

Exotic $c\bar{c}$ Mesons

Eric Braaten

The Ohio State University

collaborator

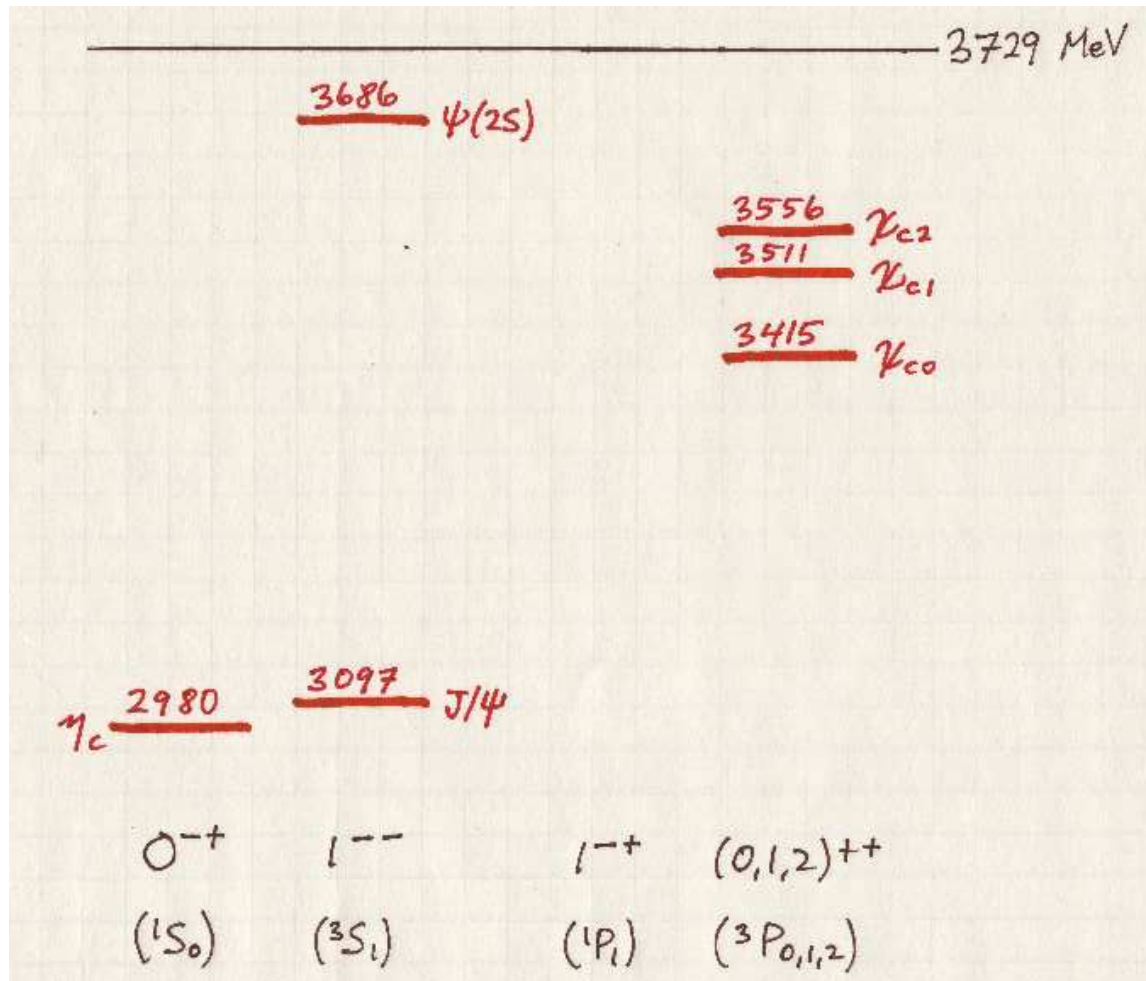
Meng Lu (student at Ohio State)

support:

