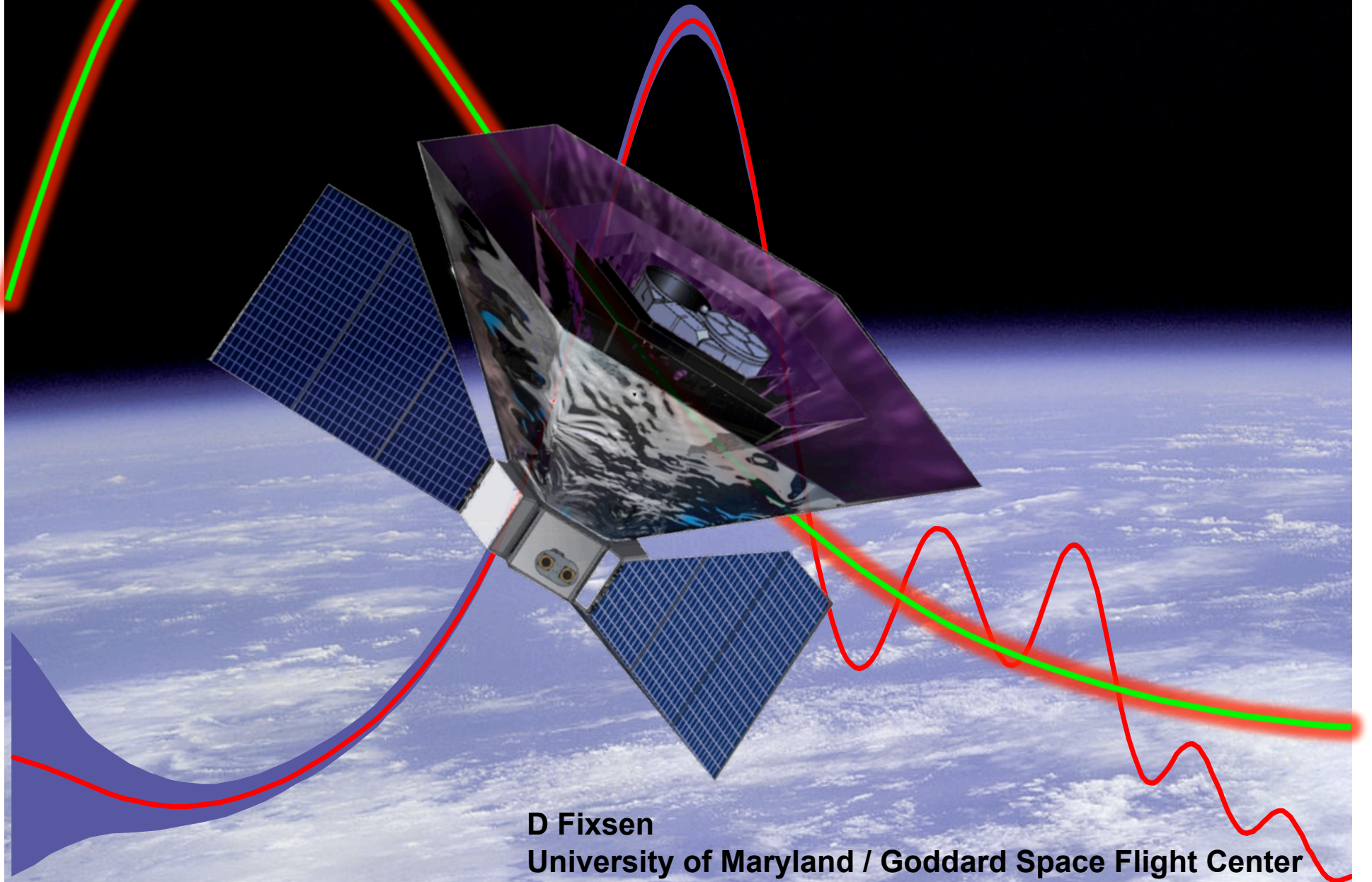
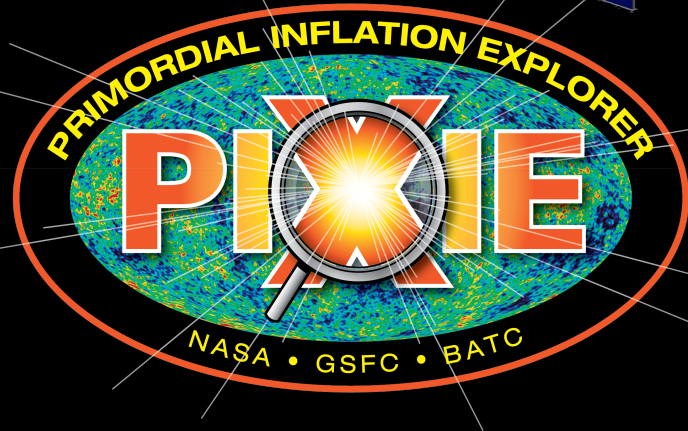
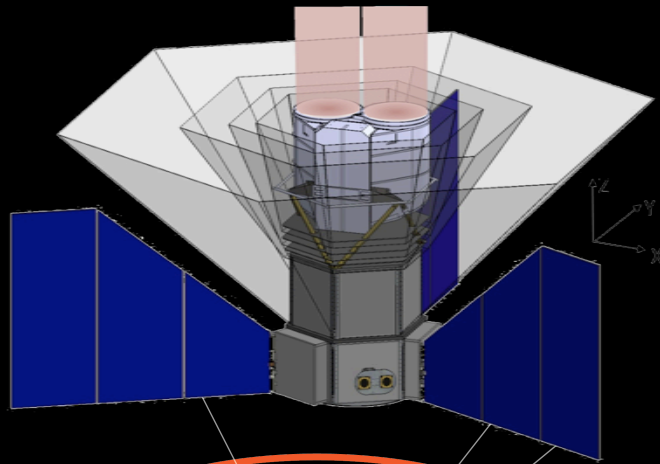


Control of Systematics for the Primordial Inflation Explorer (PIXIE)



