

1 **Accessibility and the Ring of Unreliability**

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1 **ABSTRACT**

2 This study measures the variability of job accessibility via automobile for the Minneapolis-St. Paul
3 region. The accessibility analysis uses cumulative opportunity measures. The travel times on the
4 network are tested at various level (10th percentile speed, 50th percentile speed, 90th percentile
5 speed) using the TomTom speed data for 2010. It is shown that accessibility varies widely day-to-
6 day as travel speeds on the network vary. Some parts of the region (a ring around the core) have
7 more volatility in accessibility (and are thus less reliable) than others.

1 INTRODUCTION

2 Facing engineering failures such as bridge collapses, natural disasters like floods, and intentional
3 terrorist attacks, a progressively urbanized world has become increasingly vulnerable to interrup-
4 tions in its interconnected and interdependent networked transportation systems, including streets
5 and highways, transit routes, and truck-based supply chains. This research uses GPS data to in-
6 vestigate how transportation network performance depends on the variability of travel speeds, and
7 conjectures why some parts of the region are more reliable than others.

8 Recent efforts have assessed and validated GPS data from commercial vehicles for perfor-
9 mance measures highway traffic monitoring (1). The research team has developed a data process-
10 ing and analysis framework to generate performance measures from transit, truck, and auto GPS
11 data (2, 3, 4). Much of the transportation system is brittle, so small disruptions to the system could
12 result in widespread effects (5, 6, 7). The rise in nonrecurring congestion due to traffic incidents is
13 one example of how disruptions affect operations (8). Larger disruptions, such as Hurricane Sandy
14 or the 2014 Atlanta winter storm, propagate throughout highway, transit, and freight transportation
15 networks.

16 Transportation network structure has long been of interest to transport geographers, who
17 considered it an outcome of an evolutionary process and an input into travel behavior and system
18 performance (9, 10, 11, 12, 13, 14, 15) and more recently physicists looking at the geography and
19 spatial aspects of transportation networks to understand and reproduce their qualitative features
20 (16, 17).

21 In transportation, the research team and others have picked up the research thread relating
22 street network structure to travel behavior and system performance, such as the impacts of net-
23 work topology and its evolution over time on commuting patterns (18), the relationship between
24 network circuitry and residential location choice relative to work (19), the relationship between
25 network structure and travel distance (20) and travel time perception (21), how network structure
26 and travel patterns affect the long-term vulnerability of road (22, 23) and transit networks (24) and
27 the relationship of road safety to street network characteristics (25).

28 Transportation systems are designed and constructed as interdependent layered networks.
29 The hierarchy of services include short and long distance transportation services (e.g buses, freight)
30 that make use of different and overlapping parts of the street network. The question of resilience
31 is relevant to most of these layers. Transportation will be interrupted to a greater or lesser extent
32 if the physical alignment is blocked (e.g. flood, snow, hazmat leak), if the road or bridge structure
33 failures (e.g. potholes, sinkholes, heaving, a bridge collapse), if traffic control devices (signs,
34 markings, signals) fail or deteriorate (e.g. an electrical outage, weathering), if vehicles fail to work
35 (e.g. gasoline shortages (or electrical outages in the case of EVs), or system-wide vehicle recalls),
36 if the driver is unable to drive the vehicle (e.g. strikes or illness), or if a service is interrupted (e.g.
37 airplanes are grounded, trains or buses are cancelled, traveler information systems are disrupted
38 (26)). Overuse of transportation facilities (congestion) may lead to a type of traffic failure that
39 results when travel times increase beyond an acceptable level (or the area reachable in a given time
40 shrinks). This can have consequences ranging from annoying to critical.

41 Within these layered networks are a hierarchy of roads and services. The hierarchy of
42 roads is an emergent phenomenon (27, 28) that has become enmeshed in road and highway design
43 – some roads are more significant (faster, more intensively used) than others. Similarly, transit
44 systems are often designed with feeder routes connecting with regional routes, and freight systems
45 have collector / distributor networks (local delivery networks) that connect to a long distance sys-

1 tem. This hierarchical arrangement is also common in other networked utility systems (electrical,
2 natural gas, water, etc.).

3 The foremost purpose of transportation is to connect people and things. While speed on
4 the network is an important aspect of this, it is not the only feature, the connectivity of the network
5 and its circuitry also matter. The effectiveness of the network also depends on the distribution of
6 activities.

7 Accessibility, the ability to reach valued destinations is a widely used metric of the effec-
8 tiveness of transportation networks (29, 30, 31, 32, 33, 34, 35, 36). However it has until recently not
9 been measured (and instead has been estimated from models), and it has usually been considered
10 from the perspective of mean or expected travel times, rather than accounting for the distribution
11 of travel times that we see every day.

12 The study of travel time reliability considers the variability of the transportation network,
13 and provides needed attention to the observation that the performance of the system is not generally
14 a binary (can I reach it?), but continuous (how easily can I reach it?) and variable (how predictably
15 can I reach it?).

16 This research connects the idea of travel time reliability with accessibility, and conjectures
17 the features of network structure that might explain the findings. Sections 3, 4, 5, and 6 discuss the
18 Data, Methods, Results, and Conclusions in turn.

19 **DATA**

20 Several different sources of data are applied in this research.

21 The first is GPS speed data for the year 2010. Comprehensive GPS data have high spatial
22 and temporal coverage on the most widely traveled links, and reflect the actual driving patterns
23 of drivers with GPS data. While this may not be perfectly representative of the population as a
24 whole, it is the best available data, and there is no reason to believe the speeds that are reported
25 are systematically biased due to sampling. (It is possible that flows on the links estimated from
26 GPS traces are biased by sampling drivers with GPS devices, which may not be typical). This
27 study employs data from TomTom, which was acquired by the Metropolitan Council. The original
28 data were collected by millions of GPS logging and navigation devices, while the speed data were
29 aggregated and processed based on that (37).