DOE, Division of High Energy Physics
DOE, Division of Basic Energy Sciences

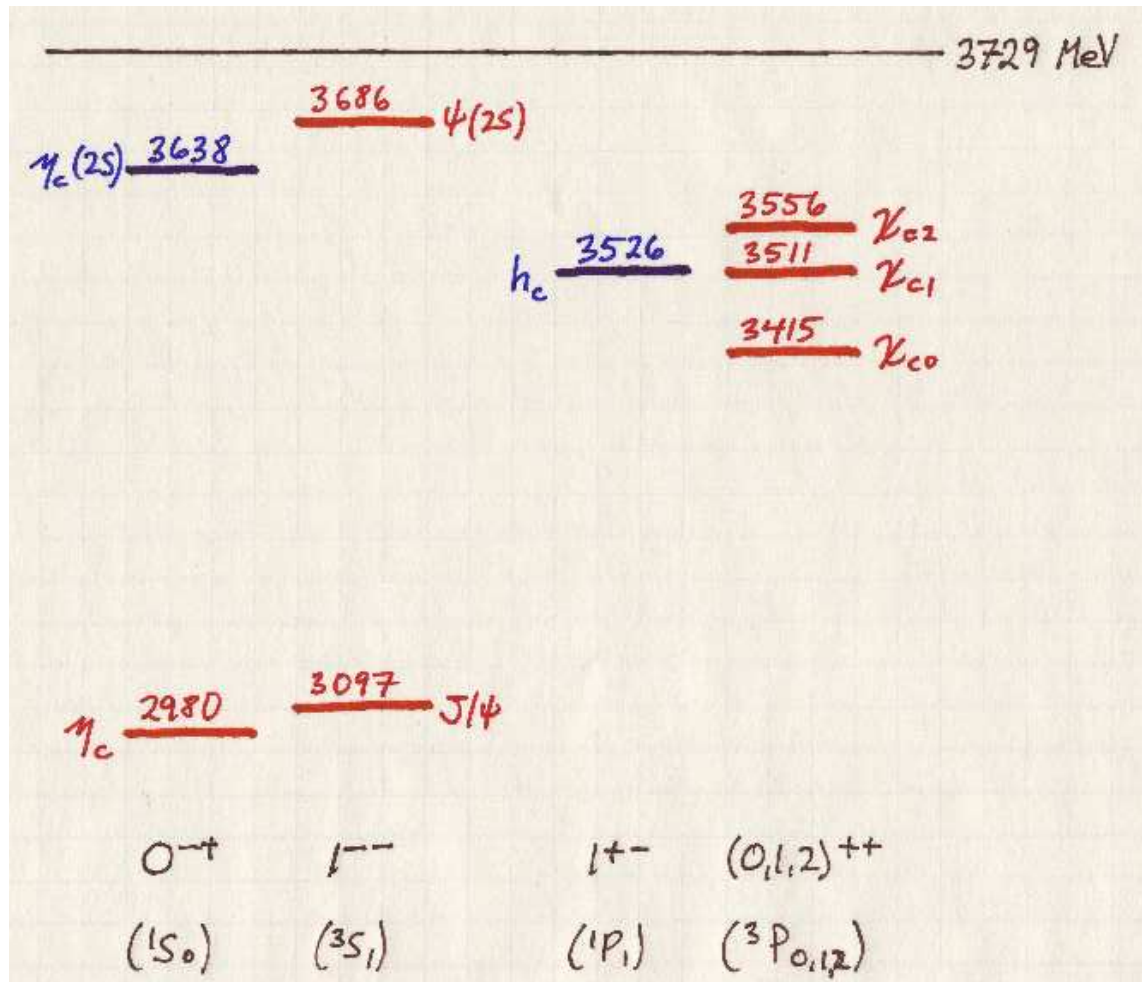
$c\bar{c}$ mesons below $D\bar{D}$ threshold

