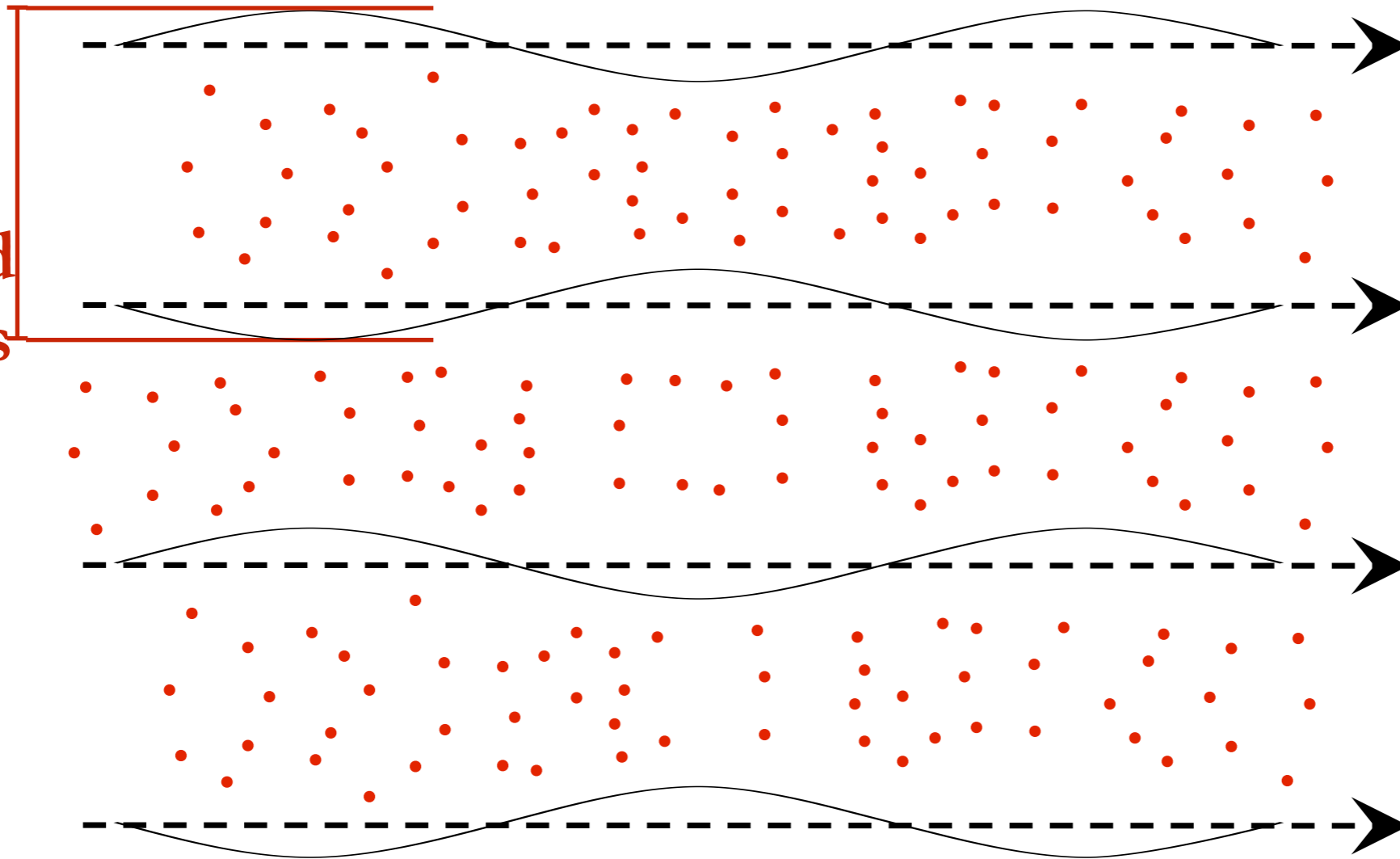


passing

trapped

ρ_i
H

fixed
distance
between
perturbed
field lines

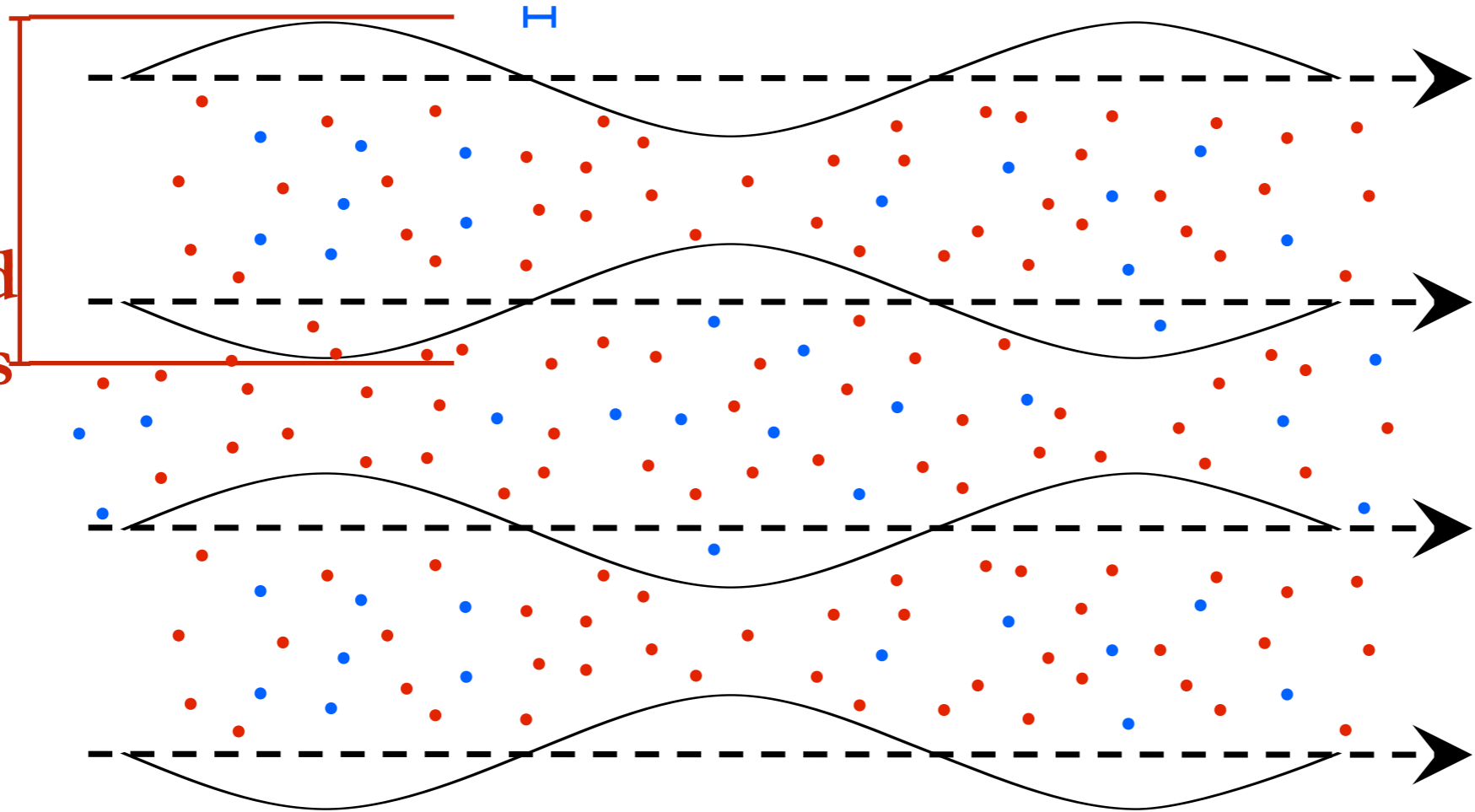


passing

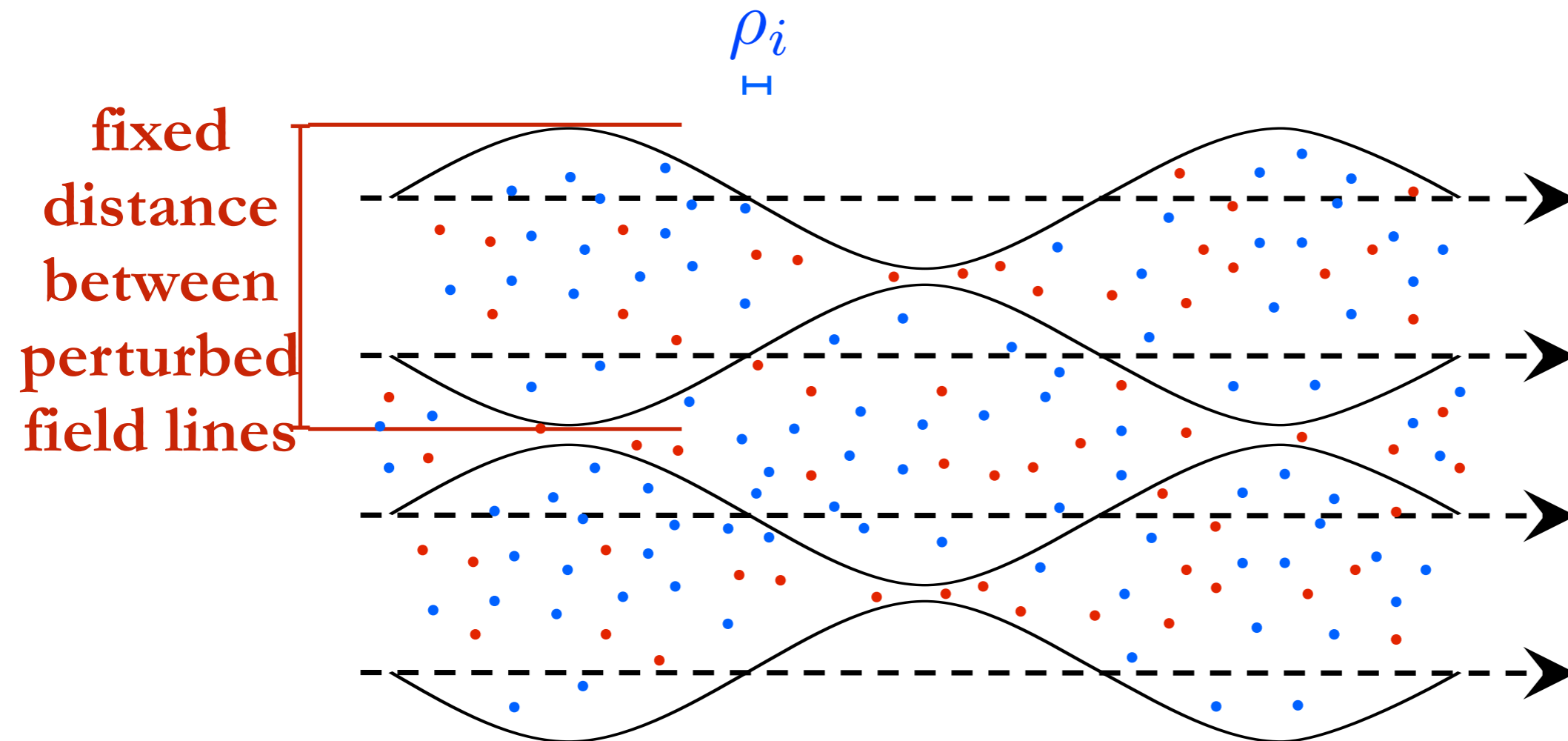
trapped

ρ_i
H

fixed
