

# *Neutrino Frontiers – 2008*

*TPI – University of Minnesota*

## *Leptogenesis*

**Enrico Nardi**

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## Brief historical review

Leptogenesis: is a class of scenarios where the Universe baryon asymmetry  $Y_{\Delta B} \equiv \frac{n_B - \bar{n}_B}{s} \approx 8.7 \times 10^{-11}$  is produced from a lepton asymmetry ( $Y_{\Delta L}$ ) generated in the decays of heavy singlet Majorana (seesaw) neutrinos.

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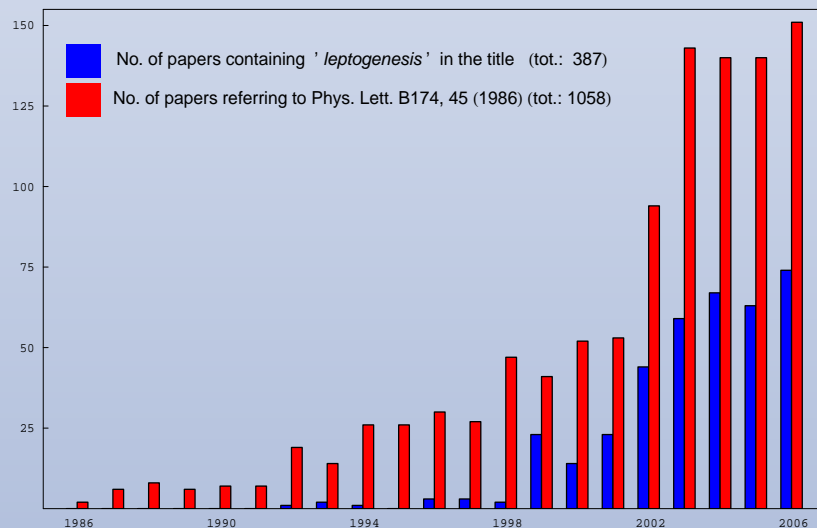
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Experimental confirmation of  $m_\nu \neq 0$   
 $m_\nu \ll m_f \Rightarrow$  hints to the seesaw ?  
 (there is a stronger reason - see below).

## Quantitative LG in the one-flavor approximation:

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“Towards a complete theory of thermal leptogenesis in the SM and MSSM,” *NPB***685**, 89 (2004).  
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- Quantitative and qualitative differences from 1-flavor approx. (Jan. 2006):  
*A. Abada, S. Davidson, F.X. Josse-Michaux, M. Losada, A. Riotto*,  
“Flavour issues in leptogenesis,” *JCAP* **0604**, 004 (2006); [*hep-ph/0601083*].  
*EN, Y. Nir, E. Roulet & J. Racker*,  
“The importance of flavor in leptogenesis,” *JHEP* **0601**, 164 (2006); [*hep-ph/0601084*].
- The asymmetry generated in the decays of the heavier  $N_{2,3}$  Majorana neutrinos can also give sizeable contributions to  $Y_{\Delta B}$  (Dec. 2006).  
*G. Engelhard, Y. Grossman, EN & Y. Nir*,  
“The importance of  $N_2$  leptogenesis,” *Phys. Rev. Lett.* **99** (2007) 081802.



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Direct test of LG: Produce  $N$ 's and measure the  $CP$  asymmetry in their decays

$$m_\nu \sim \frac{\lambda^2 v^2}{M_N} \sim \left( \frac{\lambda}{10^{-6}} \right)^2 \left( \frac{1 \text{ TeV}}{M_N} \right) \sqrt{\Delta m_{atm}^2} \quad \underline{\text{Impossible!}}$$

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1.  $B$  violation: In the EW symmetric phase, **EW-Sphalerons** violate  $B + L$  and convert part of any existing  $L$ -asymmetry into a  $B$ -asymmetry.