30 TomTom speed data were organized based on road classifications, time periods and speed
31 percentiles. For 8 Functional Roadway Classification (FRC), speed data were separated into 4
32 groups, in which FRC0 to FRC4 were grouped into one dataset. For different time periods, con-
33 sidering the traffic properties, the time of a day was divided into seven parts, including Overnight,
34 Morning Peak Hours (Two parts), Mid-Day, Evening Peak Hours (Two Parts) and Evening. More-
35 over, for each group, different percentiles of speed measurements, from 5th percentile to 95th
36 percentile, in the same time period of a day were joined in the same databases. The 5th percentiles
37 speed shows the speed on links in the times which were the fastest 5 percent of those recorded,
38 while the 95th percentile speeds similarly stands for the lowest speed.

39 The road network linked to TomTom data was obtained together with TomTom speed data
40 from TomTom by the Metropolitan Council, which was used as a map shape file. It could help to
41 analysis the road network, like searching for the shortest travel time paths between certain origins
42 and destinations, based on the link speed.

43 The second data source that we used is TIGER/Line Shapefiles at the Block Level of Min-
44 nesota in 2010, which were acquired from the United States Census Bureau (38). The data contains

1 selected geographic and cartographic information in Minnesota, which works in a GIS environ-
 2 ment such as ArcGIS. In our research, the features in Twin Cities were selected from Minnesota's
 3 Block level based on locations, and the centroids of each block were extracted as the origins and
 4 destinations that we used to measure the accessibility.

5 The third data set is the LODES 7.0 dataset, which stands for the LEHD Origin-Destination
 6 Employment Statistics, where LEHD itself stands for Longitudinal Employment Household Dy-
 7 namics, which was also obtained from the United States Census Bureau (39). For measuring the
 8 job accessibility, we used the Workplace Area Characteristic Data, in which the number of jobs
 9 are integrated by work census block in 2010. Based on the Census Block Code, the employment
 10 information could be jointed with the geographic information at the Census Block Level.

11 METHODS

12 The Cumulative Opportunity Measure (40, 41) is the most basic method to calculate accessibility.
 13 The Cumulative Opportunity measure counts the number of opportunities (destinations) within
 14 a given travel time threshold using a certain transportation mode. For accessibility to jobs, the
 15 opportunity refers to the number of jobs. While there are many more sophisticated measures (such
 16 as a gravity and utility-based measures), they are not directly measurable, and do not have physical
 17 meaning. Hence, the cumulative opportunity measure for job accessibility is typically expressed
 18 as,

$$A_i = \sum_j O_j f(C_{ij}) \quad (1)$$

$$f(C_{ij}) = \begin{cases} 1 & \text{if } C_{ij} \leq T \\ 0 & \text{if } C_{ij} > T \end{cases} \quad (2)$$

19 Where:

20 A_i stands for the job accessibility of block i ,

21 O_j stands for the number jobs in block j ,

22 C_{ij} stands for the shortest travel time between block i and block j ,

23 T represents the travel time threshold.

24 The cumulative opportunity measure is a simple way to explain and calculate accessibility
 25 since its cost function is binary, which is determined by the predetermined time threshold and the
 26 cost. This measure of cumulative opportunity is calculated for each block using the data described
 27 in Section 3.

28 Based on the cumulative opportunity measure, the process of measurement was divided
 29 into two parts.

30 The first part was to use the ArcGIS to search for the shortest travel time path (using the
 31 network speeds from TomTom) and calculate the travel time for traveling from each origin to each
 32 destination. These OD travel times are used in the cumulative opportunity function by comparing
 33 them with the predetermined time threshold.

34 The second part was to join the job opportunity with the cost function to calculate the job
 35 accessibility for each origin. Considering the data scale of OD Matrix on the census block level,
 36 SQL Server were used to process the accessibility calculation. The results of job accessibility
 37 covers 54775 blocks in the seven counties of the Twin Cities.

1 RESULTS

2 Figures 1 shows the job accessibility measurement with the time threshold of 20 minutes based on
 3 the 50th percentile speed. The basic distribution pattern of job accessibility in the Twin Cities was
 4 represented by this map.