distance
between
perturbed
field lines



passing trapped



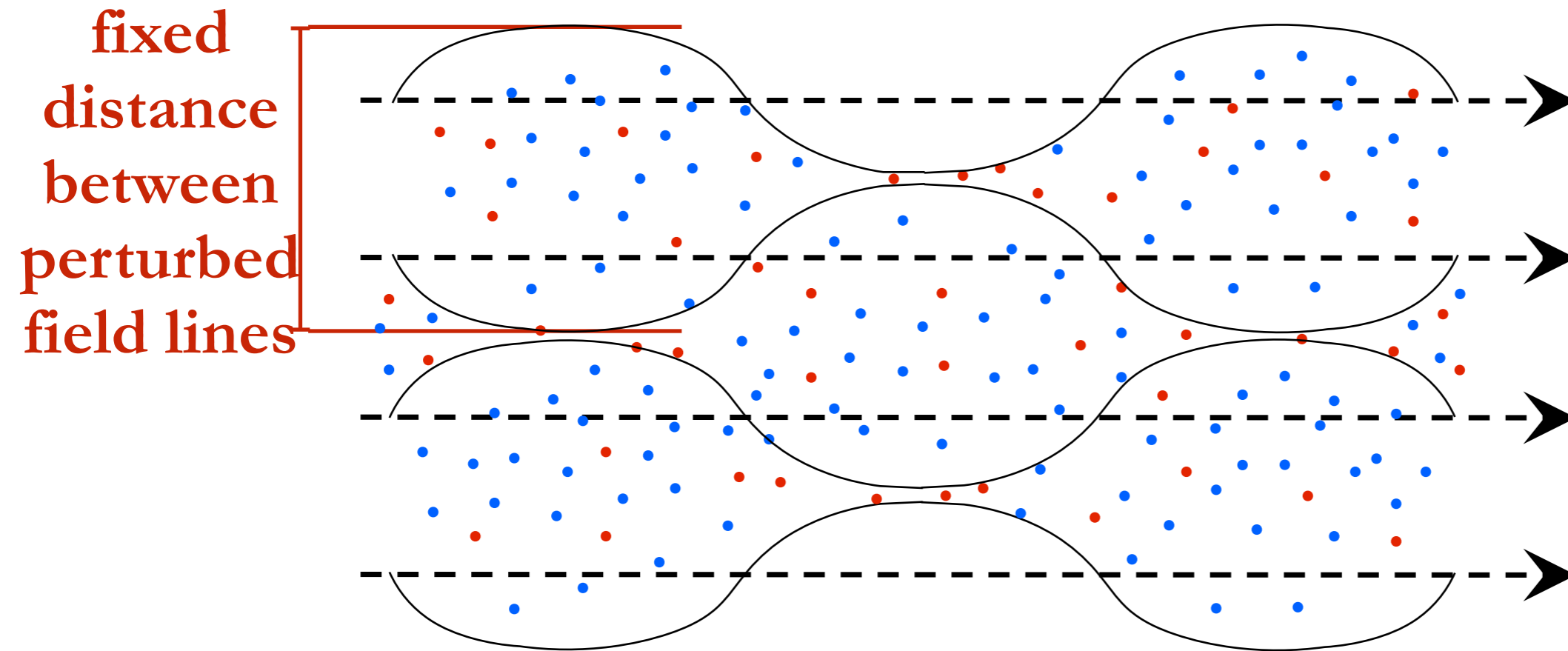
most particles do not even know that the mean field is increasing!

What does this mean for ion viscosity? I'm not sure...