Experimentally: we can predict  $-Y_{\Delta L} \sim \mathcal{O}(Y_{\Delta B})$ . [More precisely:  $Y_{\Delta \nu} \sim -3Y_{\Delta B}$ ]  
(However, since  $L_\nu \leftrightarrow \nu$ -helicity, at  $T_\nu \sim 10^{-4}$  eV  $\Delta \nu$  has already “evaporated”)

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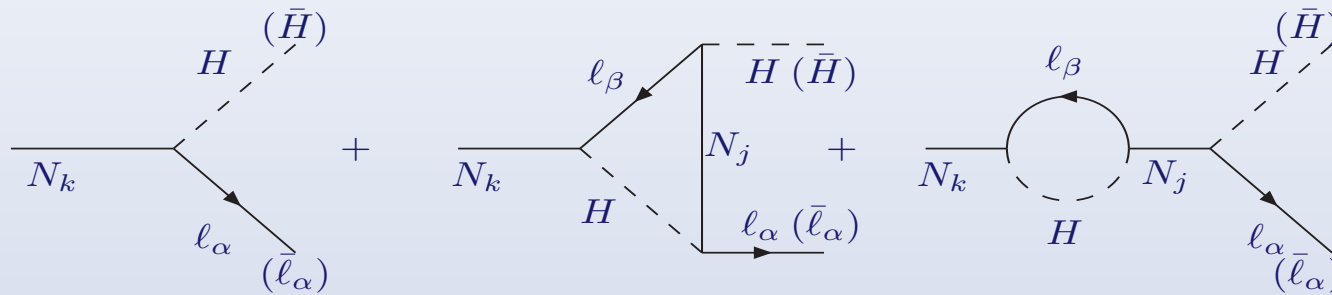
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$L$  violation: Is provided by the Majorana nature of the  $N$ 's:  $\ell_\alpha \phi \leftrightarrow N \leftrightarrow \bar{\ell}_\beta \bar{\phi}$   
(Important: generically, the rates for violation of individual  $L_\alpha$  differ)

Experimentally: we hope to see  $0\nu 2\beta$  decays (But only if IH or if  $\nu$ 's are quasi degenerate)

2. C & CP violation: From interference between tree and 1-loop amplitudes, due to complex Yukawa couplings ( $\lambda_{\alpha k}^* \bar{\ell}_\alpha H^* N_k$ ).

The CP-asymmetry between  $\Gamma_\alpha \equiv \Gamma(N \rightarrow \ell_\alpha H)$  and  $\bar{\Gamma}_\alpha \equiv \Gamma(N \rightarrow \bar{\ell}_\alpha \bar{H})$  decays

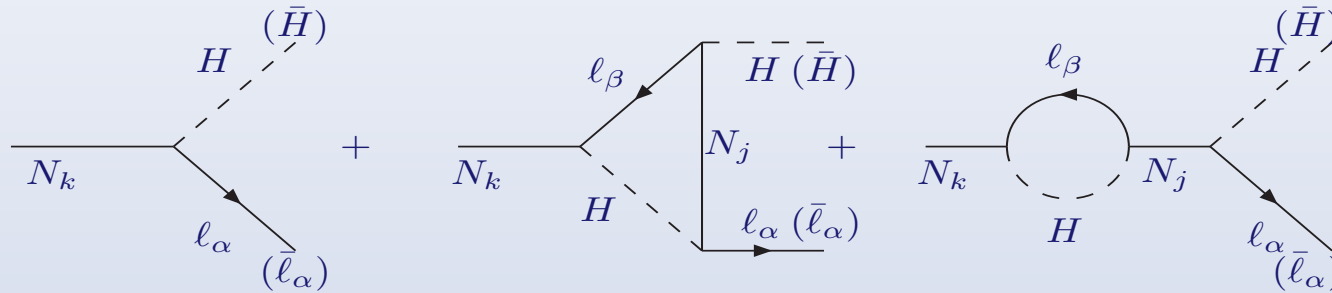


Necessary condition :  $\epsilon_\alpha = \frac{\Gamma_\alpha - \bar{\Gamma}_\alpha}{\Gamma_N} \neq 0$  (but  $\epsilon \equiv \sum_\alpha \epsilon_\alpha \neq 0$  is not necessary)