D Fixsen
University of Maryland / Goddard Space Flight Center

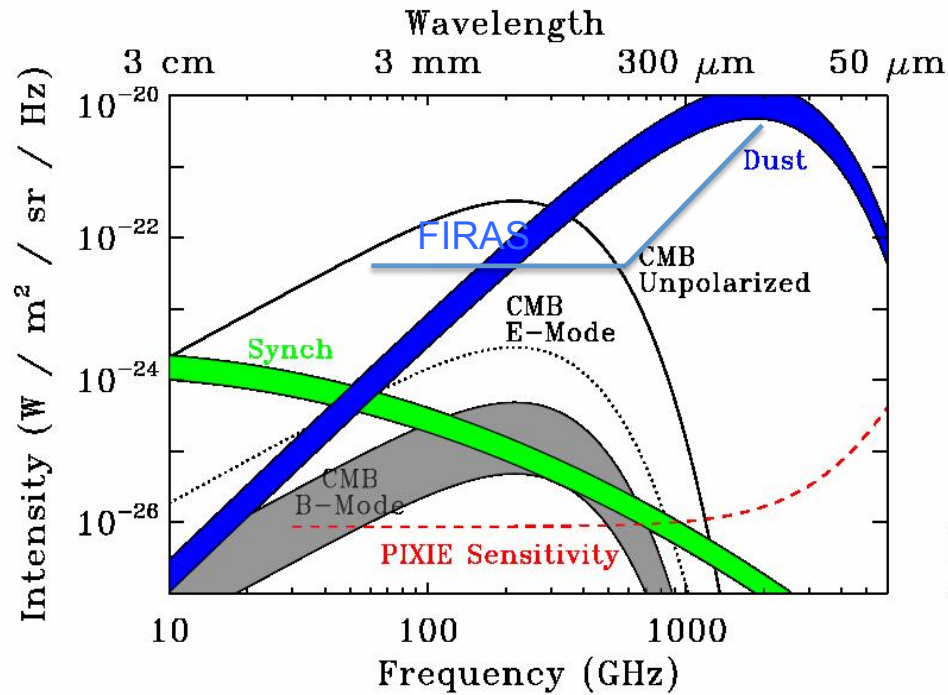
Primordial Inflation Explorer



Name	Role	Institution
A. Kogut	PI	GSFC
D. Fixsen	IS	UMD
D. Chuss	Co-I	GSFC
J. Dotson	Co-I	ARC
E. Dwek	Co-I	GSFC
M. Halpern	Co-I	UBC
G. Hinshaw	Co-I	UBC
S. Meyer	Co-I	U. Chicago
H. Moseley	Co-I	GSFC
M. Seiffert	Co-I	JPL
D. Spergel	Co-I	Princeton
E. Wollack	Co-I	GSFC

**Measure B-Mode Polarization
To Limits Imposed By Astrophysical and Cosmological Foregrounds**

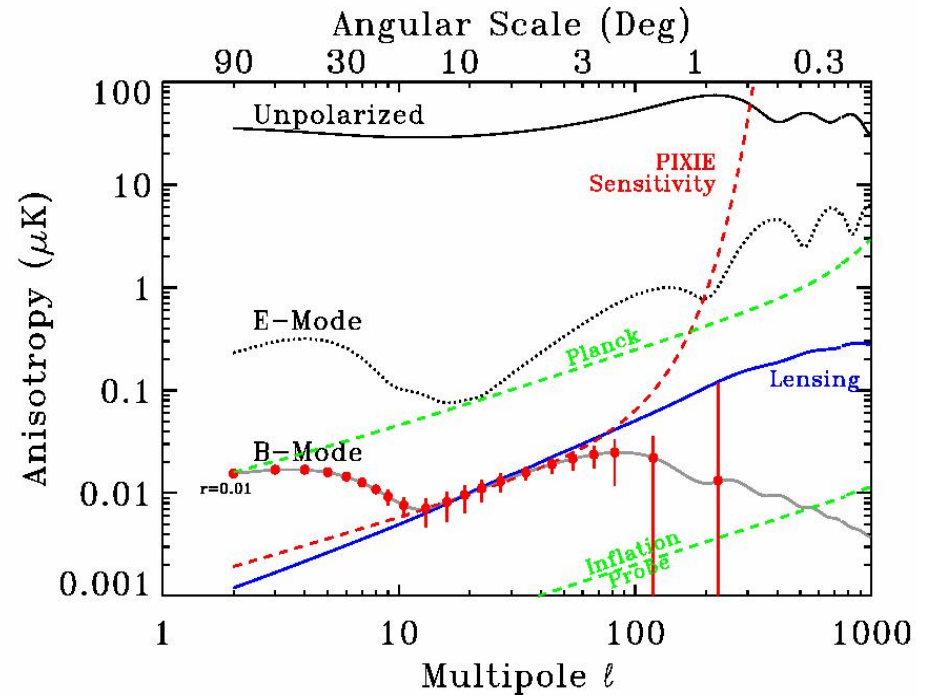
PIXIE B-Mode Science



- Detect ~all large-field models
- Power spectrum to $l \sim 200$
- Reach limit of lensing foreground

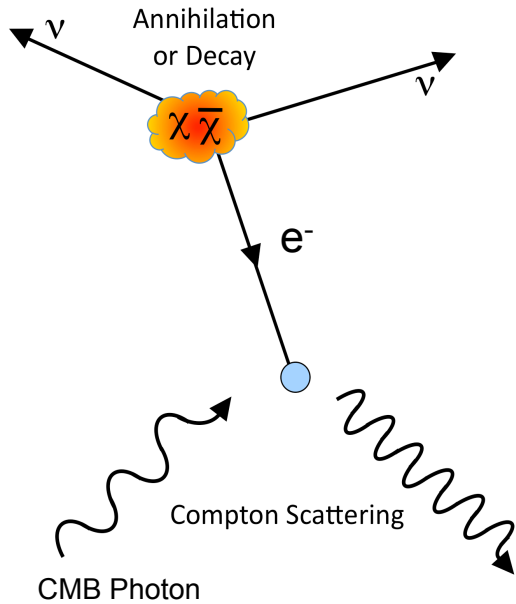
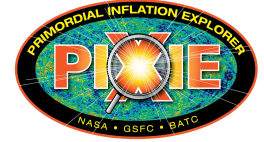
Full-Sky Spectro-Polarimetric Survey

- 400 frequency channels, 30 GHz to 6 THz
- Stokes I, Q, U parameters
- 49152 sky pixels each $0.9^\circ \times 0.9^\circ$
- Pixel sensitivity $6 \times 10^{-26} W m^{-2} s^{-1} sr^{-1}$
- CMB sensitivity 70 nK RMS per pixel



Measure $r < 0.001$ at 5σ (after foreground subtraction)