passing

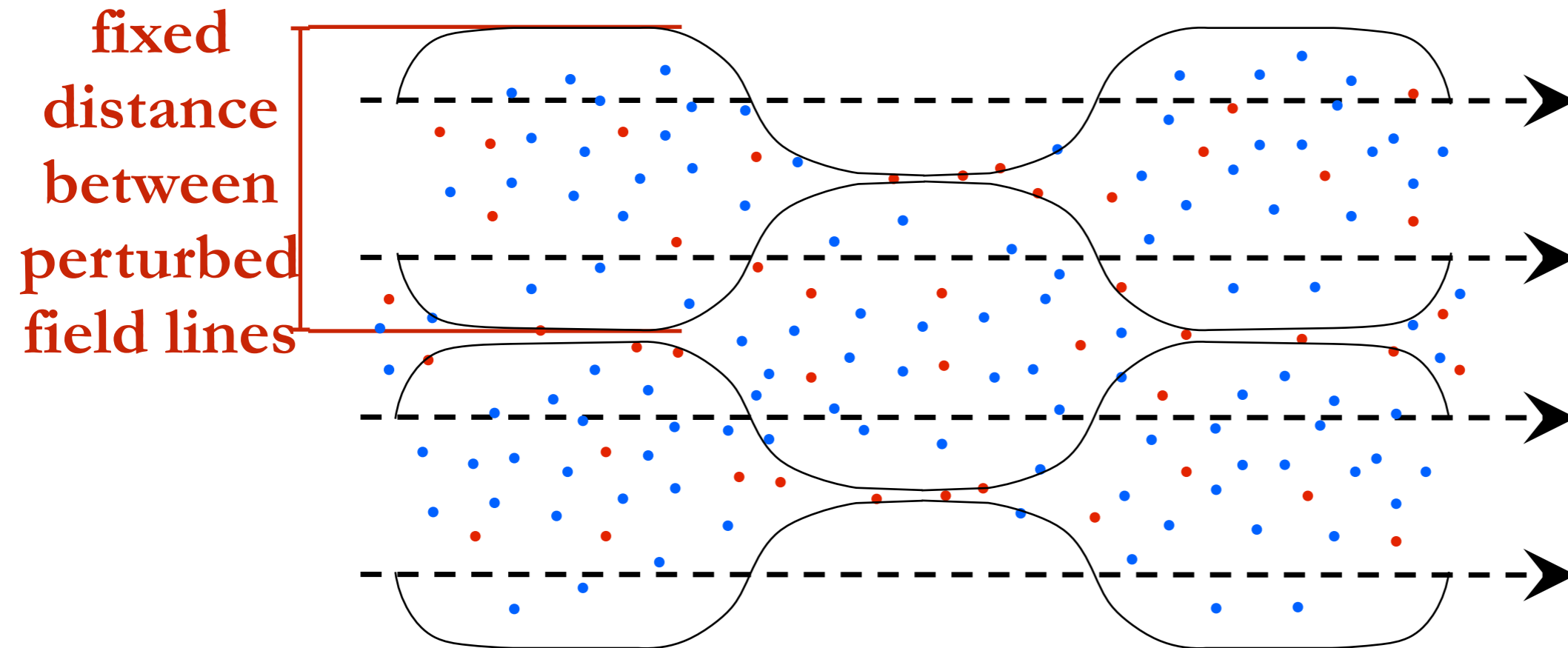
trapped

$$\frac{\rho_i}{H}$$



passing trapped

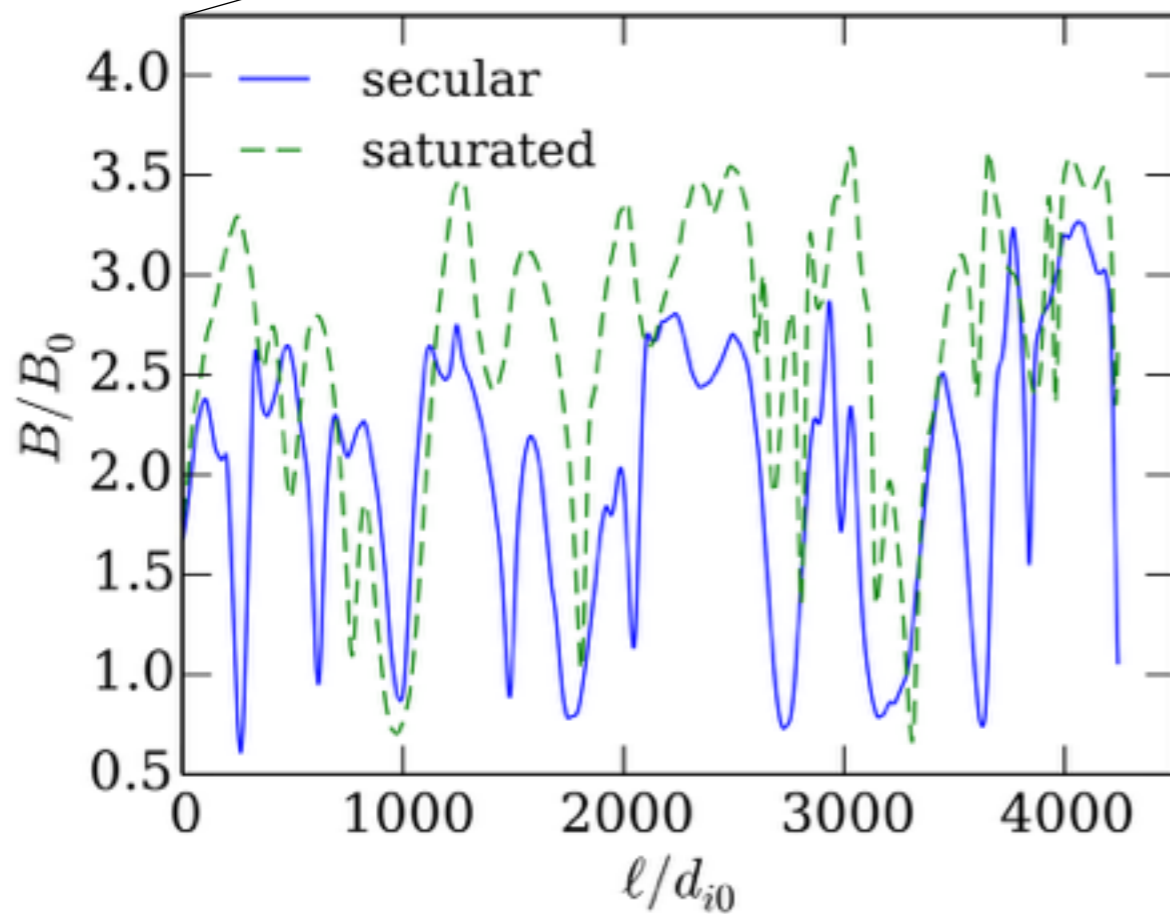
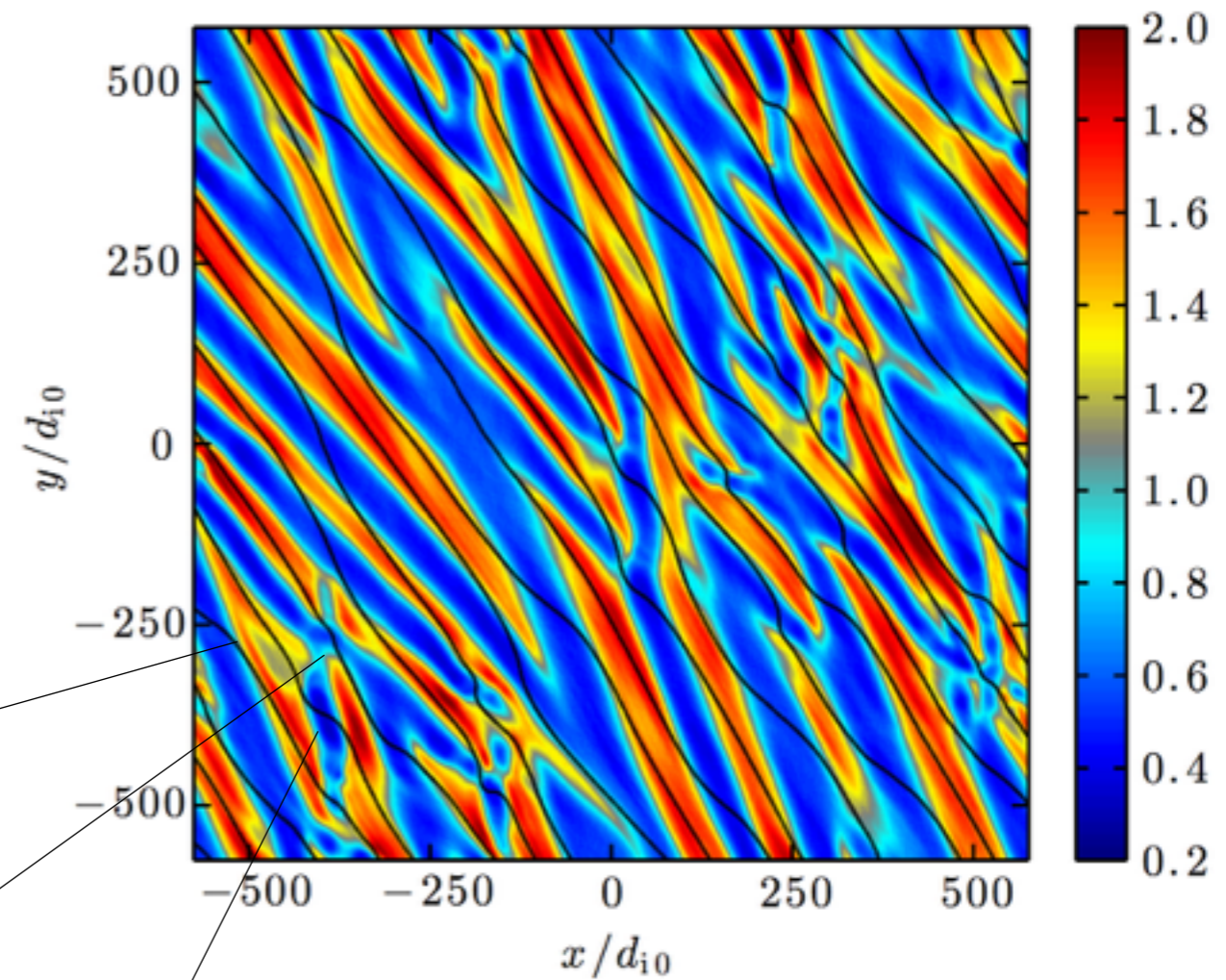
ρ_i
H



