

Critical doping and superconductivity domes in doped strontium titanate

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Superconducting Transition Temperatures of Semiconducting SrTiO_3

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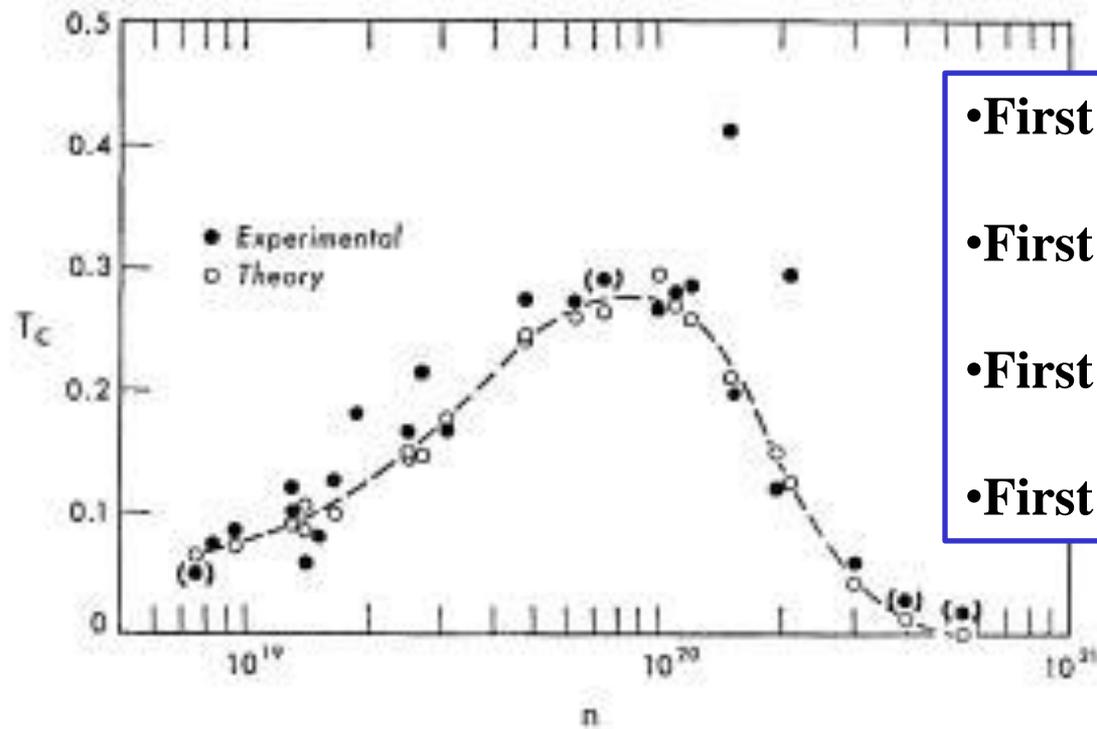
Department of Physics, University of California, Berkeley, California

AND

J. F. SHOOLEY,‡ W. R. HOSLER,§ AND E. R. PFEIFFER

National Bureau of Standards, Washington, D. C.

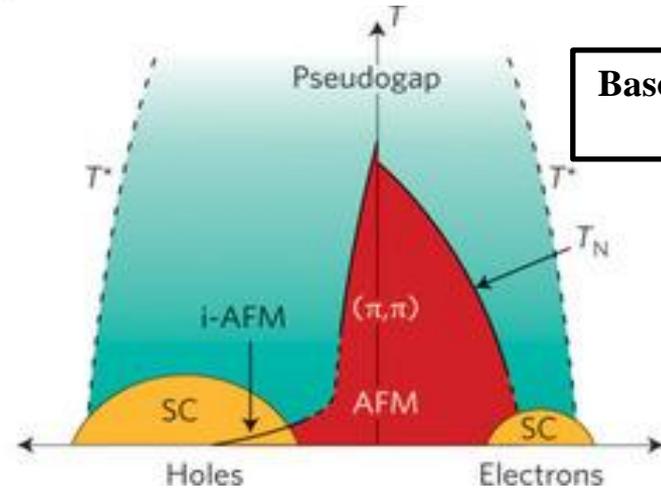
(Received 5 July 1967)