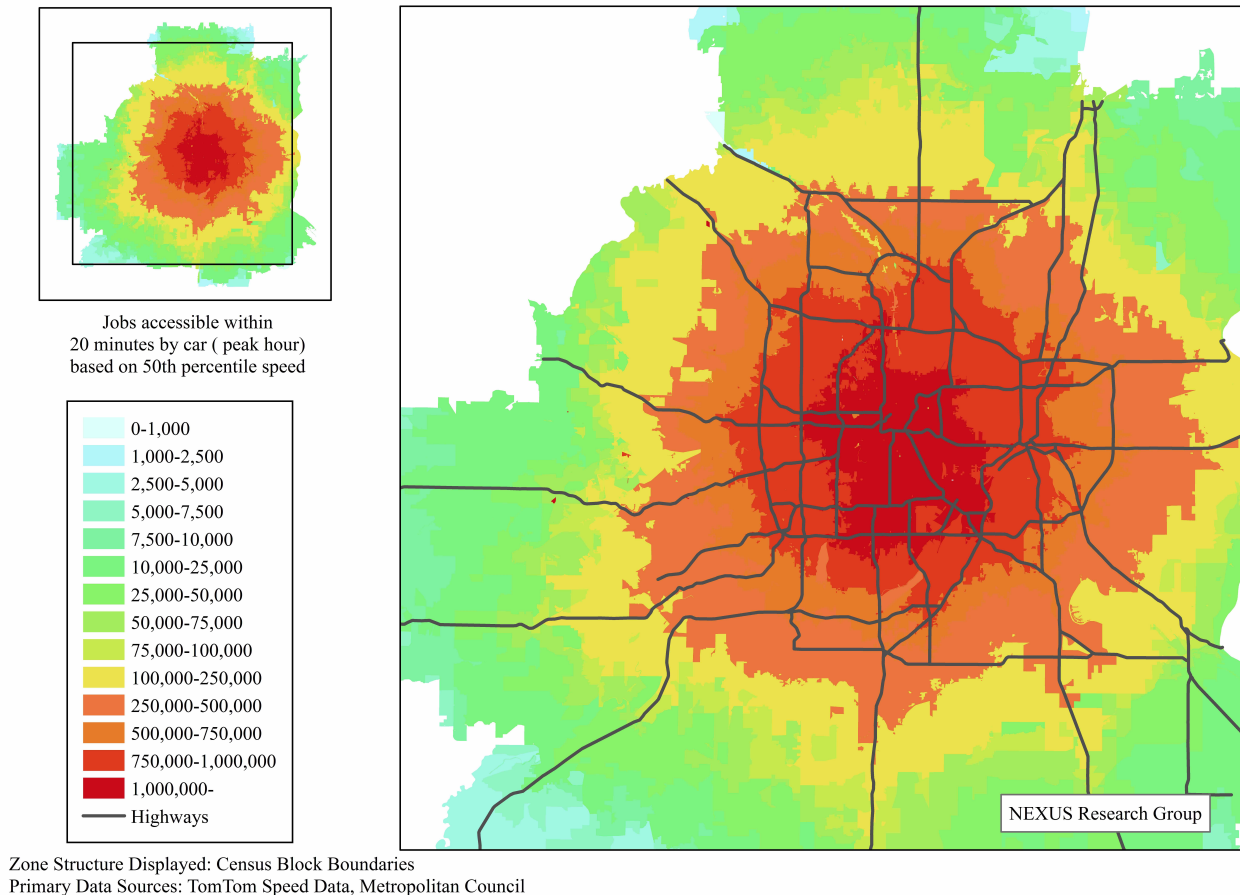
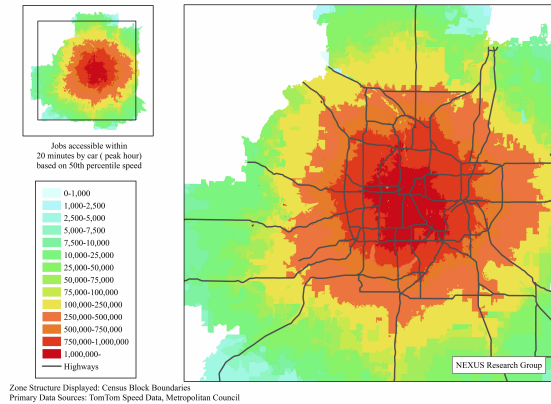


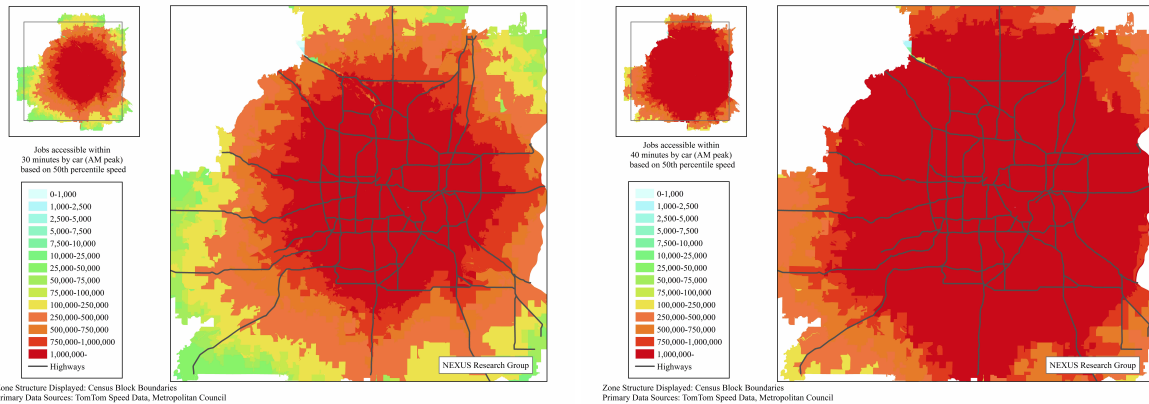
FIGURE 1 : Job accessibility in 20 minutes based on the 50th percentile speed

5 The blocks with higher job accessibility are centered on downtown Minneapolis, which is
 6 visualized with the red color. With the increase of distance to the downtown area, the colors in
 7 Figure 1 change gradually from red to light blue, which illustrates the decline of job accessibility.
 8 In the exurban areas, the blocks have the lowest job accessibility. This condition comports with
 9 our understanding of the region, since the number of jobs in and around the downtown area are
 10 relative higher than in the far reaches, so suburbanites and exurbanites need more time to reach the
 11 same number of jobs. As a result, land prices are typically higher in central areas, as people and
 12 firms pay a premium for accessibility.

13 With different time thresholds, the results of job accessibility change significantly. Figures
 14 2a, 2b, and 2c shows the job accessibility measurements with time thresholds of 20 , 30, and 40
 15 minutes respectively. In all of these figures, the speed on the network is still set as 50th percentile
 16 speed.