Spectral Distortion from Energy Release



Optically thin case: Compton y distortion

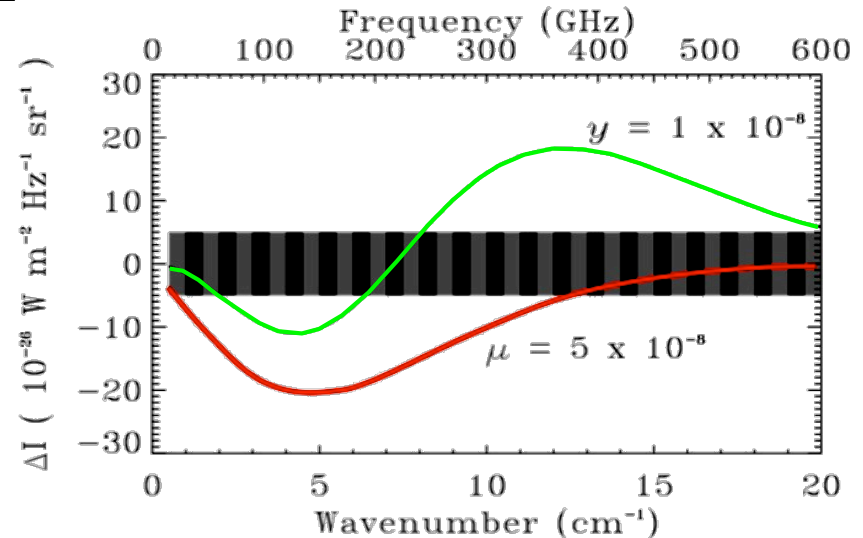
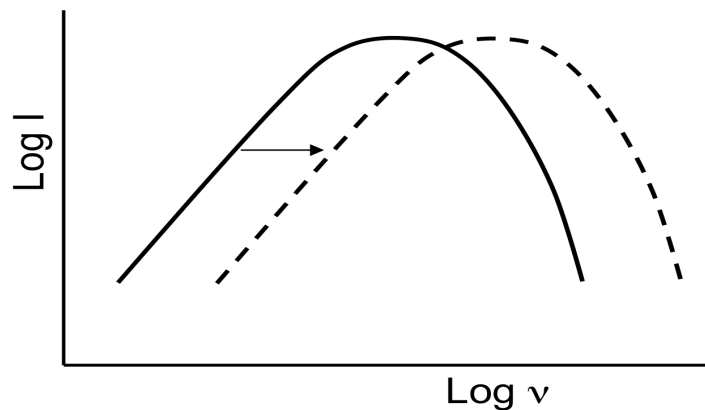
$$I(\nu, T) = \frac{2h\nu^3}{c^2} \frac{1}{\exp(x) - 1} \left[1 + \frac{yx \exp(x)}{\exp(x) - 1} \left(\frac{x}{\tanh(x/2)} - 4 \right) \right]$$

$$y = \int \frac{kT_e}{mc^2} n c \sigma_T dt \quad \text{FIRAS limit } 1.5 \times 10^{-5}$$

Optically thick case: Chemical potential distortion

$$I(\nu, T) = \frac{2h\nu^3}{c^2} \frac{1}{\exp\left(\frac{h\nu}{kT} + \mu\right) - 1}$$

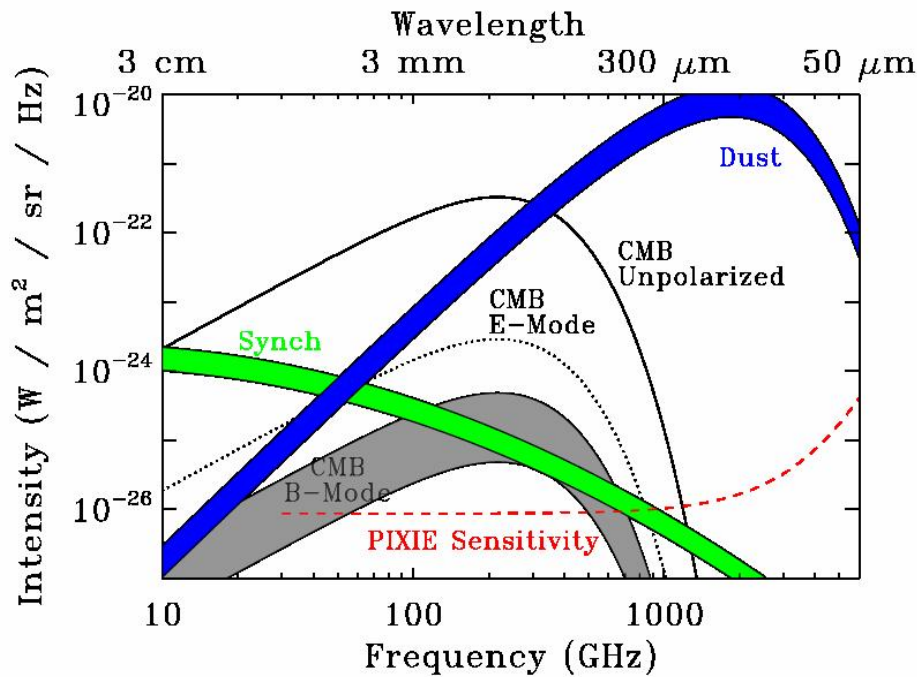
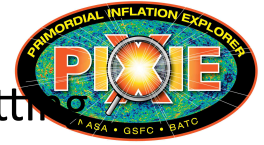
$$\mu = 1.4 \frac{\Delta E}{E} \quad \text{FIRAS limit } 9 \times 10^{-5}$$



Distortion to blackbody spectrum proportional to integrated energy release

Foreground Science: Interstellar Dust

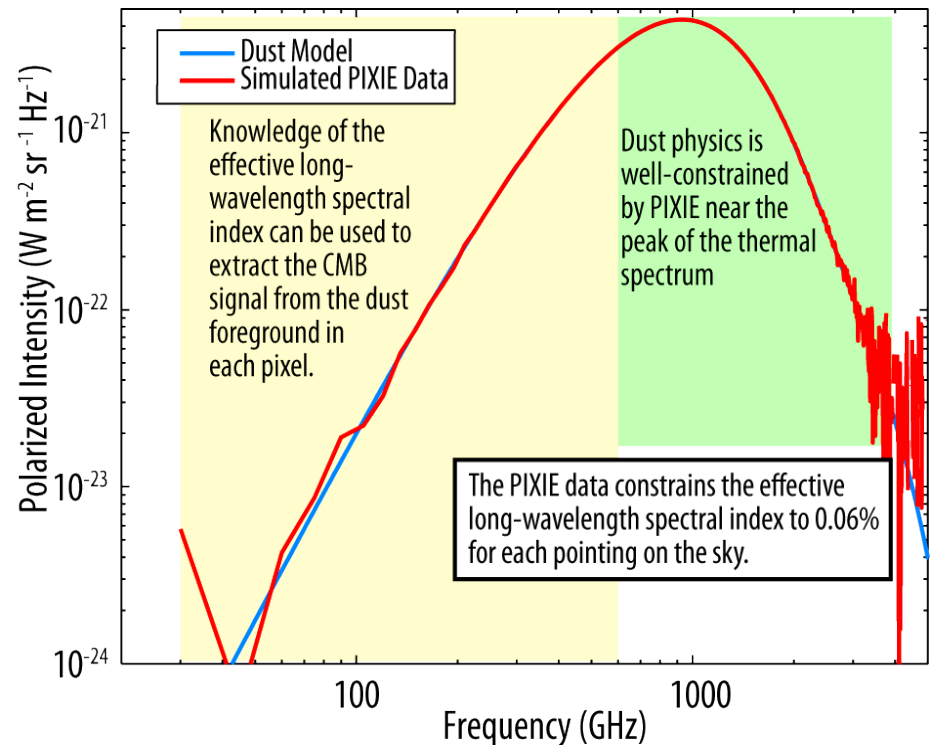
Science from high-frequency channels informs low-frequency fitting