start pitch-angle scattering and leaking trapped particles

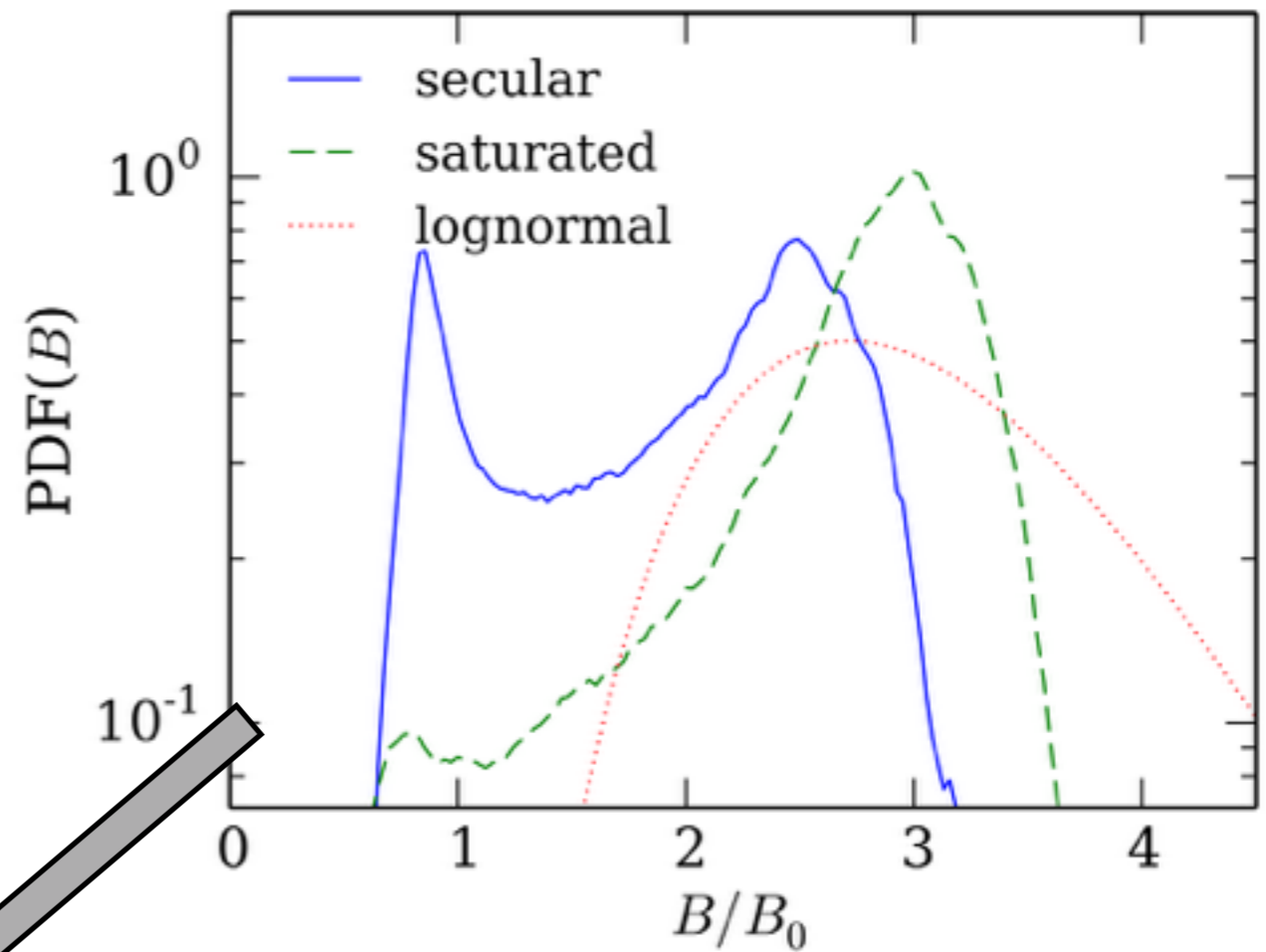
application: determination of
plasma thermal diffusion

extract B information
along magnetic-field line

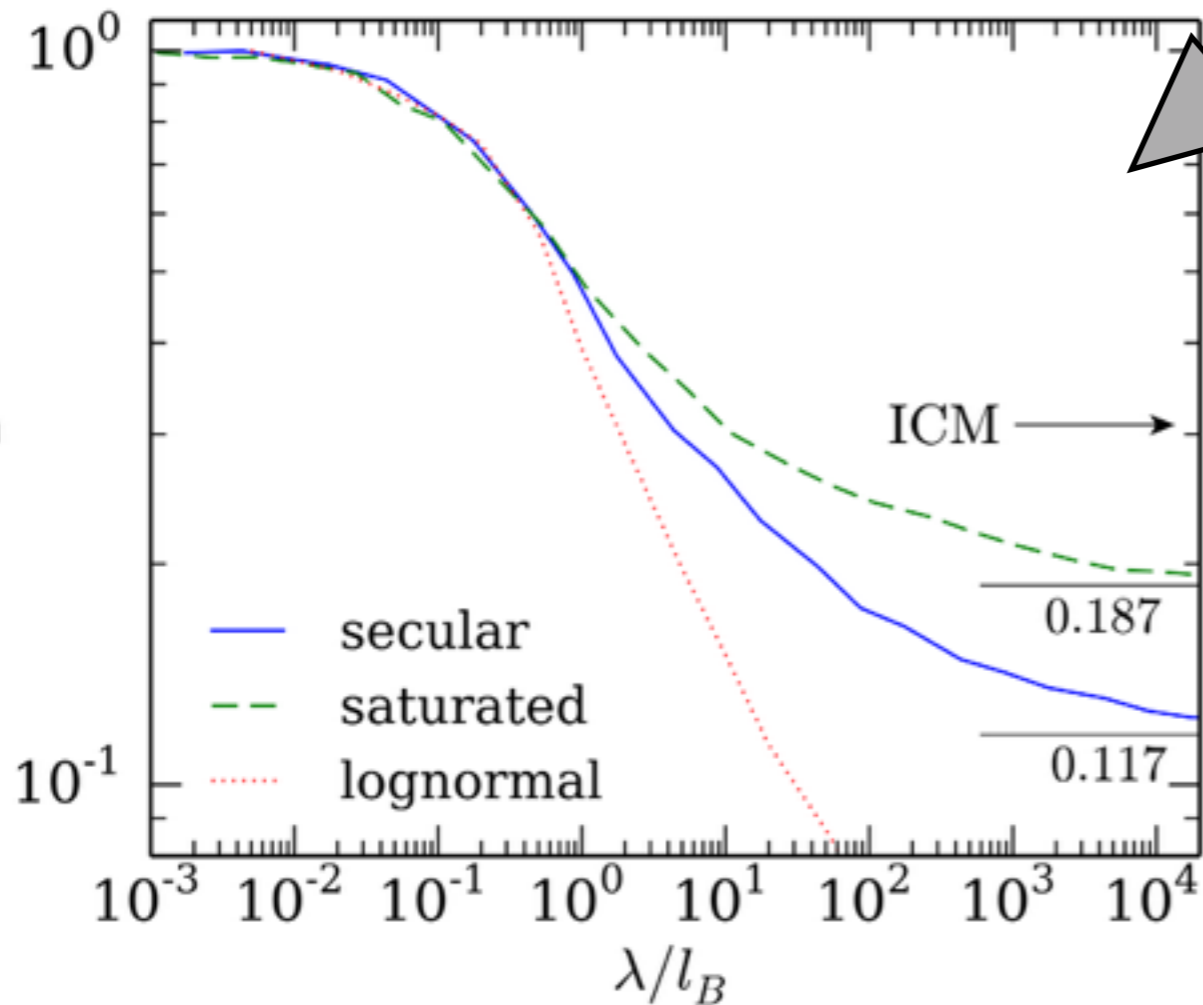


Sergey Komarov, Kunz,
Churazov, & Schekochihin
MNRAS 2016

compute PDF(B):



suppression of electron diffusion
as a fraction of unbridled Spitzer



suppression of electron conduction
as a fraction of unbridled Spitzer

$$S_{\kappa} \sim 0.2$$

see also Gareth Roberg-Clark's poster
& recent work by Riquelme *et al.* (2016)

another example application:
plasma dynamo

Try to **decrease field** strength, trigger firehose, and nearly instantaneously create an **effective viscosity** $\sim v_A^2 / S$.