(a) Job accessibility in 20 minutes based on the 50th percentile speed



(b) Job accessibility in 30 minutes based on the 50th percentile speed

(c) Job accessibility in 40 minutes based on the 50th percentile speed

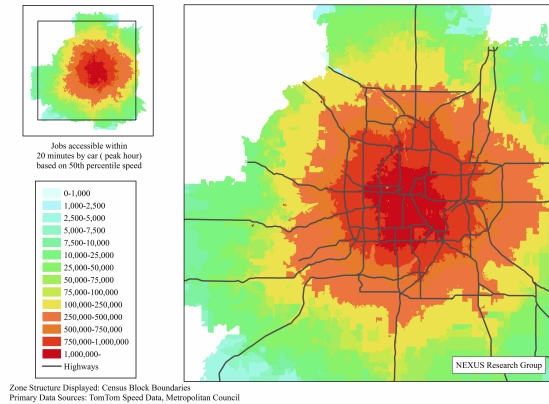
FIGURE 2 : Job accessibility in different time thresholds based on the 50th percentile speed

1 From Figures 2b and 2c we see that an expansion of the red area centering on the downtown
 2 occurs with the increase of time threshold. It is obvious that the most of the Twin Cities region has
 3 a high job accessibility when the time threshold was set as 40 minutes.

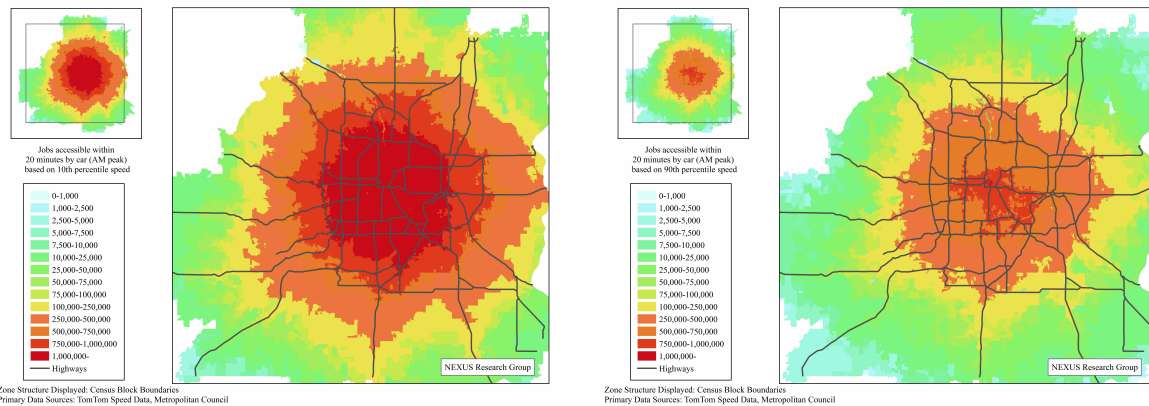
4 Based on the cumulative opportunity measure, another important parameter could influence
 5 the job accessibility measurement is travel time. To find the distribution pattern of job accessibility
 6 based on different travel time, the 10th percentile speed and the 90th percentile speed of the road
 7 network were chosen to calculate the shortest travel time. We set the time threshold as 20 minutes.

8 The changes of accessibility distribution are clearly shown in Figures 3b and 3c. When
 9 10th percentile speed was set on the road network, more blocks show higher accessibility to jobs
 10 than 90th percentiles speed since the red area in Figure 3b is larger than that in Figure 3c. The
 11 changes are also clearly reflected from Figure 4a, 4b, and 4c , which shows the difference of job
 12 accessibility based on different percentile speed on the road network.

13 The explanation for this condition is also reasonable that more destinations are reachable
 14 on the road network with higher speed. Hence, the job accessibility measurements of 10th and 90th
 15 percentile speed have a larger differences than that of 10th and 50th, and 50th and 90th. Moreover,



(a) Job accessibility in 20 minutes based on the 50th percentile speed

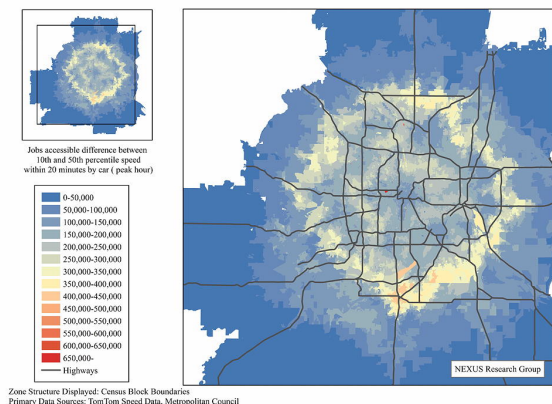


(b) Job accessibility in 20 minutes based on the 10th percentile speed

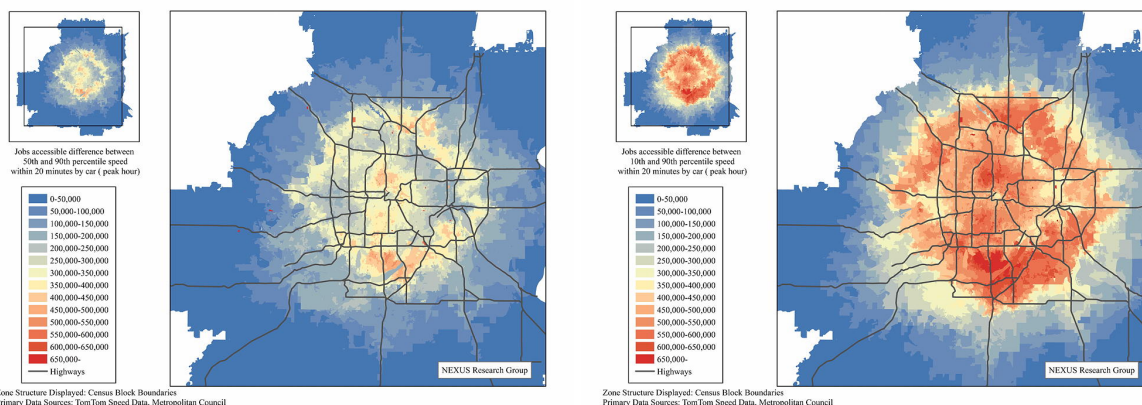
(c) Job accessibility in 20 minutes based on the 90th percentile speed