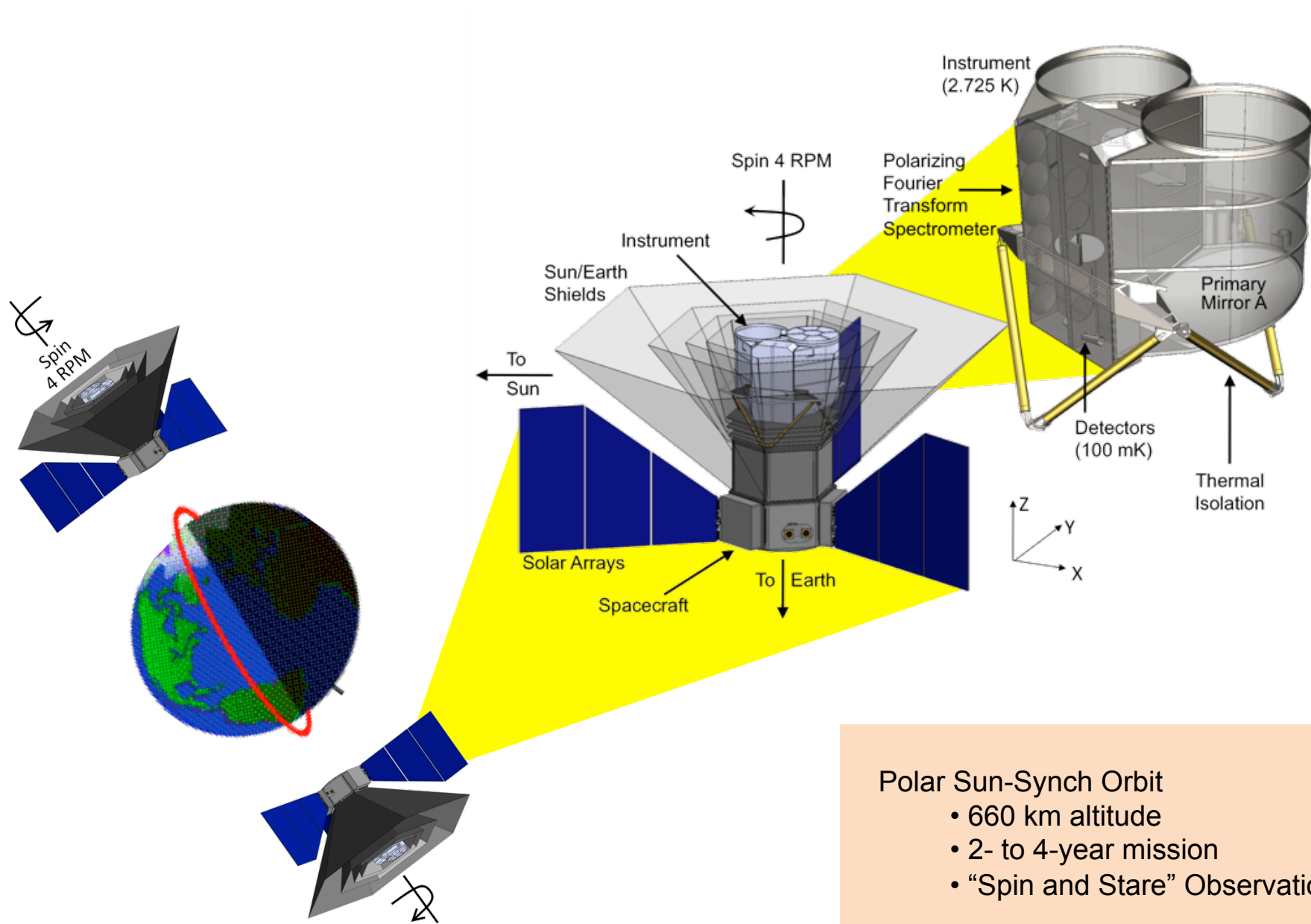
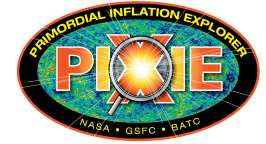
Pixel-by-pixel dust characterization

- 400 channels to fit models of far-IR dust emission
- Spectral index uncertainty ± 0.001 in each pixel
- Dust physics for foreground subtraction