before the B factories



$c\bar{c}$ mesons below $D\bar{D}$ threshold

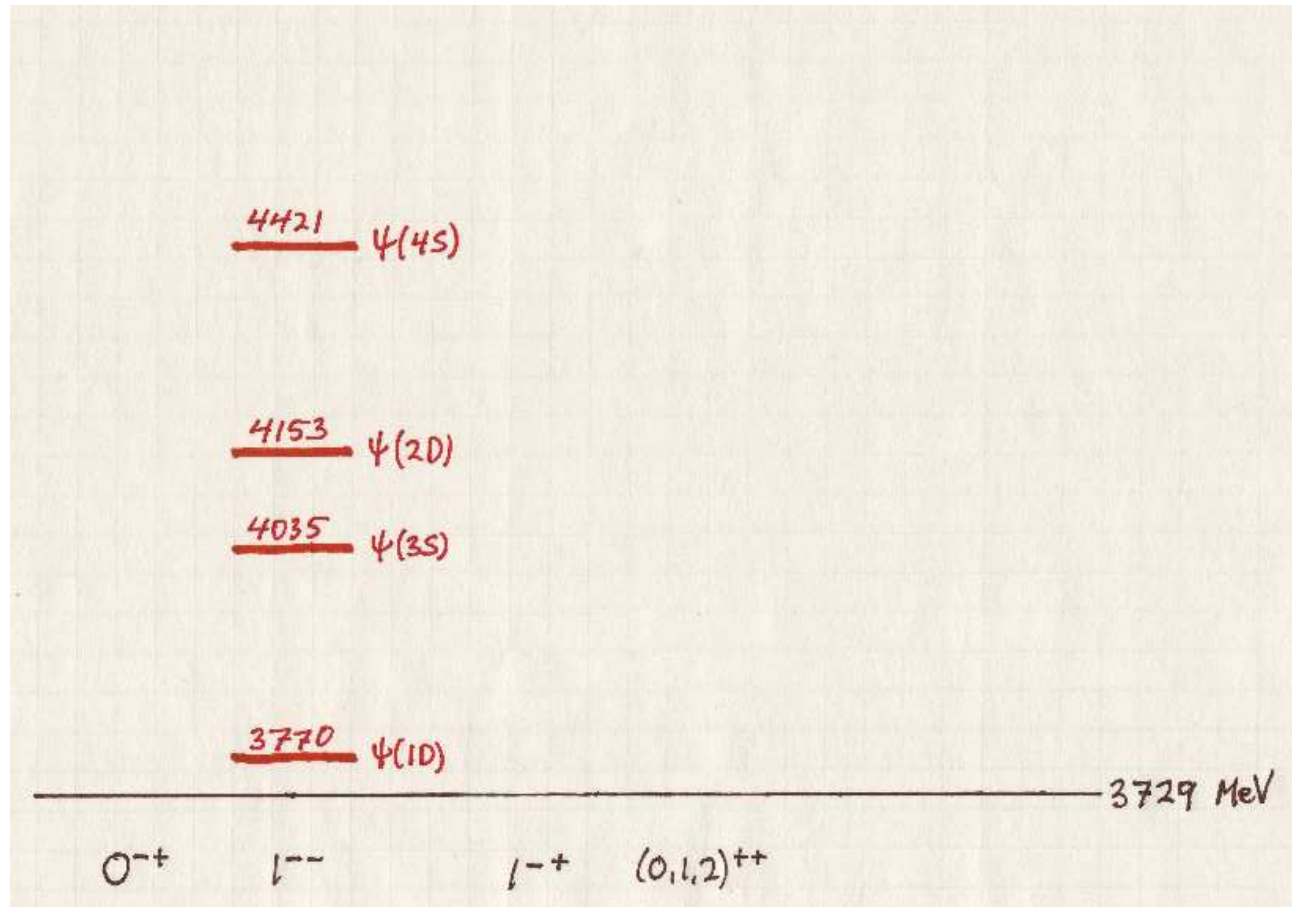
after the B factories



- 3 complete multiplets: $1S$, $1P$, $2S$

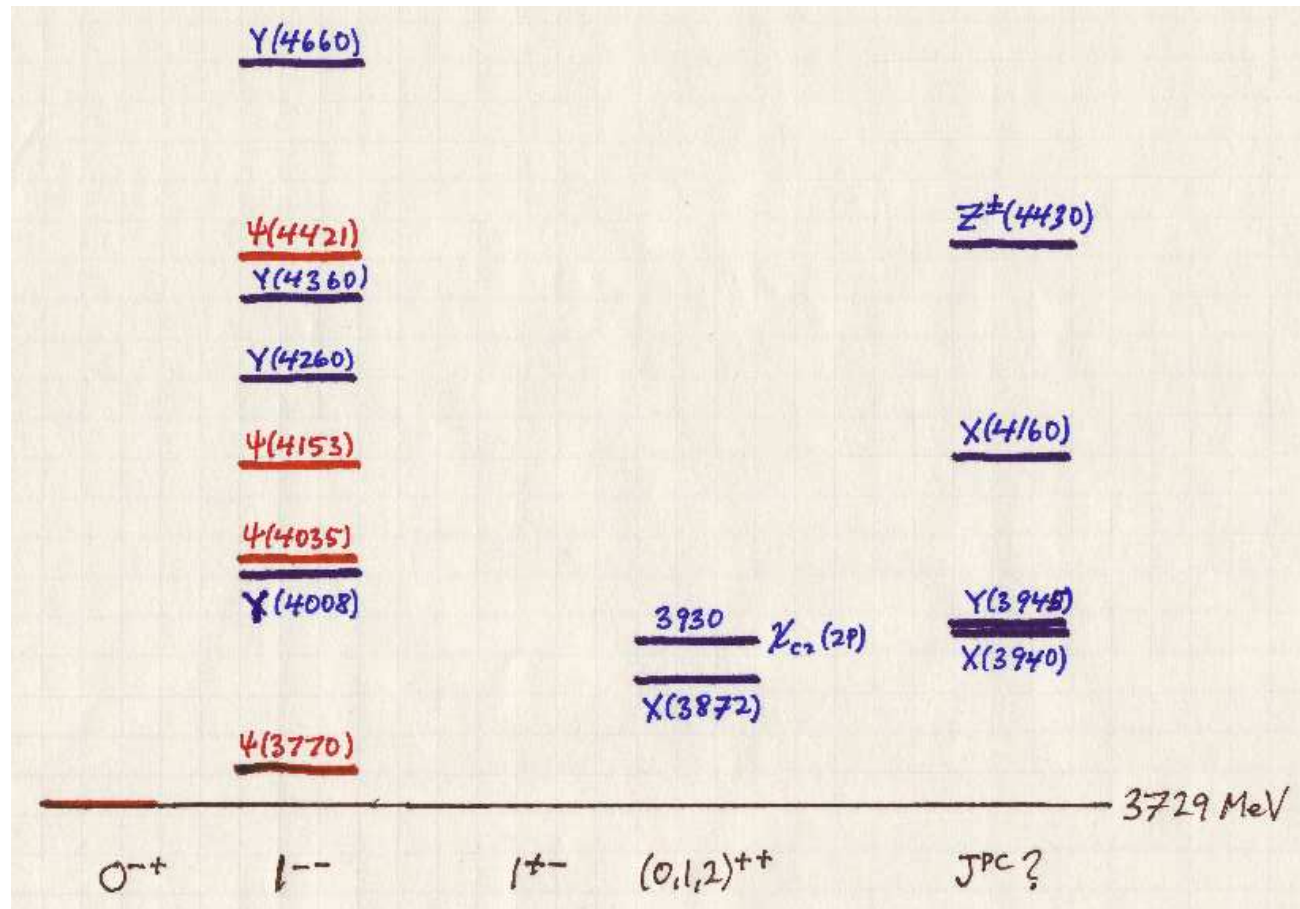
$c\bar{c}$ mesons above $D\bar{D}$ threshold

before the B factories



$c\bar{c}$ mesons above $D\bar{D}$ threshold

after the B factories



- four new 1^{--} states
- exotic $c\bar{c}$ mesons: $X(3872)$, $Z^{\pm}(4430)$

Recent reviews on **new $c\bar{c}$ mesons**

The New Heavy Mesons: A Status Report

Swanson, [hep-ph/0601110](#)

Quarkonia and their Transitions

Eichten, Godfrey, Mahlke, and Rosner, [hep-ph/0701208](#)

Charmonium

Voloshin, [arXiv:0711.4556](#)

The Exotic XYZ Charmonium-like Mesons

Godfrey and Olsen, [arXiv:0801.3867](#)

$X(3872)$

discovered by Belle collaboration

November 2003

$$B^+ \longrightarrow K^+ + X, \quad X \longrightarrow J/\psi \pi^+ \pi^-$$

confirmed by CDF, BaBar, D0

Mass: 3871.4 ± 0.6 MeV

Width: < 2.3 MeV (90% C.L.)

J^{PC} : 1^{++}