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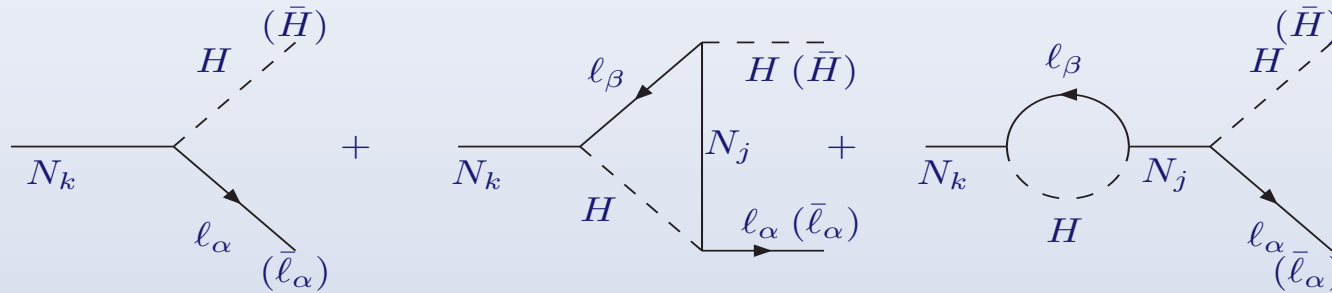
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$$\left[ \Gamma_{N_1} \sim H \right]_{T=M_{N_1}} \times \frac{8\pi v^2}{M_{N_1}^2} \Rightarrow \frac{(\lambda^\dagger \lambda)_{11}}{M_{N_1}} v^2 \equiv \tilde{m}_1 \sim m_* \simeq 10^{-3} \text{ eV}$$

Condition 3. is (optimally) satisfied for  $\tilde{m}_1 \sim \sqrt{\Delta m_\odot^2} - \sqrt{\Delta m_{atm}^2}$  ( $\tilde{m}_1 > m_{\nu_1}$  always)

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Other considerations (sufficient amount of CPV, perturbativity of  $\lambda$  couplings) suggest a mass scale  $M_{N_1} \sim 10^{11 \pm 2} \text{ GeV}$  – the seesaw scale.

# Flavor: the lepton basis issue

To simplify: neglect  $N_{2,3}$  except for their effects in the loops ( $CP$  asymmetry)

$$-\mathcal{L}_{\text{Yukawa}} = \lambda_{\alpha 1}^* \bar{\ell}_\alpha N_1 H_u + h_{\alpha\beta} \bar{\ell}_\alpha e_\beta H_d + h.c.$$



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Different bases give different results. The approx. solution of the BE for LG:

$$Y_{\Delta B} \approx 10^{-3} \times \eta_\ell \cdot \epsilon_\ell \quad \eta_\ell \sim \frac{m_*}{\tilde{m}_\ell} \text{ (strong washout); } \tilde{m}_\ell \propto \lambda_{\ell 1}^* \lambda_{\ell 1}$$

$$Y_{\Delta B} \approx 10^{-3} \times \begin{cases} \sum \eta_\alpha \cdot \epsilon_\alpha & \text{flavor regime} \\ \sum \eta_\alpha \cdot \sum \epsilon_\alpha \equiv \eta \cdot \epsilon & \text{one flavor approximation} \end{cases}$$

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The physical basis is determined dynamically at each  $T$  by the  $h$ -reaction rates.