FIGURE 3 : Job accessibility in 20minutes based on the network with different percentile speed

- 1 Figures 4a, 4b, and 4c show a clear ring on each map.
- 2 This “Ring of Unreliability” shows where job accessibility within 20 minutes differs most
- 3 greatly at the 10th and 90th percentile speeds. In short, the ring illustrates the origins that suffer
- 4 most due to travel time variability. While we expected some areas to be more reliable than others,
- 5 this ring pattern is especially noticeable.
- 6 Notably this is most prominent in the outer suburbs (along the I-494/I-694 beltway around
- 7 the Twin Cities).
- 8 In part this is a feature of a cumulative opportunities measure. Some part of the region is
- 9 just inside or just outside some number of jobs within 20 minutes, and since jobs are spatially con-
- 10 centrated, even a small perturbation in travel times will move some that were inside the threshold
- 11 to just outside. However, the magnitude of the changes (several hundred thousands of jobs), is
- 12 much greater than the difference between finding one job center within 20 minutes or just beyond
- 13 20 minutes. The region’s largest job center, the Minneapolis Central Business District, has only
- 14 100,000 or so jobs (depending on definitions), about 6 percent of the region’s total (42).
- 15 Figure5 shows the patterns of "the ring of unreliability" in different time thresholds from 10



(a) The difference of job accessibility between 10th and 50th percentile speeds



(b) The difference of job accessibility between 50th and 90th percentile speeds

(c) The difference of job accessibility between 10th and 90th percentile speeds

FIGURE 4 : The difference of job accessibility between networks with different percentile speeds

1 minutes to 60 minutes. Since people care more about the traffic delay in reality, only the differences
 2 of job accessibility between 50th and 90th percentile speed are showed in Figure5. On each map,
 3 the ring is showed clearly and noticeable, which proved the existence of the ring is not constrained
 4 by the time threshold in a cumulative opportunity measure. However, from Figure5, we can see
 5 that the time threshold affects the geographical distribution of the ring. A higher time threshold
 6 would result in the spreading of the "unreliability ring" and moving the ring farther from the down
 7 town area.

8 Time-weighted accessibility is a complete accessibility measure, which combined different
 9 time threshold with a different impedance (43). Based on the definition of time-weighted accessi-
 10 bility, it could be expressed as,

$$A_{i,time-weighted} = \sum_{T=10}^{60} (A_{i,T} - A_{i,T-10})e^{\beta * T} \quad (3)$$

11 The differences of time-weighted accessibility between 50th and 90th percentile speed are
 12 showed in Figure 6. The "ring of unreliability" is also clearly showed on the map. And it distributes