- isospin violating decays: $X \longrightarrow J/\psi \rho^* \longrightarrow J/\psi \pi\pi$ ($I = 1$)
 $X \longrightarrow J/\psi \omega^* \longrightarrow J/\psi \pi\pi\pi$ ($I = 0$)

- mass higher in $D^0 \bar{D}^0 \pi^0$
than in $J/\psi \pi^+ \pi^-$ by 3.8 ± 1.1 MeV

New $1^{--} c\bar{c}$ mesons

discovered by Belle and Babar collaborations
through initial state radiation

$$e^+e^- \longrightarrow \gamma + e^+e^- \longrightarrow \gamma + Y$$

- decay into $J/\psi \pi\pi$ OR $\psi(2S) \pi\pi$

$$Y(4008) \longrightarrow J/\psi \pi^+ \pi^-$$

$$Y(4260) \longrightarrow J/\psi \pi^+ \pi^-$$

$$Y(4360) \longrightarrow \psi(2S) \pi^+ \pi^-$$

$$Y(4660) \longrightarrow \psi(2S) \pi^+ \pi^-$$

- no resonant peaks in $\sigma[e^+e^-]$

$$\sigma[e^+e^- \rightarrow D\bar{D}, D^*\bar{D}, D^*\bar{D}^*]$$

$Z^\pm(4430)$

discovered by Belle collaboration

August 2007

$$B^+ \longrightarrow K^0 + Z^+, \quad Z^+ \longrightarrow \psi(2S) \pi^+$$

Mass: 4433 ± 5 MeV

Width: 45^{+35}_{-18} MeV

J^P : ??