## More in detail: Lepton Flavor Effects

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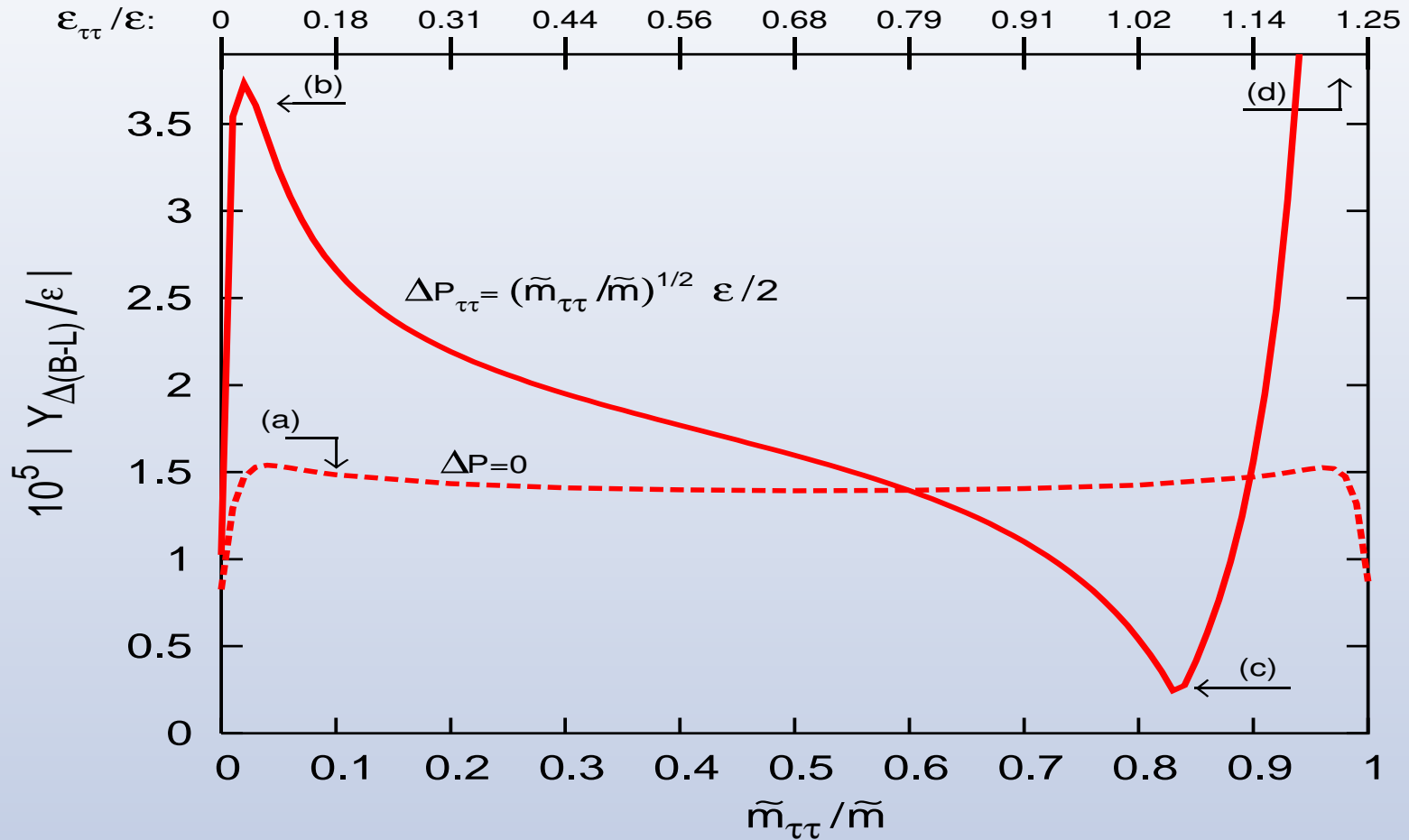
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The most interesting effects are due to the different flavor composition of  $\ell_1, \bar{\ell}'_1$ :

$$CP(\bar{\ell}'_1) \neq \ell_1 \Rightarrow \Delta P_\alpha \equiv P_\alpha - \bar{P}_\alpha \neq 0$$