One person's foreground is another person's science

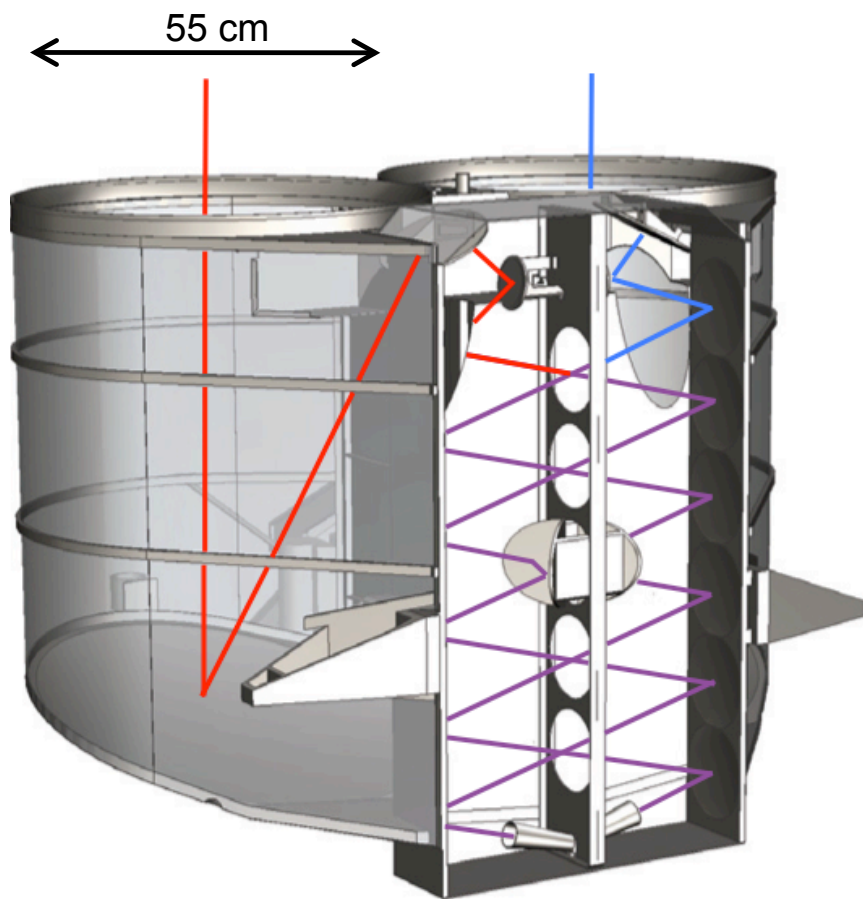


Instrument and Observatory



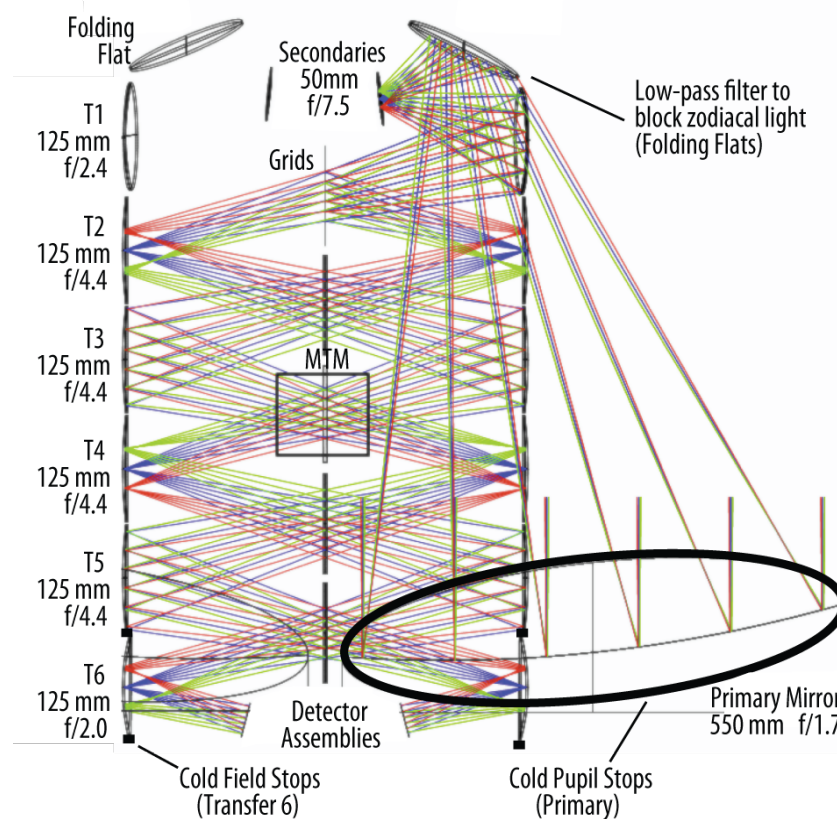
- Polar Sun-Synch Orbit
- 660 km altitude
 - 2- to 4-year mission
 - “Spin and Stare” Observations

PIXIE Non-Imaging Optics

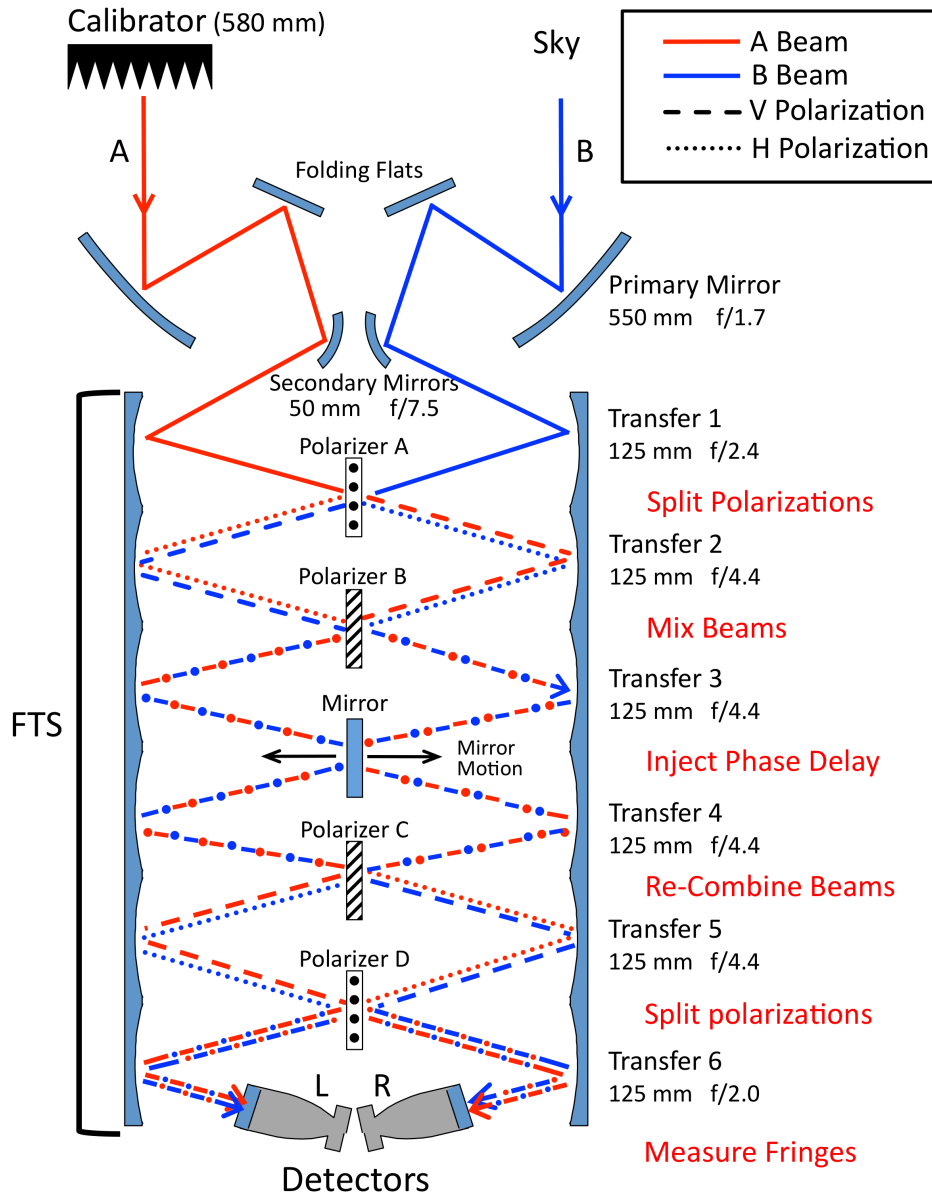
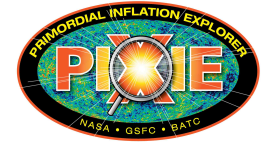