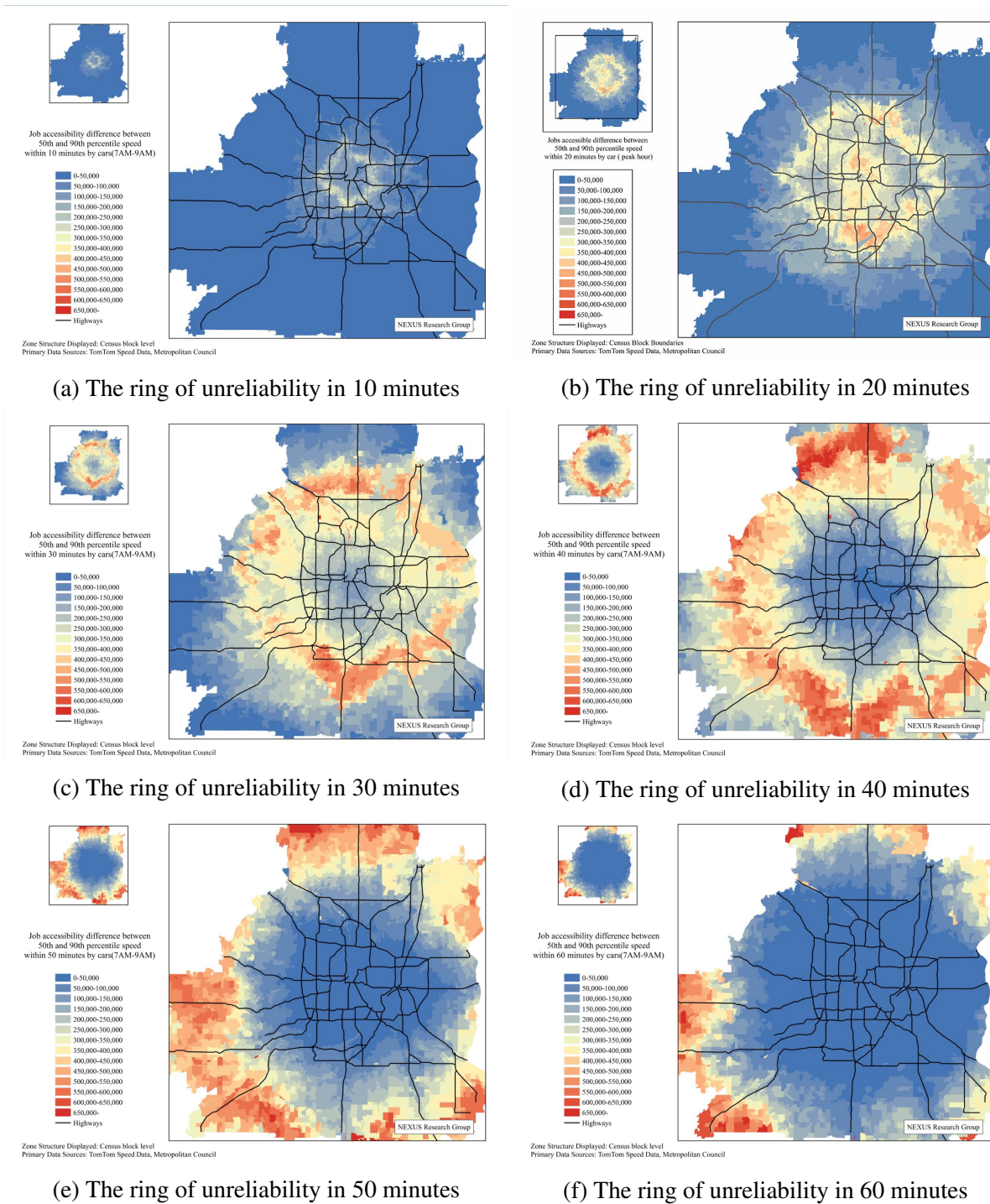


FIGURE 5 : The ring of unreliability in different time thresholds from 10 minutes to 60 minutes

1 around the down town area, and has the similar location as differences in 20 minutes.

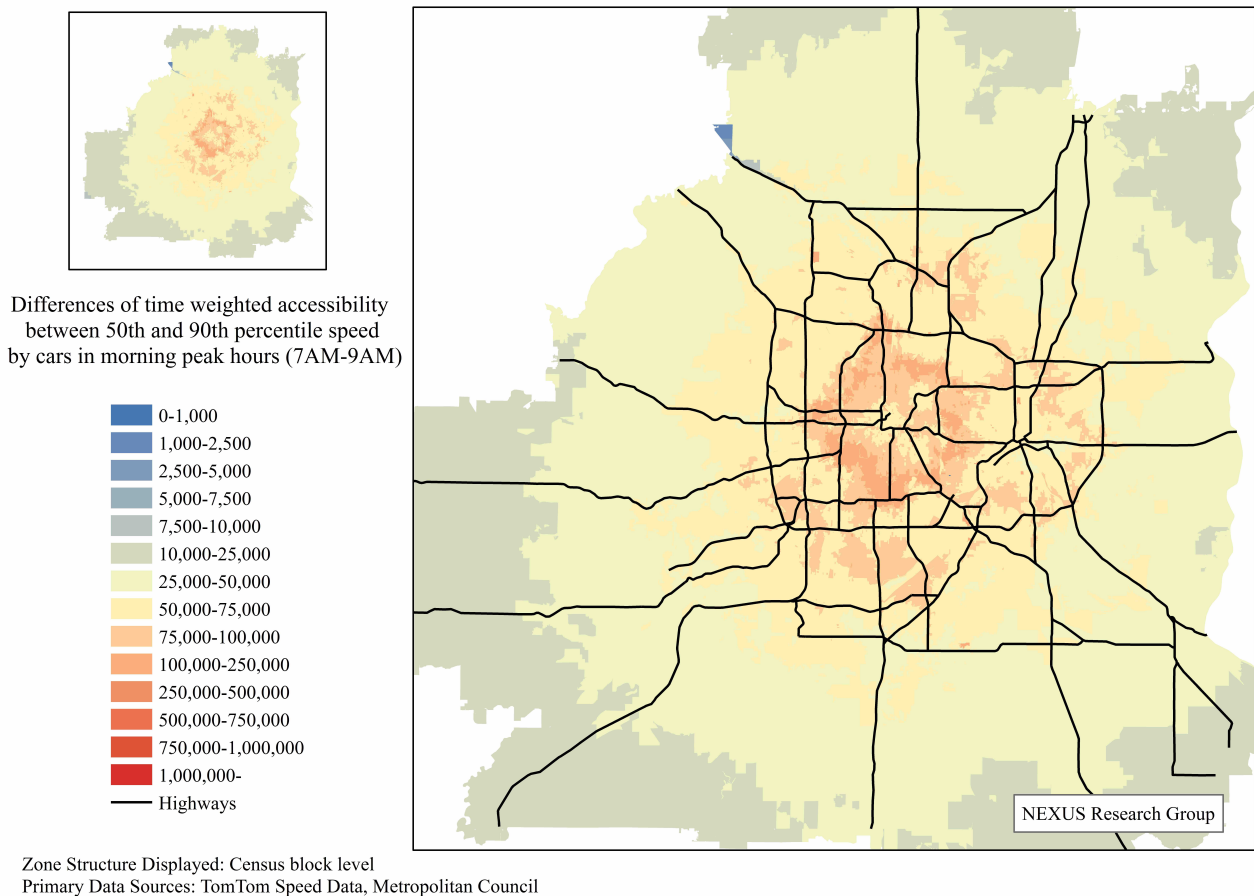


FIGURE 6 : The time weighted difference of job accessibility between 50th and 90th percentile speeds

- 2 We conjecture the following reasons, which will be tested in future research:
- 3 1. People living in the outer suburbs use freeways for a larger proportion of their travel,
- 4 particularly to work than those in the core cities and inner suburbs.
- 5 2. Freeways are more vulnerable to incidents than a connected arterial network because
- 6 their limited access and egress points and expect to see that freeways have a wider
- 7 percentage variation in travel times than arterials.
- 8 3. The very economy of scale that results in freeways having a lower average travel time
- 9 (higher speed) makes them less reliable and more vulnerable to incidents.