This implies dynamo is nonlinear as soon as threshold is crossed, in that viscosity knows about β ;
hardly any kinematic phase, even when field is “weak”

Try to **increase field** strength, trigger mirror, the result being that most **particles don't** even **know** that the **mean field is increasing!**

explosive? Effective Re increases as B is changed.

Turbulent cascade can then get to smaller scales where field amplification is faster

working this out is a daunting task
(which is why my Ph.D. student, Denis St-Onge, is doing it)

just a taste of what we're doing...

$$\frac{\partial f_i}{\partial t} + \mathbf{v} \cdot \nabla f_i + \left[\frac{Ze}{m_i} \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right) + \frac{\mathbf{F}}{m_i} \right] \cdot \frac{\partial f_i}{\partial \mathbf{v}} = 0$$

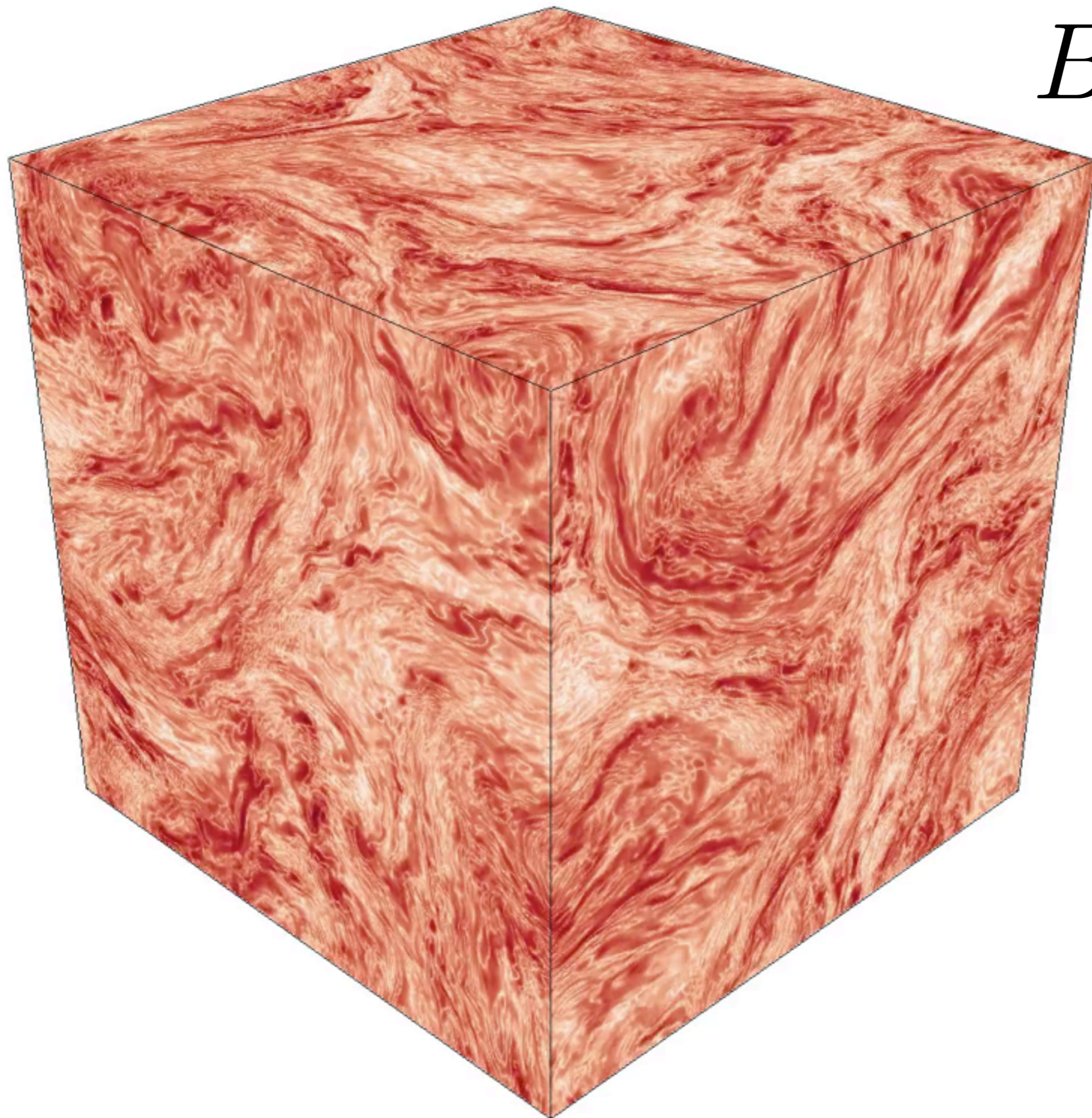
$$\nabla \cdot \mathbf{F} = 0. \quad k_f \in [1, 2] \times (2\pi/L)$$

forcing is time-correlated, with $\Omega_i t_{\text{corr}} \ll 1$.

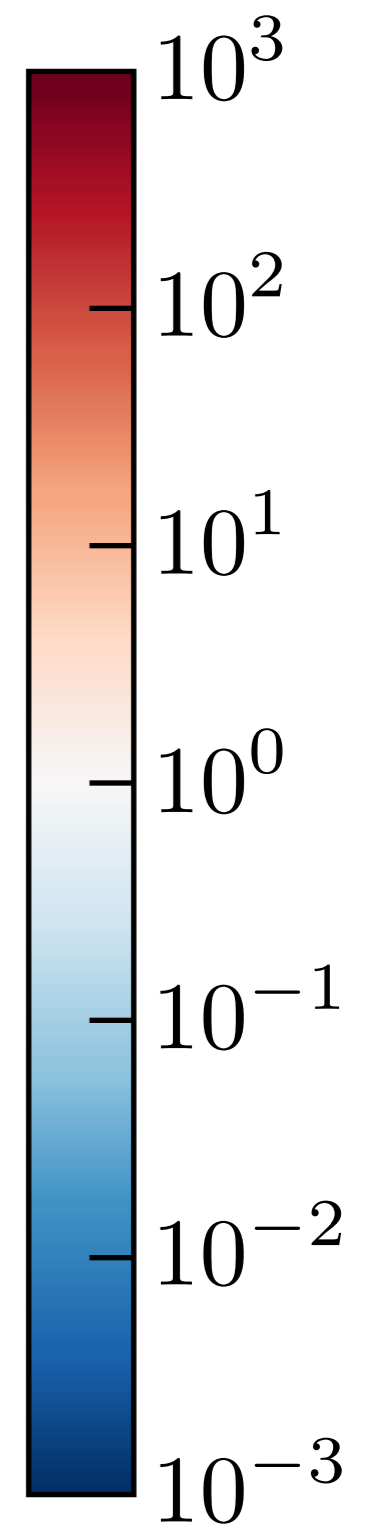
$$\Delta x \ll \rho_{i0} \ll L \quad \beta_{i0} = 10^4 - 10^8$$