44,000 modes
on 4 detectors

Parameter	Value
Primary Mirror Diam	550 mm
Etendu	4 cm ² sr
Beam Diam	2.6° Tophat 1.6° Gaussian approx
Efficiency	82%



PIXIE Nulling Polarimeter



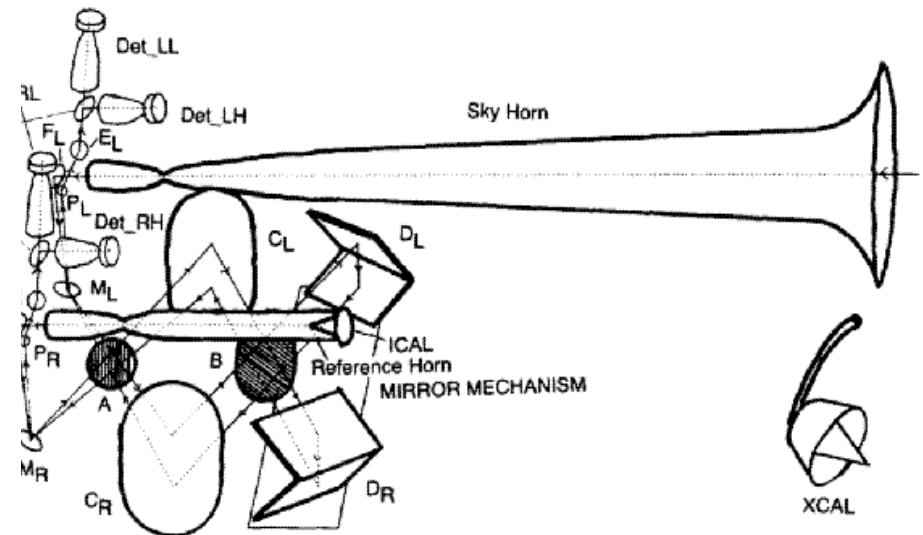
AC Readout
Nulling Polarimeter: Zero = Zero

$$P_{Lx} = \frac{1}{2} \int (E_{Ay}^2 + E_{Bx}^2) + (E_{Bx}^2 - E_{Ay}^2) \cos(zv/c) dv$$

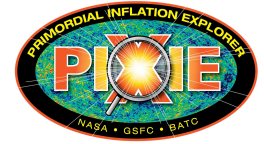
$$P_{Ly} = \frac{1}{2} \int (E_{Ax}^2 + E_{By}^2) + (E_{By}^2 - E_{Ax}^2) \cos(zv/c) dv$$

$$P_{Rx} = \frac{1}{2} \int (E_{Ax}^2 + E_{By}^2) + (E_{Ax}^2 - E_{By}^2) \cos(zv/c) dv$$

$$P_{Ry} = \frac{1}{2} \int (E_{Ay}^2 + E_{Bx}^2) + (E_{Ay}^2 - E_{Bx}^2) \cos(zv/c) dv$$



Fourier Transform



$$P_{Lx} = \frac{1}{2} \int \left(E_{Ay}^2 + E_{Bx}^2 \right) + \left(E_{Bx}^2 - E_{Ay}^2 \right) \cos(z\nu/c) d\nu$$

$$P_{Lx}(\omega) = g_{Lx}(\omega) \left(S_{Bx}(\nu) - S_{Ay}(\nu) \right), \quad \omega = \nu * u/c$$

$$P_{Ly}(\omega) = g_{Ly}(\omega) \left(S_{By}(\nu) - S_{Ax}(\nu) \right)$$

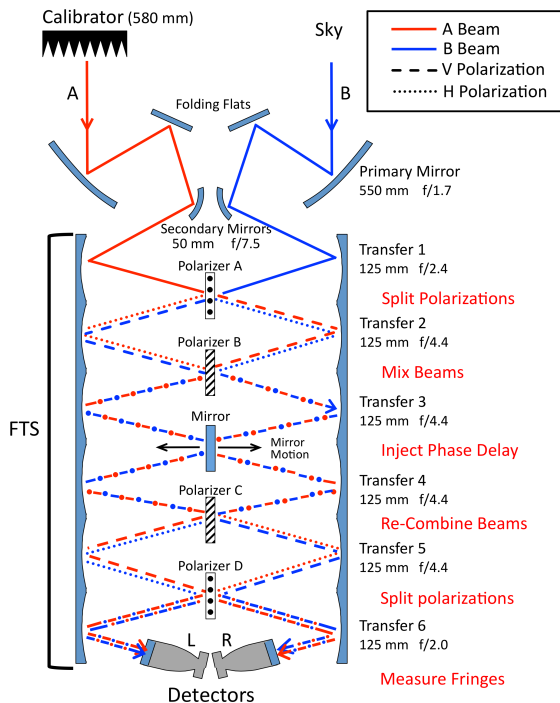
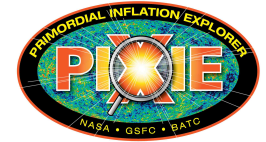
$$P_{Rx}(\omega) = g_{Rx}(\omega) \left(S_{Ax}(\nu) - S_{By}(\nu) \right)$$

$$P_{Ry}(\omega) = g_{Ry}(\omega) \left(S_{Ay}(\nu) - S_{Bx}(\nu) \right)$$

Resolution set by
maximum excursion,

highest frequency set
by sample spacing

Systematics: Mirrors



Signal = few mK (the mirror is $2.725 \pm .005$ K)

$\times \sim .01$ (Mirror emissivity)

$\times \sim .01$ (Left / Right asymmetry)

$\times \sim .01$ (Move Calibrator, switch sign)