I^G : 1^+

decay products: $\psi(2S) = c\bar{c}$, $\pi^+ = u\bar{d}$
 $\implies Z^+$ has constituents $c\bar{c}u\bar{d}$

Manifestly exotic $c\bar{c}$ meson!!

What are the new $c\bar{c}$ mesons

above $D\bar{D}$ threshold?

Ordinary $c\bar{c}$ mesons?

Charmonium: $c\bar{c}$

Exotic $c\bar{c}$ mesons?

Charmonium hybrids: $c\bar{c}g$

Tetraquark mesons: $c\bar{c}q\bar{q}$

compact tetraquark

$$(c\bar{c}q\bar{q})_1$$

diquark-antidiquark

$$(cq)_{3^*} + (\bar{c}\bar{q})_3$$

charm meson molecule

$$(c\bar{q})_1 + (\bar{c}q)_1$$

hadro-charmonium

$$(c\bar{c})_1 + (q\bar{q})_1$$

...

Sexaquark mesons: $c\bar{c}qq\bar{q}\bar{q}$

Charmonium

Potential models

Barnes, Godfrey, and Swanson; Eichten, Lane, and Quigg

well-developed phenomenology

except for effects of coupling to charm meson pairs

Missing states:

$3S$ multiplet	
$\eta_c(3S)$	0^{-+}
<hr/>	
$2P$ multiplet	
$h_c(2P)$	1^{+-}
$\chi_{c1}(2P)$	1^{++}
$\chi_{c0}(2P)$	0^{++}
<hr/>	
$1D$ multiplet	
$\psi_3(1D)$	3^{--}
$\psi_2(1D)$	2^{--}
$\eta_{c2}(1D)$	2^{-+}

Missing multiplets: $4S$, $3P$, $2D$, ...

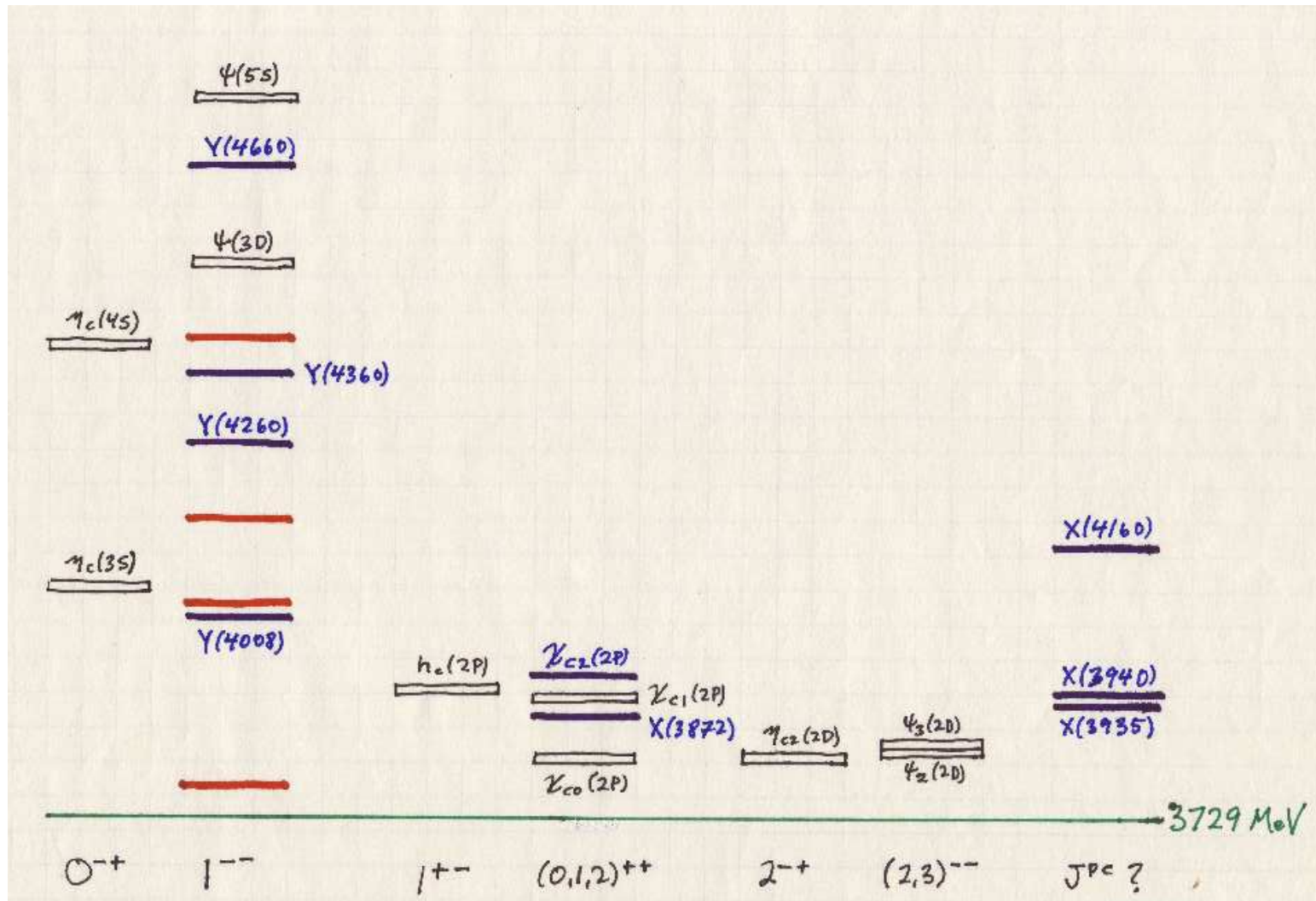
Charmonium (cont.)