$\sim 500^3$ and $\sim 1000^3$ cells

~ 30 billion particles



B



some results embargoed here

Linear Vlasov theory of a magnetised, thermally stratified atmosphere

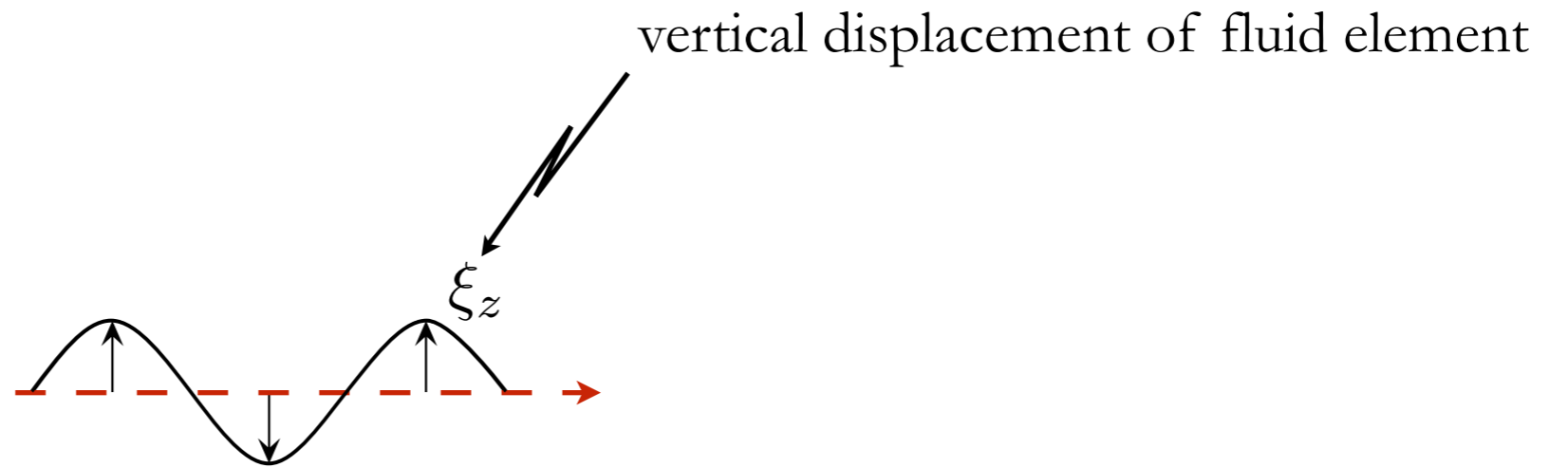
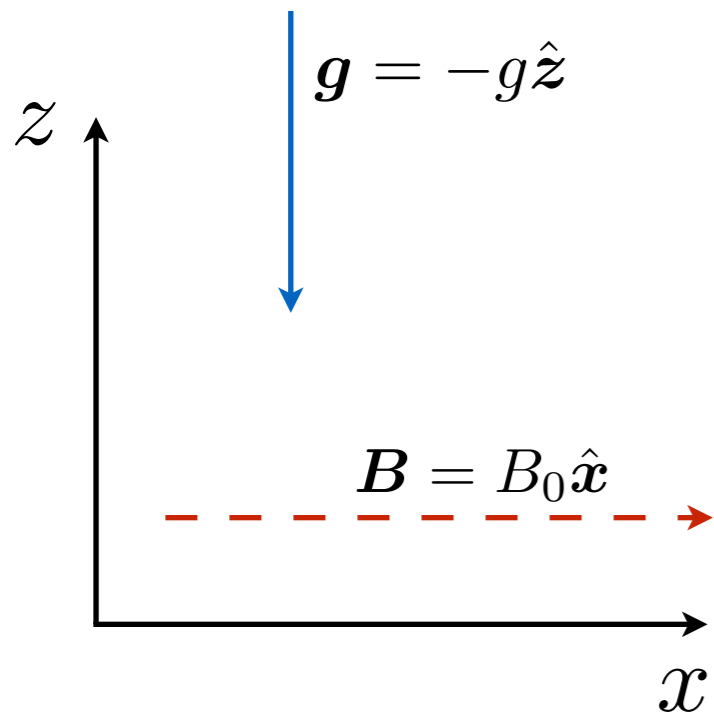
R. XU¹ AND M. W. KUNZ^{1,2†}

arXiv:1608.05316; to appear in *J. Plasma Phys.*

contains:

- 1) Review of convection in magnetized, collisional plasma
- 2) Discussion of convection in magnetized, collisionless plasma
- 3) Linear Vlasov theory:
 - i. Drift-kinetic limit
 - ii. Gyroviscous limit
 - iii. Gyrokinetic limit
- 4) Comparison with fusion-relevant convection (ITG/ETG)
- 5) Character-building algebra and unnecessarily long appendices

we worked *really* hard to make this clear and pedagogical!

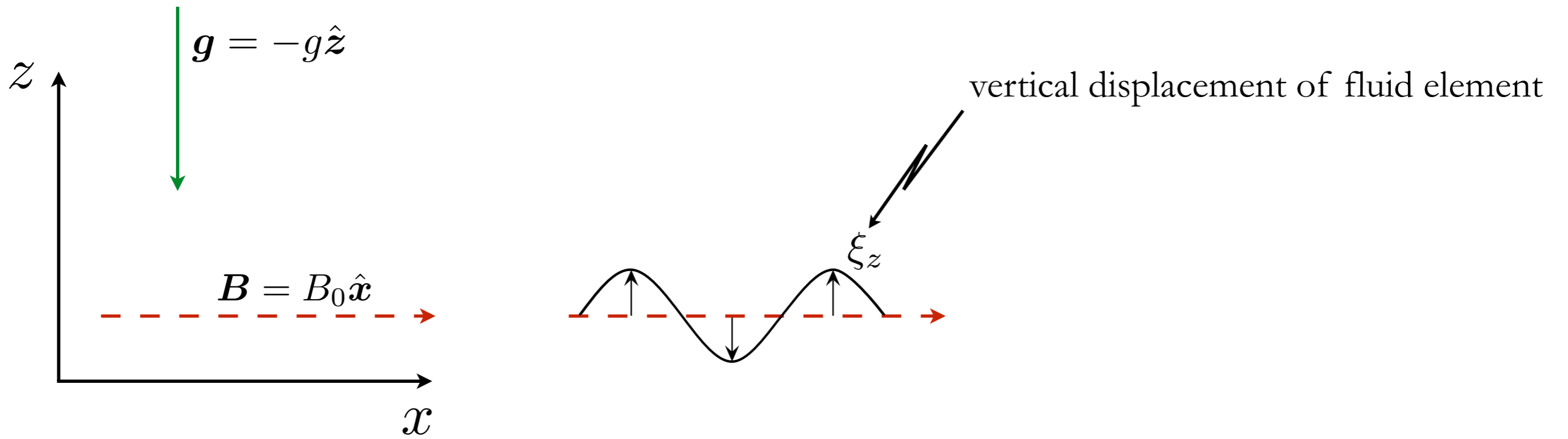


take limit $\omega \ll kv_{th}$:

$$\left(\frac{\partial}{\partial t} + \omega_{cond} \right) \frac{\delta T}{T} = - \left(\frac{N^2}{g} \frac{\partial}{\partial t} + \omega_{cond} \frac{d \ln T}{dz} \right) \xi_z$$

$$\omega_{cond} \rightarrow 0 : \frac{\delta T}{T} = - \frac{N^2}{g} \xi_z$$

$$\frac{\partial^2 \xi_z}{\partial t^2} = -N^2 \xi_z$$



take limit $\omega \ll kv_{th}$:

$$\left(\frac{\partial}{\partial t} + \omega_{cond} \right) \frac{\delta T}{T} = - \left(\frac{N^2}{g} \frac{\partial}{\partial t} + \omega_{cond} \frac{d \ln T}{dz} \right) \xi_z$$

$$\omega_{cond} \rightarrow \infty : \frac{\delta T}{T} = - \frac{d \ln T}{dz} \xi_z \implies \frac{\Delta T}{T} = 0$$

$$\frac{\partial^2 \xi_z}{\partial t^2} = -g \frac{d \ln T}{dz} \xi_z$$

Review of convection in magnetized, collisional plasma ©



Frozen magnetic fields serve as conduits along which heat flows from tethered fluid elements, one to the next; the rate of transport increases as B becomes more aligned with the gradient of T .

Magneto-thermal instability ensues. Balbus would be glad.

Balbus (2000, 2001)

Review of convection in magnetized, collisional plasma ©



But viscous transport
is also channeled along
magnetic-field lines,
coupling Alfvénic
fluctuations to slow modes;
 P is a tensor.

This time Alfvén waves
are buoyantly unstable.
Now Kunz is happy.

Kunz (2011)

That this carries over to a collisionless plasma is not obvious.

- 1) Inertia-bearing ions and conducting electrons need not remain in thermal equilibrium as the plasma is perturbed.
(No collisional equilibration.)

That this carries over to a collisionless plasma is not obvious.