1 CONCLUSION

2 This study measured the accessibility to jobs in the Twin Cities region based on the TomTom road
3 speed network data for 2010 and illustrated how accessibility to jobs changes at different time
4 thresholds and speed percentiles on the road network.

5 First, job accessibility measurement in the Twin Cities has a clear distribution pattern that
6 the downtown area has higher job accessibility, while suburban area has lower one.

7 Second, time threshold is an important parameter for measuring accessibility when using
8 the cumulative opportunity measure. The influence pattern is as expected, in that a larger time
9 threshold results in higher accessibility.

10 Third, job accessibility measurement depends significantly on the speed on the road net-
11 work. Higher speeds increase the number of job opportunities that can be reached in a given time.
12 This result reflects an efficient way to increase the job accessibility that is to improve the speed on
13 the road network.

14 Fourth, the difference in job accessibility at different percentile speeds displays a prominent
15 ring pattern in different time thresholds, with the greatest loss in job accessibility found in a ring
16 around the center of the region. Time threshold affects the graphical distribution of the ring. A
17 higher time threshold causes a ring farther from the downtown area. The differences in time-
18 weighted accessibility to jobs also show the ring clearly around the center area, which is similar to
19 the patterns in 20 minutes. The existence of the ring is associated with an increased dependence on
20 freeways for travel in lieu of local streets. The network connectivity in the second, third, and fourth
21 ring suburbs is typically lower than in central cities (and older first ring suburbs). Thus it is more
22 vulnerable to incidents, as it is more highly channelized, and this is reflected in the large differences
23 in accessibility for 10th and 90 percentile speeds. We dub this the "Ring of Unreliability".

24 This study only considered the morning peak period, future study should examine other
25 periods of the day and particularly peak vs. non-peak periods, to see if the "Ring of Unreliability"
26 remains. More complex accessibility measures can be considered to see whether this relationship
27 remains with a composite (weighted cumulative opportunity) accessibility measure, rather than
28 just at a single time threshold. We hypothesize the pattern will remain, but this needs to be tested.

29 Future research will try to explain the reliability of accessibility at the origin level as a
30 function of specific network structure characteristics, such as circuitry and connectivity.

31 REFERENCES

- 32 [1] Science Applications International Corporation (SAIC), Delcan Corporation and University
33 of Virginia., *Evaluation of Utilizing Probe-based Freight Data to Support Congestion Mon-*
34 *itoring on the Highway System, Results and Initial Conclusions Summary*. Federal Highway
35 Administration, 2012.
- 36 [2] Liao, C.-F., Generate Reliable Freight Performance Measures Using Truck GPS Data - A
37 Case Study in Twin Cities Metropolitan Area, Minnesota. *Transportation Research Record:*
38 *Journal of the Transportation Research Board*, Vol. (in press), 2014.
- 39 [3] Anderson, P., A. Owen, and D. Levinson, *The Time Between: Continuously-defined accessi-*
40 *bility functions for schedule-based transportation systems*, 2012.
- 41 [4] Zhu, S. and D. Levinson, People don't use the shortest path. In *12th Conference of the Inter-*
42 *national Association for Travel Behaviour Research, Jaipur, India*, 2009.

- 1 [5] Sheffi, Y., *The resilient enterprise: overcoming vulnerability for competitive advantage*. The
2 MIT Press, 2005.
- 3 [6] Ortiz, D. S., B. Weatherford, H. H. Willis, M. Collins, N. Mandava, and C. Ordowich, *In-*
4 *creasing the capacity of freight transportation: US and Canadian perspectives*, Vol. 228.
5 Rand Corporation, 2007.
- 6 [7] Ortiz, D. S., L. Ecola, and H. H. Willis, *Freight Transportation Resilience: How a system-*
7 *wide perspective can help MPOs and DOT*. NCHRP - Transportation Research Board of the
8 National Academies, Washington, DC, 2009.
- 9 [8] Federal Highway Administration, *Statewide Opportunities for Linking Planning and Opera-*
10 *tions: A Primer*. US Department of Transportation, 2008.
- 11 [9] Garrison, W. L. and D. F. Marble, *The Structure of Transportation Networks*. Transportation
12 Center at Northwestern University, Evanston, Ill., 1961, draft of a report submitted Octo-
13 ber 31, 1961 to U.S. Army Transportation Research Command, Fort Eustis, Virginia, by the
14 Transportation Center at Northwestern University under contract DA-44-177-TC-685, Trans-
15 portation geography study.
- 16 [10] Kansky, K., *Structure of Transportation Networks: Relationships Between Network Geome-*
17 *try and Regional Characteristics*. Ph.D. thesis, University of Chicago, 1963, research Paper
18 No. 84.
- 19 [11] Kissling, C., Linkage Importance in a Regional Highway Network. *The Canadian Geogra-*
20 *pher*, Vol. 13, No. 2, 1969, pp. 113–127.
- 21 [12] Taaffe, E., H. Gauthier, and E. Morton, *Geography of Transportation*. Prentice-Hall, Upper
22 Saddle River, NJ, 1996.
- 23 [13] Gauthier, H. L., *Highway development and urban growth in Sao Paulo, Brazil: a network*
24 *analysis*. Ph.D. thesis, Northwestern University, 1966.
- 25 [14] Rodrigue, J.-P., C. Comtois, and B. Slack, *The Geography of Transport Systems*. Routledge,
26 London; New York, 2006.
- 27 [15] Haggett, P. and R. Chorley, *Network analysis in geography*. Edward Arnold, London, U.K.,
28 1969.
- 29 [16] Gastner, M. and M. Newman, The spatial structure of networks. *The European Physical*
30 *Journal B-Condensed Matter and Complex Systems*, Vol. 49, No. 2, 2006, pp. 247–252.
- 31 [17] Barthélemy, M., Spatial networks. *Physics Reports*, Vol. 499, No. 1, 2011, pp. 1–101.
- 32 [18] Patuelli, R., A. Reggiani, P. Nijkamp, and F. Bade, The evolution of the commuting network
33 in Germany: Spatial and connectivity patterns. *Journal of Transport and Land Use*, Vol. 2,
34 No. 3/4, 2010, pp. 5–37.
- 35 [19] Levinson, D. and A. El-Geneidy, The minimum circuitry frontier and the journey to work.
36 *Regional Science and Urban Economics*, Vol. 39, No. 6, 2009, pp. 732–738.