Missing charmonium states

old charmonium states

new $c\bar{c}$ mesons

missing charmonium states



Charm meson molecules

Bander, Shaw, Thomas, and Meshkov; Voloshin and Okun;
de Rujula, Georgi, and Glashow; Nussinov and Sidhu (1976-78)

Meson potential model

with one-pion-exchange and UV cutoff on $1/r^3$ potential

Tornqvist (1991, 1994)

predicted charm meson molecules near threshold

in several J^{PC} channels with $I = 0$

$D\bar{D}$: none

$D^*\bar{D}/D\bar{D}^*$: $1^{++}; 0^{-+}$
(threshold = 3872 MeV)

$D^*\bar{D}^*$: $0^{++}, 1^{+-}, 2^{++}, 0^{-+}$
(threshold = 4014 MeV)

Charm meson molecules (cont.)

Tornqvist essentially predicted $X(3872)$ in 1994

modulo effects of isospin splitting: D^+-D^0 , $D^{*+}-D^{*0}$

Updated analysis

Swanson

use mass of $X(3872)$ to tune UV cutoff on $1/r^3$ potential

include quark exchange interactions

predictions for charm meson molecules

$D^*\bar{D}/D\bar{D}^*$: 1^{++} $X(3872)$ (input)

$D^*\bar{D}^*$: 0^{++} $X(4013)$ predicted

predictions for bottom meson molecules

$B^*\bar{B}/B\bar{B}^*$: 0^{-+} , 1^{++}

$B^*\bar{B}^*$: 0^{++} , 0^{-+} , 1^{+-} , 2^{++}

binding energies: 40 to 70 MeV

Diquark–antidiquark tetraquark mesons

Maiani, Piccinini, Polosa, and Riquer; Ishida, Ishida, and Maeda; Ebert, Faustov, and Galkin

constituent diquarks: $S \equiv (cq)_{3^*, S=0}$, $A \equiv (cq)_{3^*, S=1}$

S-wave tetraquarks

$$\begin{aligned} S\bar{S} &: 0^{++} \\ A\bar{S}, S\bar{A} &: 1^{++}, 1^{+-} \\ S\bar{S} &: 0^{++}, 1^{+-}, 2^{++} \end{aligned}$$

flavor multiplets for each J^{PC} :

$$\begin{aligned} q = u, d, s &: 9 \text{ states} \\ q = u, d &: 4 \text{ states} : (X^-, X^0, X^+) X^{0'} \end{aligned}$$

Diquark–antidiquark tetraquark mesons (cont.)