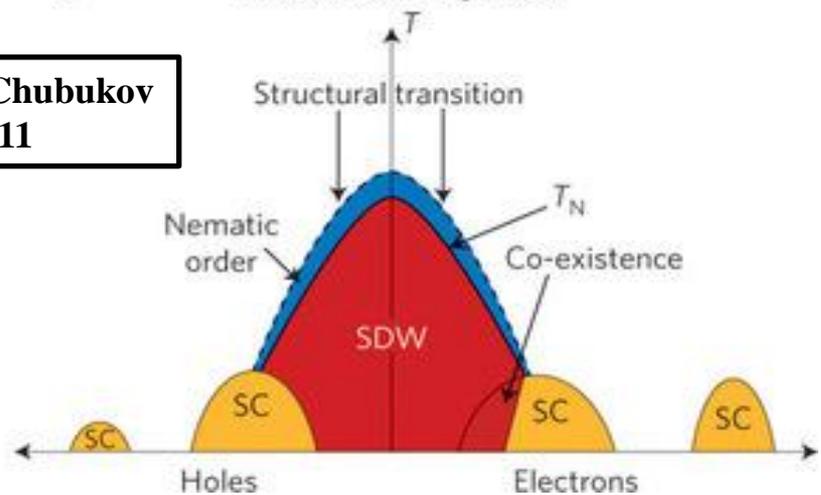
- First **oxide** superconductor
- First **multi-band** superconductor
- First **semiconducting** superconductor
- First superconducting **dome**

Superconducting domes

a Cuprates

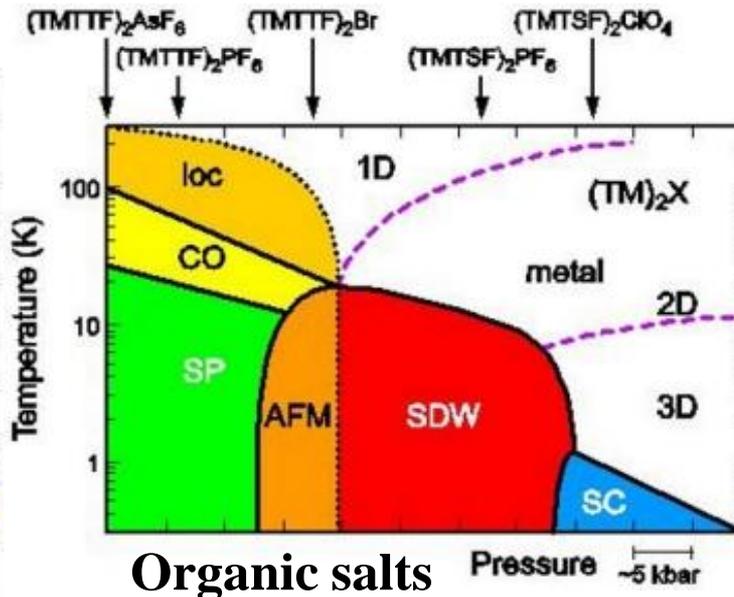
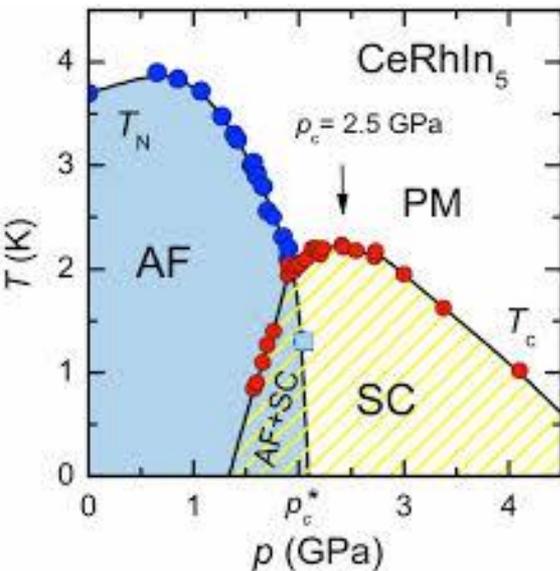