- 1 [20] Parthasarathi, P., H. Hochmair, and D. Levinson, Network structure and spatial separation.
2 *Environment and Planning B, Planning and Design.*, Vol. 39, No. 1, 2012, pp. 137–154.
- 3 [21] Parthasarathi, P., D. Levinson, and H. Hochmair, Network structure and travel time percep-
4 tion. *PloS one*, Vol. 8, No. 10, 2013, p. e77718.
- 5 [22] Yang, C., Y. Tu, and X. Chen, Analysis Method for Topology Vulnerability of Transportation
6 Network. In *Proceedings of the Second International Conference on Transportation Engi-
7 neering* (Q. Peng, K. C. P. Wang, and Y. Qiu, eds.), ASCE, Reston, VA, 2009, pp. 3639–3644.
- 8 [23] Jenelius, E., Network structure and travel patterns: Explaining the geographical disparities
9 of road network vulnerability. *Journal of Transport Geography*, Vol. 17, No. 3, 2009, pp.
10 234–244.
- 11 [24] Rodríguez-Núñez, E. and J. C. García-Palomares, Measuring the vulnerability of public trans-
12 port networks. *Journal of Transport Geography*, Vol. 35, 2014, pp. 50–63.
- 13 [25] Marshall, W. and N. Garrick, Street network types and road safety: A study of 24 California
14 cities. *Urban Design International*, Vol. 15, 2010, pp. 133–147.
- 15 [26] Townsend, A., *Re-Programming Mobility: How the Tech Industry Is Driving Us Towards A
16 Crisis in Transportation Planning*. New Cities Foundation, 2012.
- 17 [27] Levinson, D. and B. Yerra, Self Organization of Surface Transportation Networks. *Trans-
18 portation Science*, Vol. 40, No. 2, 2006, pp. 179–188.
- 19 [28] Yerra, B. M. and D. M. Levinson, The emergence of hierarchy in transportation networks.
20 *The Annals of Regional Science*, Vol. 39, No. 3, 2005, pp. 541–553.
- 21 [29] Cervero, R., Paradigm shift: from automobility to accessibility planning. *Working Paper 677*,
22 1996.
- 23 [30] Cheng, J. and L. Bertolini, Measuring urban job accessibility with distance decay, competi-
24 tion and diversity. *Journal of Transport Geography*, 2013.
- 25 [31] El-Geneidy, A. M. and D. M. Levinson, *Access to Destinations: development of accessibility
26 measures*. Minnesota Department of Transportation Research Services Section, 2006.
- 27 [32] Hansen, W. G., How accessibility shapes land use. *Journal of the American Institute of Plan-
28 ners*, 1959.
- 29 [33] Levinson, D. M., Accessibility and the journey to work. *Journal of Transport Geography*,
30 1998.
- 31 [34] Martellato, D. and P. Nijkamp, *The concept of accessibility revisited*. Accessibility, Trade and
32 Locational Behaviour, Ashgate, Brookfield, 1998.
- 33 [35] Owen, A. and D. Levinson, *Access to Destinations: Annual accessibility measure for the
34 Twin Cities Metropolitan Region*. Minnesota Department of Transportation Research Services
35 Section, 2012.

- 1 [36] Páez, A., D. M. Scott, and C. Morency, Measuring accessibility: positive and normative
2 implementations of various accessibility indicators. *Journal of Transport Geography*, Vol. 25,
3 2012, pp. 141–153.
- 4 [37] TomTom International BV, *Speed Profiles*, ????
- 5 [38] US Census Bureau, *TIGER/Line Shapefiles*, 2010.
- 6 [39] US Census Bureau, *LEHD origin-destination employment statistics dataset structure format*
7 *version 7.0.*, 2013.
- 8 [40] Vickerman, R. W., Accessibility, attraction, and potential: a review of some concepts and
9 their use in determining mobility. *Environment and Planning*, 1974.
- 10 [41] Wachs, M. and T. G. Kumagai, Physical accessibility as a social indicator. *Socio-Economic*
11 *Planning Sciences*, 1973.
- 12 [42] Demographia, *Demographia United States Central Business Districts (Downtown): With*
13 *data for selected additional employment areas: 3rd Edition*, 2014.
- 14 [43] Anderson, P., D. Levinson, and P. Parthasarathi, Accessibility Future. *Transaction in GIS*,
15 2013.