Problem: too many states

S-wave, $n = 1$, $(cq)_3^*$ diquarks $\implies 9 \times 6 = 54$ states

also orbital excitations

radial excitations

$(cq)_6$ diquarks

4-body problem for constituent quarks

Vijande, Valcarce, et al.; Hiyama, Suganama, and Kamimura

no stable $Q\bar{Q}q\bar{q}$ states

with only 2-body color-dependent forces

QCD sum rules

Navarra, Nielsen, et al.

possibility of bound states in some channels: 1^{++} ?

Lattice QCD?

dynamical quarks are essential

exotic quantum numbers are easiest

excited states are difficult

Charmonium hybrids

Lattice gauge theory (without dynamical light quarks)

- Born-Oppenheimer approximation

Juge, Kuti, Morningstar

lowest multiplet:

$$0^{-+}, 0^{+-}, 1^{--}, 1^{++}, 1^{+-}, 1^{-+}, 2^{-+}, 2^{+-}$$

masses ≈ 4200 MeV

- conventional lattice gauge theory

Liao and Manke; Liu and Luo

lowest states with exotic quantum numbers

$$1^{-+} : 4400 \text{ MeV}$$

$$0^{+-} : 4700 \text{ MeV}$$

$$2^{+-} : 4900 \text{ MeV}$$

Mass range compatible with new 1^{--} states:

$$Y(4260), Y(4360), Y(4660)$$

Charmonium hybrids (cont.)

Decays into two charm mesons

Isgur, Kokoski, and Paton; Close and Page; Kou and Pene

- *S-wave* + *S-wave* is suppressed: $D\bar{D}$, $D^*\bar{D}$, $D\bar{D}^*$, $D^*\bar{D}^*$
- *P-wave* + *S-wave* is favored: $D_1\bar{D}^{(*)}$, $D_2\bar{D}^{(*)}$

New $1^{--} c\bar{c}$ mesons: $Y(4260)$, $Y(4360)$, $Y(4660)$

observed via $Y \rightarrow J/\psi \pi\pi$

OR $Y \rightarrow \psi(2S) \pi\pi$

not seen in $Y \rightarrow D\bar{D}, D^*\bar{D}, D^*\bar{D}^*$

charmonium hybrid mesons?

Hadro-charmonium

Voloshin, Dubynsky, Gorsky

light hadron h bound to charmonium ψ : $(\psi h) = (c\bar{c})_1 + (q\bar{q})_1$

multipole expansion for long-wavelength gluon fields:

$$\mathcal{H}_{\text{eff}} = -\frac{1}{2}\alpha_{\psi} \mathbf{E}^a \cdot \mathbf{E}^a$$

\implies attractive interaction

strong enough for bound state ??

new $c\bar{c}$ meson with J/ψ decay modes: $(J/\psi h)?$

$$Y(4008) \longrightarrow J/\psi \pi^+ \pi^-$$

$$Y(4260) \longrightarrow J/\psi \pi^+ \pi^-$$

new $c\bar{c}$ meson with $\psi(2S)$ decay modes: $(\psi(2S) h)?$

$$Y(4360) \longrightarrow \psi(2S) \pi^+ \pi^-$$

$$Y(4660) \longrightarrow \psi(2S) \pi^+ \pi^-$$

$$Z^{\pm}(4430) \longrightarrow \psi(2S) \pi^{\pm}$$

What is the $X(3872)$?

Two crucial experimental inputs

- mass is extremely close to $D^{*0}\bar{D}^0$ threshold

$$M_X - (M_{D^{*0}} + M_{D^0}) = -0.4 \pm 0.7 \text{ MeV}$$

- $J^{PC} = 1^{++}$

Conclusion

$X(3872)$ is a weakly-bound charm meson molecule

$$X = \frac{1}{\sqrt{2}} (D^{*0}\bar{D}^0 - D^0\bar{D}^{*0})$$

What is the $X(3872)$? (cont.)

“Universality of Few-Body Systems with Large Scattering Length”

Braaten and Hammer, arXiv:cond-mat/0410417

S-wave resonances near threshold have universal properties
determined by a large scattering length
(or by small binding energy E_X and width)

apply to $X(3872)$

- $J^{PC} = 1^{++} \implies$ S-wave coupling to $D^{*0}\bar{D}^0$
 - mass within 1 MeV of $D^{*0}\bar{D}^0$ threshold \implies resonant coupling!
- conclude $X(3872)$ is charm meson molecule (or virtual state)

$$X = \frac{1}{\sqrt{2}} \left(D^{*0}\bar{D}^0 - D^0\bar{D}^{*0} \right)$$

mean separation of constituents

$$\begin{aligned} \langle r \rangle_X &= \hbar / (8\mu E_X)^{1/2} \\ &= 3.5 \text{ fm} \quad \text{if } E_X = 0.4 \text{ MeV} \end{aligned}$$

What is the $X(3872)$? (cont.)