# Two-flavor case: $l_\tau, l_{\perp\tau}$ ( $10^9 \text{ GeV} < T < 10^{12} \text{ GeV}$ ): $|Y_{\Delta(B-L)}|$ versus $P_\tau^0$



$|Y_{\Delta(B-L)}|$  (units of  $10^{-5}|\epsilon|$ ) as a function of  $P_\tau^0 \equiv |\langle l_\tau | l_1 \rangle|^2$  in the 2-flavor regime. **Dashed:** special case in which  $P_\tau = \bar{P}_\tau$ . **Solid:** typical behavior when  $P_\tau \neq \bar{P}_\tau$ . The value of  $\epsilon_1^\tau/\epsilon_1$  (that can be  $> 1$ ) is marked on the upper  $x$ -axis.

# Purely Flavored Leptogenesis ( $\epsilon = 0$ ): **SM+seesaw**

Casas-Ibarra parameterization for the  $N$  Yukawa couplings [NPB618 (2001)]

$$\lambda_{\alpha K} = \frac{1}{v} \left[ U^\dagger \sqrt{m_\nu} \cdot R \sqrt{M_N} \right]_{\alpha K}; \quad R = \frac{v}{\sqrt{m_\nu}} \cdot U^T \cdot \lambda \cdot \frac{1}{\sqrt{M_N}}$$

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The flavor asymmetry  $\epsilon_\alpha$  (leading term)  $\propto$  the imaginary part of:

$$\lambda_{\alpha 1}^* \lambda_{\alpha K} \left( \lambda^\dagger \lambda \right)_{1K} = \frac{M_1 M_K}{v^4} \left( \sum_i m_{\nu_i} R_{i1}^* R_{iK} \right) \left( \sum_{i,j} \sqrt{m_{\nu_j} m_{\nu_i}} R_{j1}^* R_{iK} U_{j\alpha} U_{i\alpha}^* \right)$$

The total asymmetry  $\epsilon \propto \text{Im}:$

$$\left( \lambda^\dagger \lambda \right)_{1K}^2 = \frac{M_1 M_K}{v^4} \left( \sum_i m_{\nu_i} R_{i1}^* R_{iK} \right)^2$$

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$$\lambda_{\alpha 1}^* \lambda_{\alpha K} \left( \lambda^\dagger \lambda \right)_{1K} = \frac{M_1 M_K}{v^4} \left( \sum_i m_{\nu_i} R_{i1}^* R_{iK} \right) \left( \sum_{i,j} \sqrt{m_{\nu_j} m_{\nu_i}} R_{j1}^* R_{iK} U_{j\alpha} U_{i\alpha}^* \right)$$

The total asymmetry  $\epsilon \propto \text{Im}:$   $(\lambda^\dagger \lambda)_{1K}^2 = \frac{M_1 M_K}{v^4} \left( \sum_i m_{\nu_i} R_{i1}^* R_{iK} \right)^2$

Assuming that  $R$  is real implies surprising results:

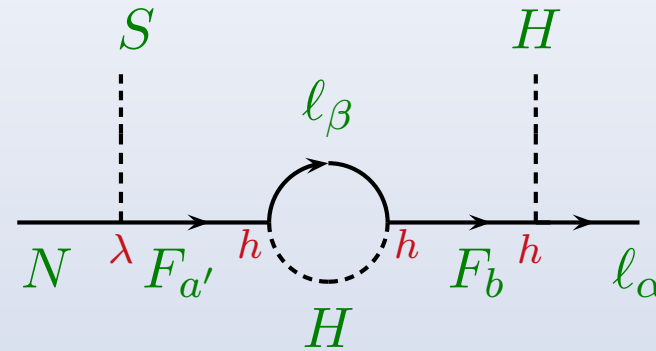
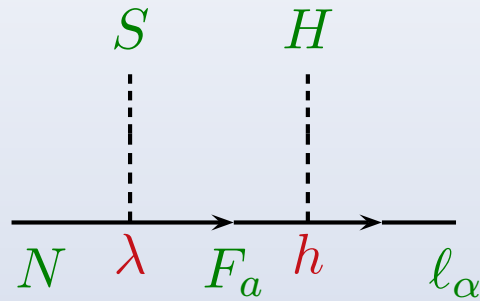
- 1:  $\epsilon = 0$ , but  $\epsilon_\alpha \neq 0$ , and thus  $Y_{\Delta B} \neq 0$
- 2:  $\epsilon_\alpha$  depends only on the  $\nu$ -mix-matrix  $U$  !

Recent studies of this scenario: Pastore *et al.*; Branco *et al.*;

# Purely Flavored Leptogenesis: Beyond the SM+seesaw

[D. Aristizabal, M. Losada, EN, PLB659 (2008)]

Assume a  $U(1)_F$  (flavor) symmetry that forbids a direct  $\bar{\ell}NH$  coupling, and that the flavor symmetry is still unbroken during LG:  $\langle S \rangle = 0$ .



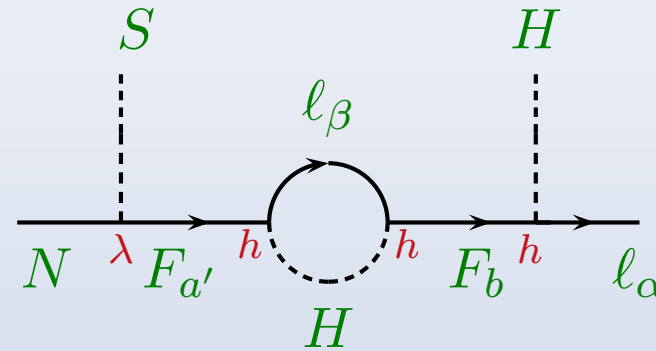
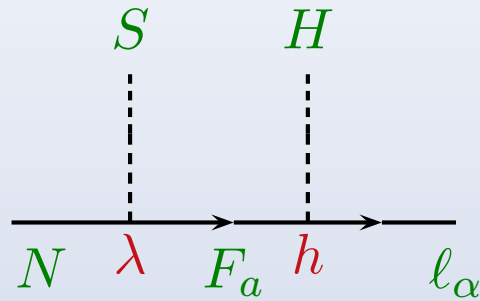
$$\tilde{\lambda}_{\alpha K} = \left( h \frac{\langle S \rangle}{M_F} \lambda^\dagger \right)_{\alpha K};$$

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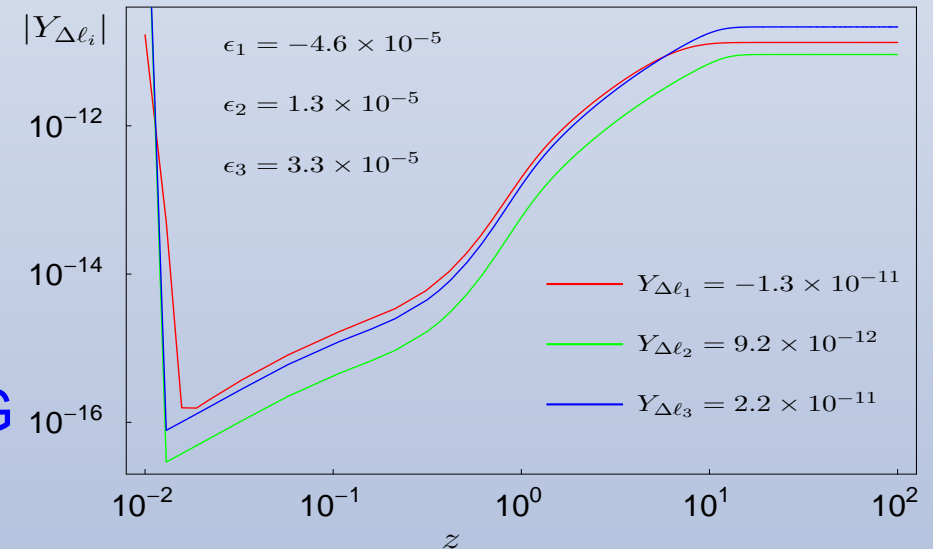
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$$\epsilon_{\alpha} = \frac{3}{128\pi} \frac{\text{Im} \sum_{\beta} \left[ (hr^2h^\dagger)_{\beta\alpha} \tilde{\lambda}_{1\beta} \tilde{\lambda}_{1\alpha}^* \right]}{(\tilde{\lambda}\tilde{\lambda}^\dagger)_{11}} \sim \mathcal{O}(h^2);$$