- 2) Changes in temperature cannot be made independently of changes in magnetic-field strength when μ is conserved.

$$\frac{\Delta T_{\perp s}}{T_s} \doteq \frac{\delta T_{\perp s}}{T_s} + \xi_z \frac{d \ln T_s}{dz} = [1 - Z_1(\zeta_s)] \frac{\delta B_{\parallel}}{B},$$
$$\frac{\Delta T_{\parallel s}}{T_s} \doteq \frac{\delta T_{\parallel s}}{T_s} + \xi_z \frac{d \ln T_s}{dz} = \frac{2Z_3(\zeta_s) - Z_1(\zeta_s)}{Z_1(\zeta_s)} \left(\frac{\Delta n_s}{n_s} - \frac{\delta B_{\parallel}}{B} \right)$$

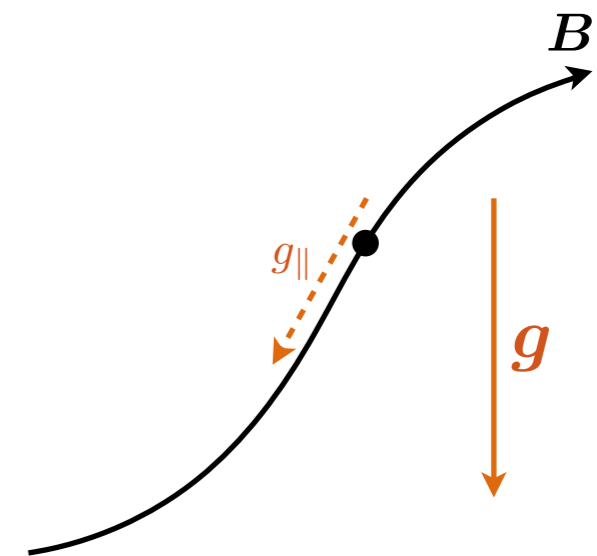
kinetic physics

That this carries over to a collisionless plasma is not obvious.

3) Collisionless damping!

$$\delta f_s(v_{\parallel}, w_{\perp}) = \underbrace{\frac{i}{k_{\parallel}} \frac{\partial f_s}{\partial z} \frac{\delta B_z}{B}}_{\text{MTI}} + \underbrace{\frac{w_{\perp}^2}{v_{th s}^2} \frac{\delta B_{\parallel}}{B} f_s}_{\mu \text{ conservation}} - \frac{i}{k_{\parallel}} \left(\underbrace{\frac{q_s \delta E_{\parallel}}{T_s}}_{\text{Landau damping}} + \underbrace{\frac{d \ln P_s}{dz} \frac{\delta B_z}{B}}_{\text{collisionless damping of MTI mode}} - \underbrace{ik_{\parallel} \frac{w_{\perp}^2}{v_{th s}^2} \frac{\delta B_{\parallel}}{B}}_{\text{Barnes damping}} \right) \frac{v_{\parallel}}{v_{\parallel} - \omega/k_{\parallel}} f_s$$

collisionless damping of MTI mode



That this carries over to a collisionless plasma is not obvious.

- 4) Pressure balance with surroundings usually maintained by radiating sound waves faster than fluid elements rise/sink; but sound waves are collisionlessly (Landau) damped.

That this carries over to a collisionless plasma is not obvious.

- 5) Conduction and buoyancy in a collisionless plasma are inextricably linked, a feature not present in a collisional fluid. Approximately isothermal displacements are tandem with the ability of those displacements to maintain pressure balance with their surroundings.

With $k_{\perp} = 0$ and $\zeta_i \doteq \omega/|k_{\parallel}|v_{thi} \ll 1$,

$$\frac{\delta P_{\perp}}{P} \sim \mathcal{O}(\zeta_i), \quad \frac{\delta P_{\parallel}}{P} \sim \mathcal{O}(\zeta_i^2), \quad \frac{\Delta T_{\perp}}{T} = 0, \quad \frac{\Delta T_{\parallel}}{T} \sim \mathcal{O}(\zeta_i) \quad (\text{collisionless, magnetised}).$$

vs.

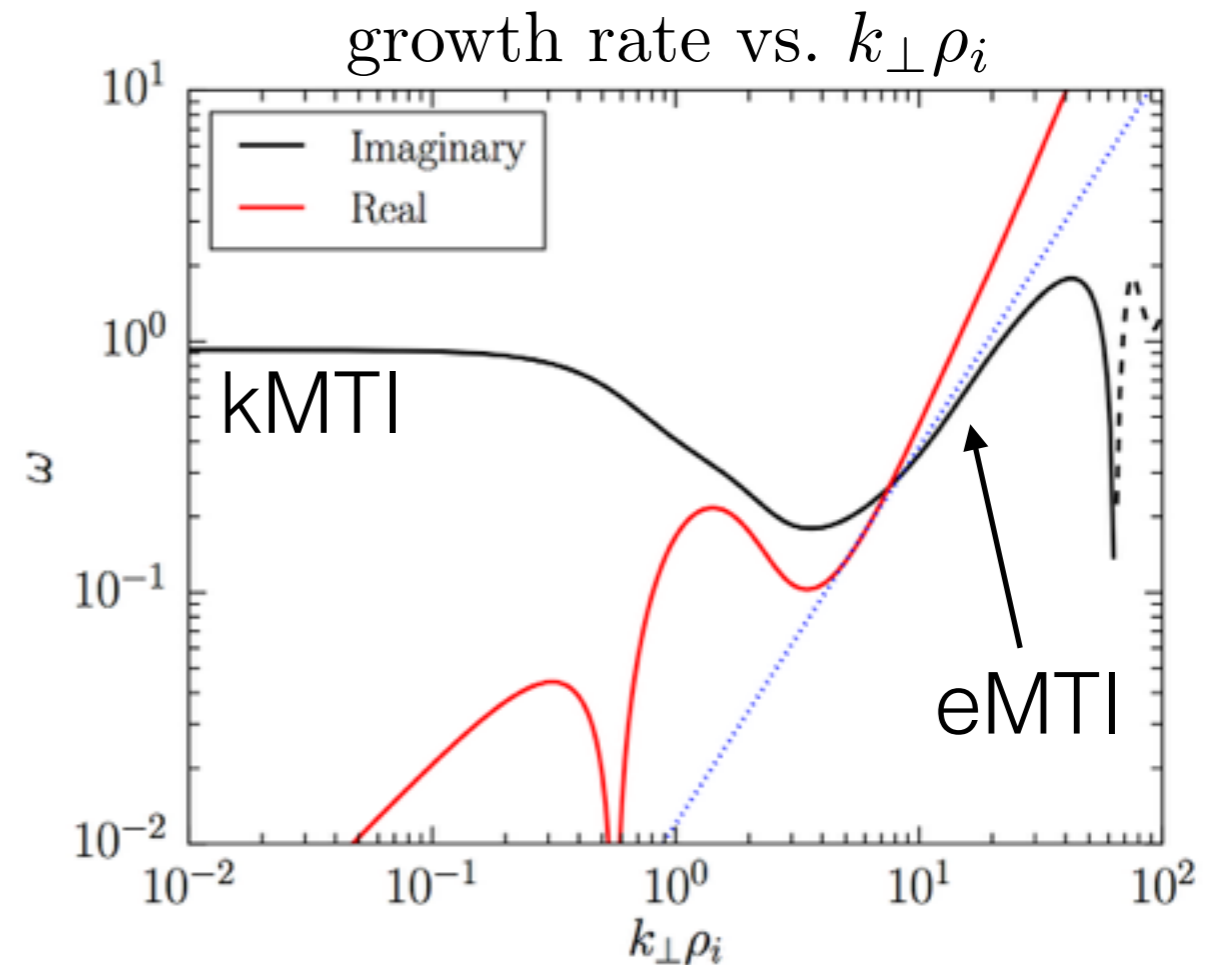
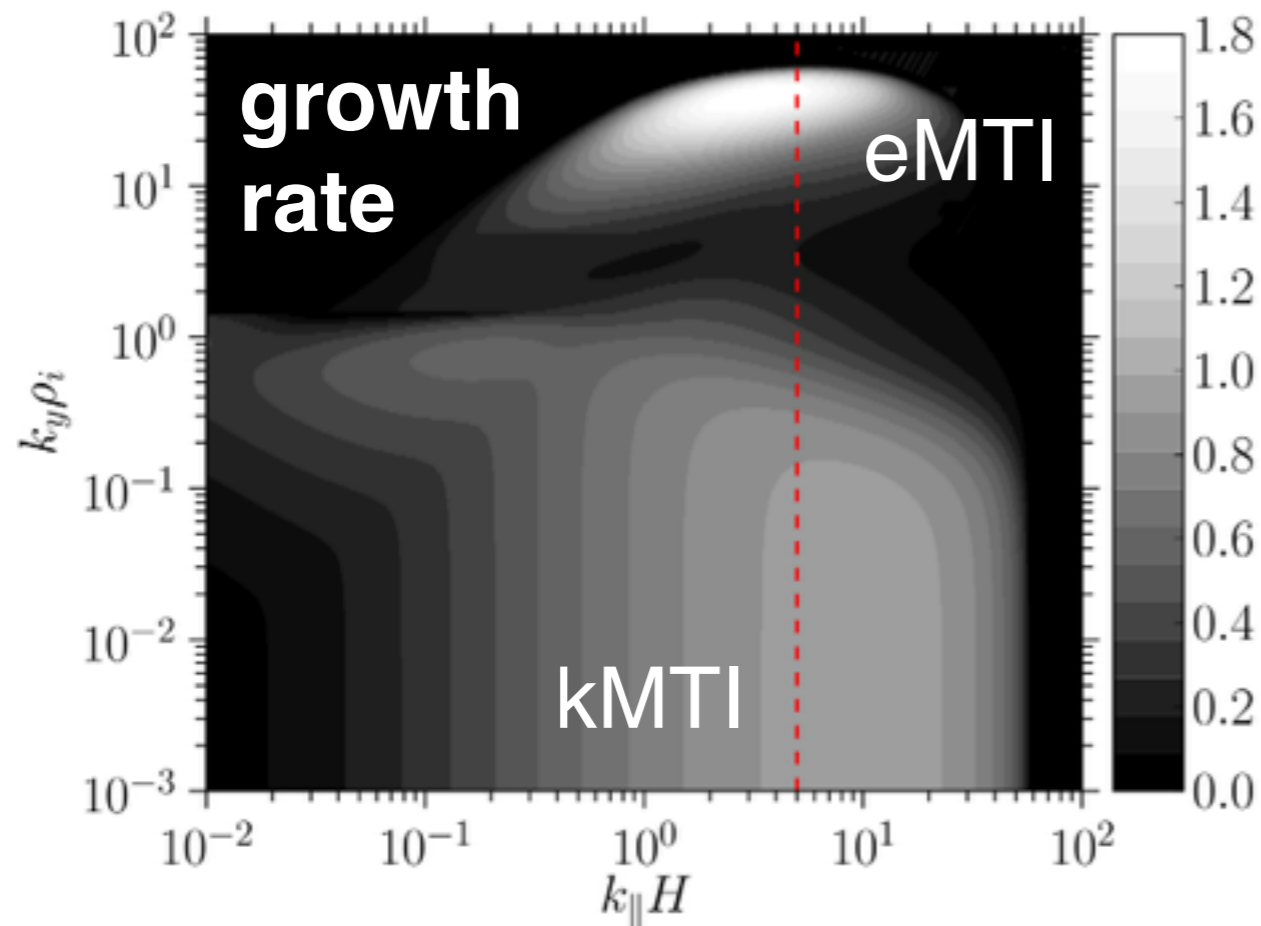
$$\frac{\delta P}{P} \sim \mathcal{O}(\zeta_i^2), \quad \frac{\Delta T}{T} \simeq \xi_z \frac{d \ln P}{dz} \frac{-i\omega}{k_{\parallel}^2 \kappa - (5/2)i\omega} \quad (\text{collisional, magnetised}).$$