Explanation of $X(3872)$ puzzles

- isospin violating decays

$$X \longrightarrow J/\psi \rho^* \longrightarrow J/\psi \pi^+ \pi^- \quad (I = 1)$$

$$X \longrightarrow J/\psi \omega^* \longrightarrow J/\psi \pi^+ \pi^- \pi^0 \quad (I = 0)$$

tuning the mass of any 1^{++} state

($D^* \bar{D}$ bound state, $\chi_{c1}(2P)$, ...)

to the $D^{*0} \bar{D}^0$ threshold (3871.8 MeV)

transforms it into a $D^{*0} \bar{D}^0$ molecule

$$X = \frac{1}{\sqrt{2}} \left(D^{*0} \bar{D}^0 - D^0 \bar{D}^{*0} \right)$$

\implies equal superposition of $I = 0$ and $I = 1$

What is the $X(3872)$? (cont.)

Explanation of $X(3872)$ puzzles

- mass difference in $D^0\bar{D}^0\pi^0$ and $J/\psi\pi^+\pi^-$

$$M_X^{D^0\bar{D}^0\pi^0} - M_X^{J/\psi\pi^+\pi^-} = 3.8 \pm 1.1 \text{ MeV}$$

$B \longrightarrow K + D^0\bar{D}^0\pi^0$ proceeds via

1. resonance production: $B \longrightarrow K + X(3872)$

followed by decay of constituent: $D^{*0} \longrightarrow D^0\pi^0$

\implies resonant peak at $(M_{D^{*0}} + M_{D^0}) - E_X$

2. charm meson production: $B \longrightarrow K + D^{*0}\bar{D}^0$

followed by decay $D^{*0} \longrightarrow D^0\pi^0$

\implies threshold enhancement peaks at $(M_{D^{*0}} + M_{D^0}) + E_X$

$B \longrightarrow K + J/\psi\pi^+\pi^-$ proceeds only via

1. resonance production: $B \longrightarrow K + X(3872)$

\implies resonant peak at $(M_{D^{*0}} + M_{D^0}) - E_X$

What is the $X(3872)$? (cont.)

Other predictions

Braaten and Lu

- Ratios of production rates*

$$\frac{\Gamma[B^0 \rightarrow K^0 + X]}{\Gamma[B^+ \rightarrow K^+ + X]} = \left| \frac{\gamma_1}{\gamma_1 - \kappa_1} \right|^2$$

$\kappa_1 = 125 \text{ MeV}$

$\gamma_1 =$ inverse scattering length for $D^*\bar{D}$ in $I = 1$ channel

- Line shapes* of $X(3872)$

$B^+ \rightarrow K^+ + J/\psi \pi^+ \pi^-:$	zero <u>6 MeV above</u> $D^{*0}\bar{D}^0$ threshold
$B^0 \rightarrow K^0 + J/\psi \pi^+ \pi^-:$	zero <u>2 MeV below</u> $D^{*0}\bar{D}^0$ threshold
$B \rightarrow K + J/\psi \pi^+ \pi^- \pi^0:$	no zeroes near threshold
$B \rightarrow K + D^0\bar{D}^0 \pi^0:$	no zeroes near threshold

* supercedes incorrect predictions by Braaten and Kusunoki and by Voloshin

Conclusions

- $Z^\pm(4430)$ is exotic tetraquark meson:

$$Z^+ = c\bar{c}u\bar{d}$$

isospin multiplet: (Z^- , Z^0 , Z^+)

J^P quantum numbers?

- $X(3872)$ is weakly-bound charm meson molecule:

$$X = \frac{1}{\sqrt{2}} (D^{*0}\bar{D}^0 - D^0\bar{D}^{*0})$$

universal properties associated with large scattering length

insensitive to details of QCD

mechanism: binding of charm mesons?

$\chi_{c1}(2P)$ near threshold?

other?

Conclusions (cont.)

- New 1^{--} mesons may be charmonium hybrids

$Y(4260)?$ $Y(4360)?$ $Y(4660)?$

confirm by observation of decays into $D_1\bar{D}^{(*)}$, $D_2\bar{D}^{(*)}$

If exotic $c\bar{c}$ mesons exist,

then exotic $b\bar{b}$ mesons probably also exist

Theoretical challenge: predict their properties!

Experimental challenge: discover them!