$$\tilde{m}_{\alpha} \sim \mathcal{O}(\tilde{\lambda}^2); \quad m_{\nu} \sim \frac{\tilde{\lambda}^2 v^2}{M_N} \sim \mathcal{O}(\tilde{\lambda}^2)$$

By decoupling  $\epsilon_{\alpha}$  from  $\tilde{m}_{\alpha}, m_{\nu}$  the LG scale can be lowered:  $M_N \sim \text{few TeV}$ .



# Including the effects of the Heavier Neutrino $N_{2,3}$

$$-\mathcal{L}_{\text{Yukawa}} = \lambda_{\alpha 1} \overline{N}_1 \ell_{\alpha} H_u + h_{\alpha}^* \overline{e}_{\alpha} \ell_{\alpha} H_d + \text{h.c.}$$



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- $\tilde{m}_1 \sim m_*$  : ‘moderate’ washouts,  $Y_{\Delta \ell_2}$  in part survives. It contributes to  $Y_{\Delta B}$ .
- $\tilde{m}_1 \gg m_*$  : ‘very strong’ washout regime,  $Y_{\Delta \ell_2}$  in part survives, and it can be the main responsible for  $Y_{\Delta B}$  (contrary to common belief).

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◇ If the following conditions are realized, LG occurs mainly through  $N_2$  effects:

$$1) \eta_2 \cdot \epsilon_2 \neq 0; \quad 2) \tilde{m}_1 \gg m_*; \quad 3) M_2/M_1 \gg 1.$$

★ Since  $\ell_0 \perp \ell_1$ , the component of the asymmetry  $Y_{\Delta\ell_2}$  along the  $\ell_0$  direction:

$$Y_{\Delta\ell_0} = |\langle \ell_0 | \ell_2 \rangle|^2 Y_{\Delta\ell_2} \text{ is protected from } N_1 \text{ washouts and survives.}$$

# Conclusions and Outlook

- Leptogenesis is a very attractive scenario to explain  $Y_{\Delta B}$ . Recent developments showed that *quantitative* and *qualitative* estimates of  $Y_{\Delta B}$  have to take into account the detailed flavor structure of the seesaw parameters.
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- Experimental detection of  $0\nu 2\beta$  decays and/or  $\mathcal{CP}_L$  in the lepton sector will strengthen the case for leptogenesis – but will not prove it.
- Failure of revealing  $\mathcal{CP}_L$  will not disprove LG.  
(However, if a sizeable  $\theta_{13} \neq 0$  is established, it would disfavor it.)
- If a *quasi degenerate* or *IH*  $\nu$ -spectrum is established, failure of revealing  $0\nu 2\beta$ -decays will *strongly disfavor* LG. (In the *DH* case no  $0\nu 2\beta$  signal is expected.)

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- Finally, **LHC + EDM** experiments will be able to establish or falsify **EWB**. This will indirectly determine the relevance of future **LG** studies.