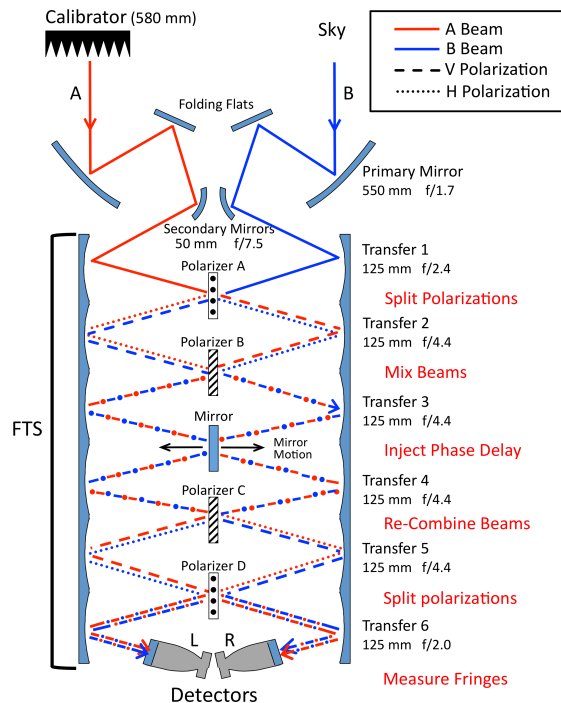
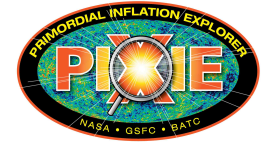
= few nK bluish tinge, **before correction**

Calibration allows measurement and correction of mirror emission during observations, **with full observational data set**. Allows data selection/weighting to match precisely. Errors < 1 nK after correction.

Identical arguments for flats, secondary, T1, T2 and T3.

T4, T5 and T6 are not modulated and so produce no signal.

Systematics: Instrument



Signal = few mK (the Instrument is ~ 2.725)

$\times \sim .01$ (Beam fraction missing mirrors)

$\times \sim .01$ (Left / Right asymmetry)

$\times \sim .01$ (Other mirror has opposite sign)

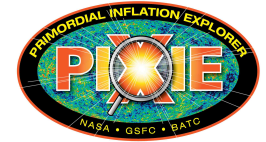
= few nK reddish tinge, **before correction**

Calibration allows measurement and correction of instrument emission during observations, **with full observational data**. Also allows data selection/weighting to match precisely. Errors < 1 nK after correction.

Identical arguments totems, septum and other areas. Areas close to the detectors are not modulated and so produce no signal.

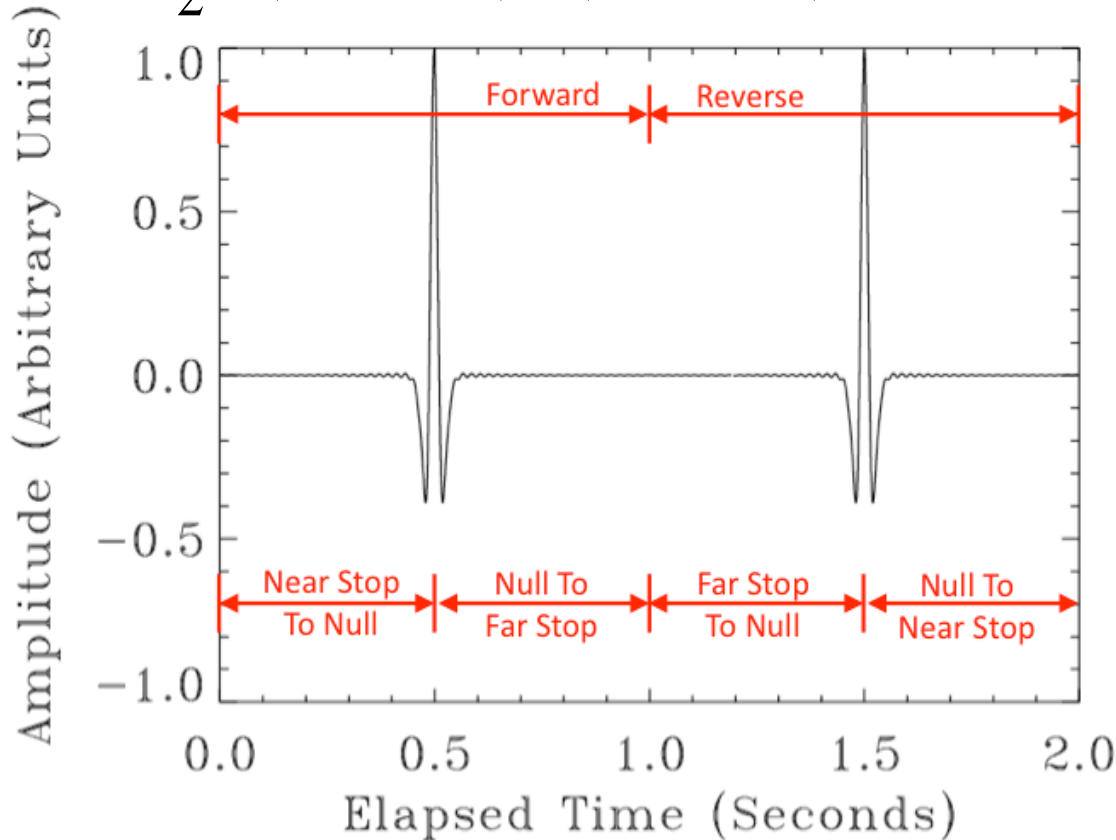
Systematics: Stroke

Fully symmetric stroke



$$P_{Lx} = \frac{1}{2} \int \left(E_{Ay}^2 + E_{Bx}^2 \right) + \left(E_{Bx}^2 - E_{Ay}^2 \right) \cos(zv/c) dv$$

Signal is $\sim 10^{-3}$ of DC



Same information 4x per stroke with 4 different time/space symmetries on each detector

Fourier Transform:

Real (cosine)=Signal

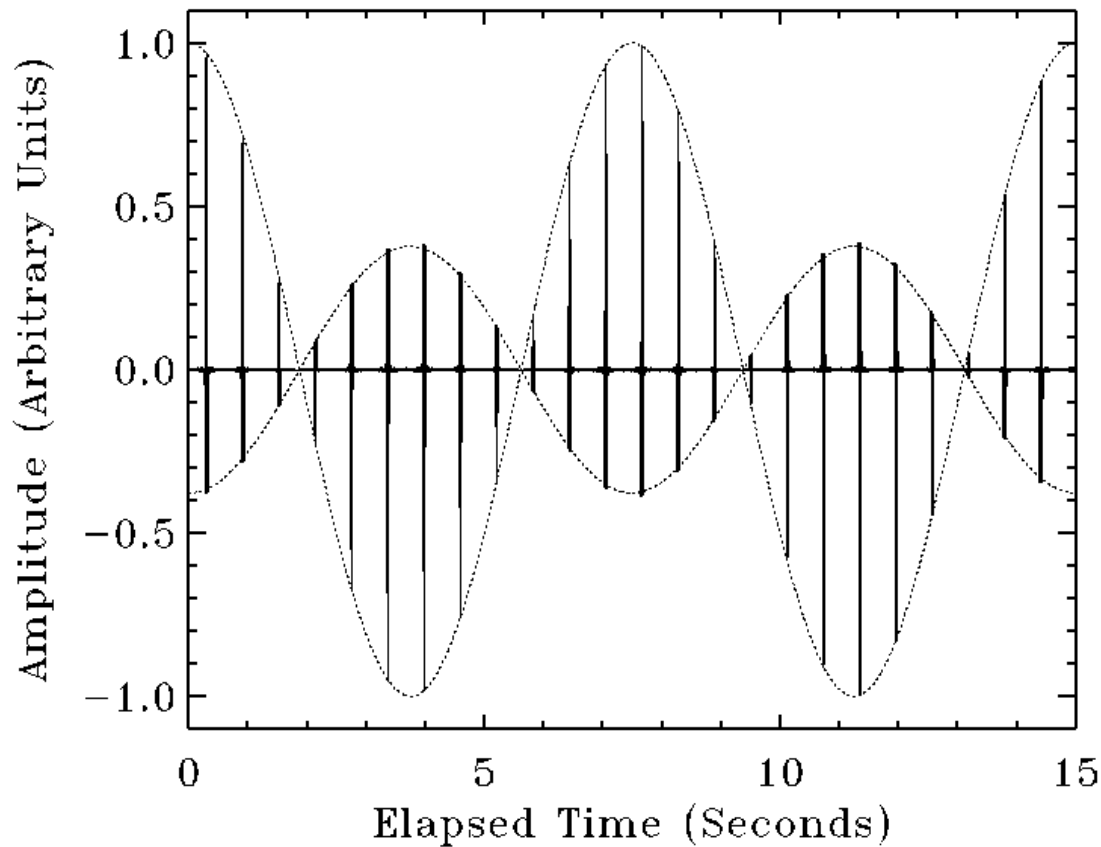
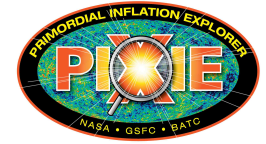
Imaginary (sine)=Phase shift

The key detector transfer function, heat capacity and thermal conductance show linearly in the imaginary part of the Fourier transform and quadratically in the real part

The forward and reverse stroke allow unambiguous untangling of effects in time, with effects from different sides. $\sim 100,000,000$ samples to compare

Systematics: Spin

Spacecraft Spin



Spacecraft spin imposes amplitude modulation of entire fringe pattern

For "perfect beam" only $m=0$ components are nonzero

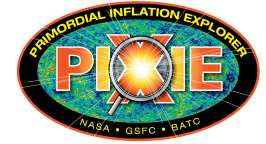
Spin allows sampling of the beam
At $m=0-12$.

Only $m=2$ is degenerate with polarization
 $m=1,3-12$ can be used to study the beam.

ONLY the $m=2$ DIFFERENTIAL
Asymmetries lead to Polarization
errors.

~6,000,000 Rotations to compare

Symmetries and Systematic Errors



20 Ways to Find An Error

Symmetry	Mitigates
x vs y Polarization	Pointing
Left vs Right Detector	Particle Hits
A vs B Beam	Differential loss
Real vs Imaginary FFT	Detector heat capacity
Forward vs Backward FTS	Microphonics
Left vs Right XCal	Calibration, Beam
Hot vs Cold	Non-Linearities
Ascending vs Descending	Far sidelobes, calibration
Spin m=2	Electronics
Spin m=1, 3 to 12	Beam asymmetries

$$P_{Lx}(\omega) = g_{Lx}(\omega) (S_{Bx}(\nu) - S_{Ay}(\nu))$$

$$P_{Ly}(\omega) = g_{Ly}(\omega) (S_{By}(\nu) - S_{Ax}(\nu))$$

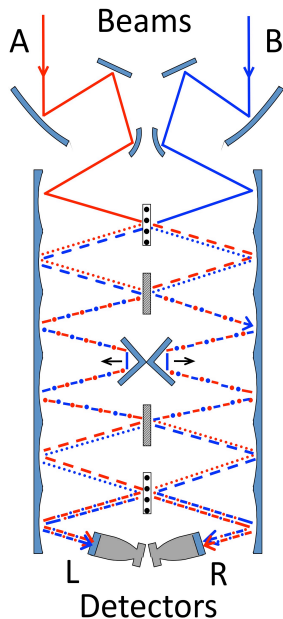
$$P_{Rx}(\omega) = g_{Rx}(\omega) (S_{Ax}(\nu) - S_{By}(\nu))$$

$$P_{Ry}(\omega) = g_{Ry}(\omega) (S_{Ay}(\nu) - S_{Bx}(\nu))$$

Add them: Sky cancels, leaving only systematics

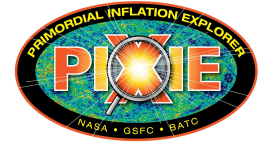
Subtract them: Instrument cancels, leaving only sky

No assumptions about sky or instrument model



Effect	Leakage	PIXIE Mitigation						Residual (nK)
		FTS	Spin	Orbit	XCal	Symmetry	Preflight	
Cross-polar beam	E→B		✓			✓	✓	1.5
Beam ellipticity	∇ ² T→TB		✓	✓		✓	✓	2.7
Polarized sidelobes	ΔT→B		✓	✓		✓	✓	1.1
Instrumental polarization	ΔT→B		✓	✓	✓	✓	✓	<0.1
Polarization angle	E→B			✓		✓	✓	0.7
Beam offset	ΔT→B		✓	✓	✓	✓	✓	0.7
Relative gain	ΔT→B	✓			✓	✓		<0.1
Gain drift	T→B	✓			✓	✓		<0.1
Spin-synchronous emission	ΔT→B	✓	✓		✓	✓	✓	<0.1
Spin-synchronous drift	T→B	✓			✓	✓	✓	<0.1

Summary



The temperature will not match the CMB ***precisely***
but good enough to limit the signals to a few mK

The instrument will not be ***perfect***
but good enough to reduce the emission to tens of uK

The symmetry will not be ***exact***
but good enough to reduce the imbalance to ~few 100 nK

The operational balance will not be ***ideal***
but good enough to reduce the bias to a few nK

The calibration is limited by the ***total data set*** so it
will be able to reduce the residual to ~1 nK