Won't go through details here (read the paper!), but
MTI and Alfvénic-MTI basically carry over to collisionless case
(with some really fun physics and interesting differences)

and a surprise...

Finite Larmor Radius effects:

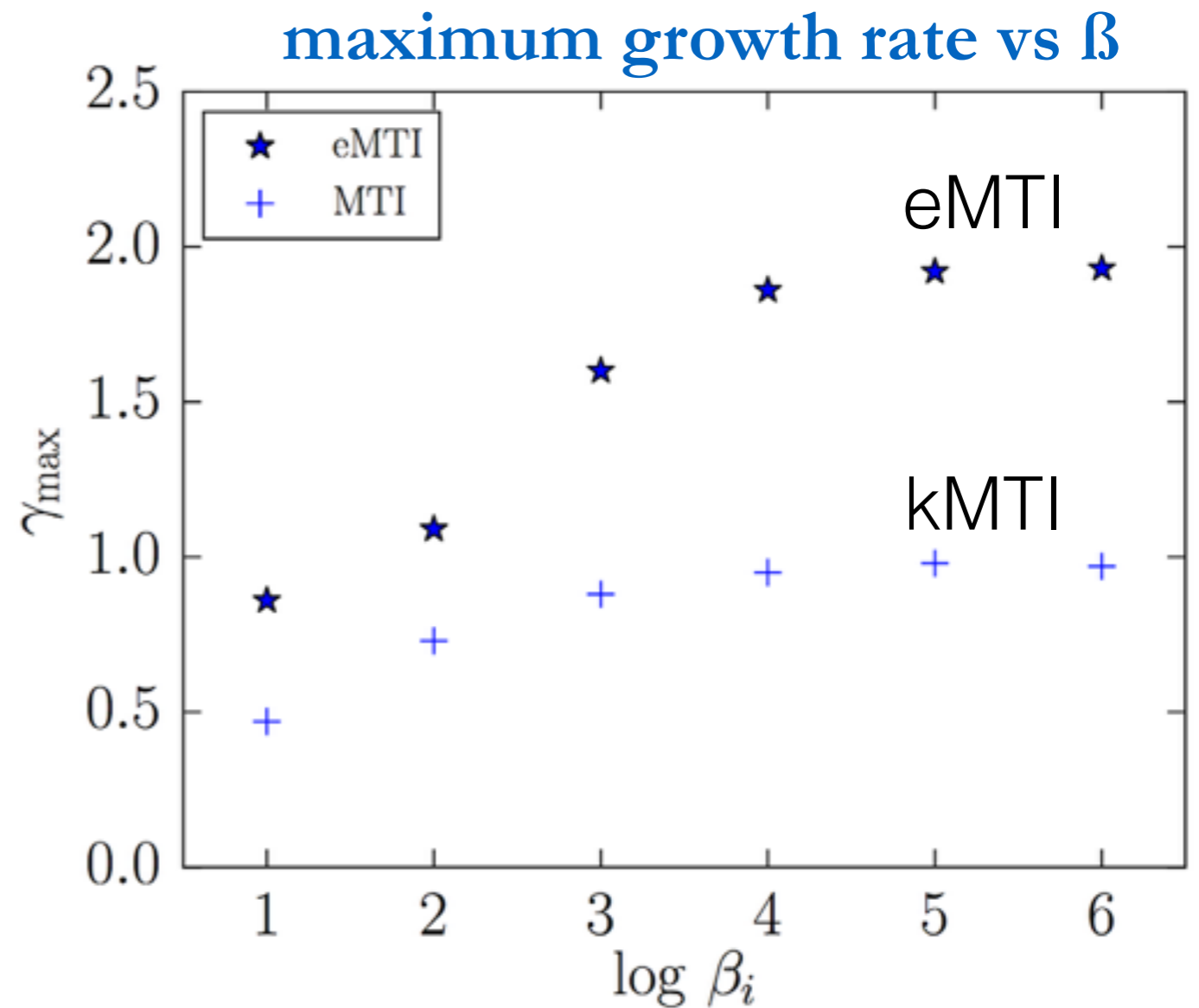
- 1) Vertical momentum can be transported in the (cross-field) horizontal direction — bad.
- 2) Gyroaveraging weakens fluid response at Larmor scales — bad.
- 3) Drift waves! Kinetic Alfvén waves! — good!
Leads to **new kind of magnetothermal instability.**



Larmor scales are more convectively unstable than are the large scales!

(drift wave coupled to a KAW)

same temperature gradient drives growth simultaneously at two disparate scales; implies large-scale MTI will likely depend upon saturation of Larmor-scale eMTI.



Summary

- (1) Micro-scale physics can play a fundamental role in dictating what macro-scale dynamics are allowed in a given system;
- (2) Ought to include effects of pressure anisotropy in studies of ICM:
 - reduces parallel transport of momentum and heat
 - accompanies and influences dynamo (possibly explosive at first)
- (3) Linear Vlasov theory still has some surprises in it.

Same temperature gradient drives growth simultaneously at large scales (drift-kinetic MTI) and small scales (electron-MTI), the latter with growth rates larger than the former.

Xu & Kunz, *JPP* (2016)

Komarov, Churazov, Kunz, & Schekochihin, *MNRAS* (2016)

Melville, Schekochihin, & Kunz, *MNRAS* (2016)

Kunz, Schekochihin, & Stone, *PRL* (2014)