b Pnictides



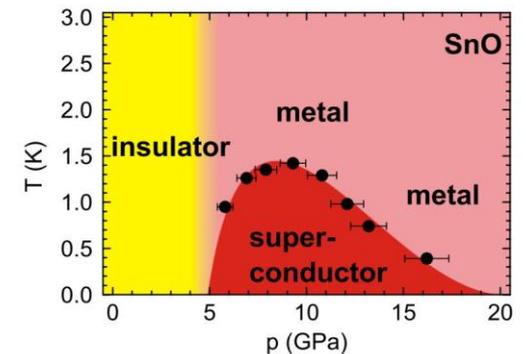
Basov & Chubukov
2011

Heavy fermions

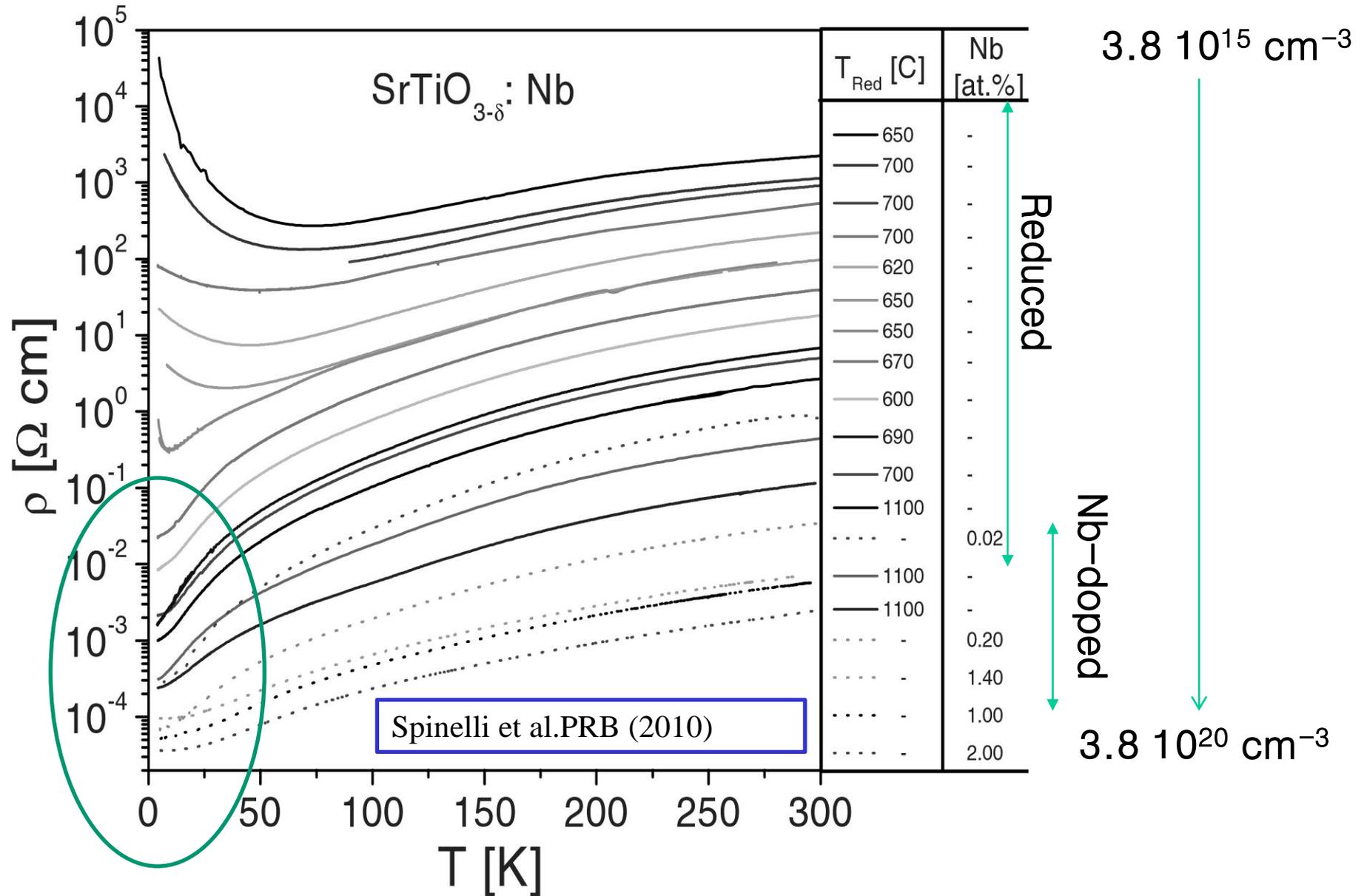


Organic salts

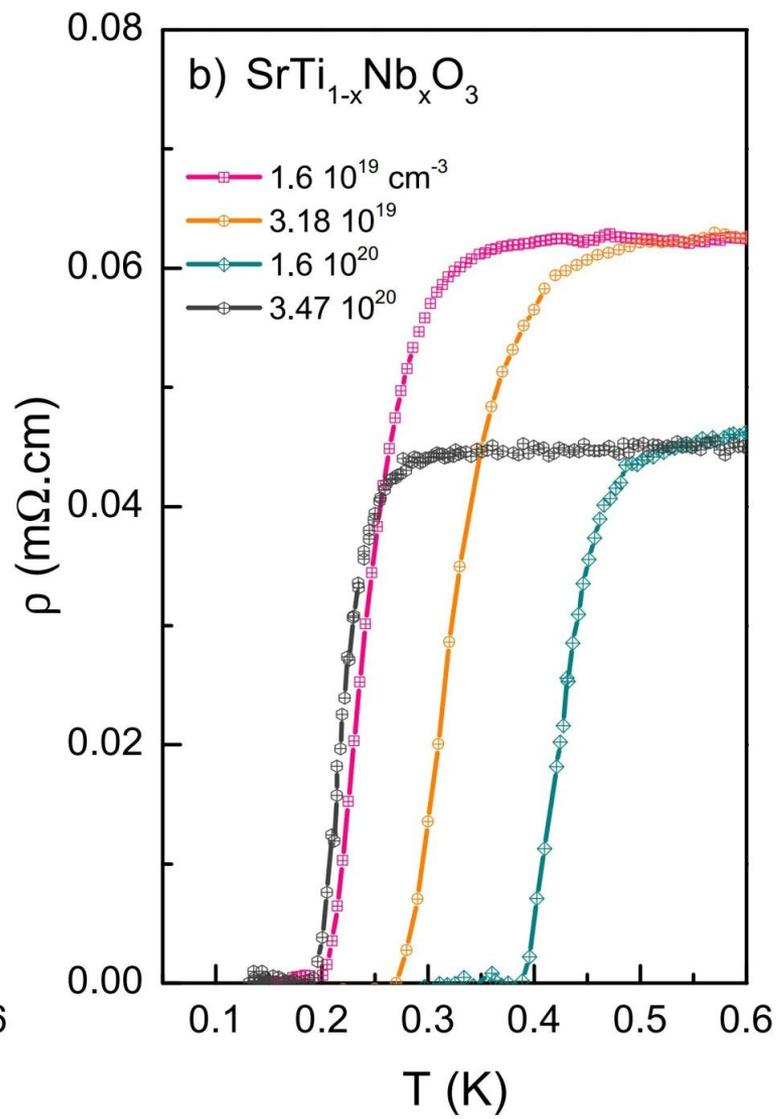
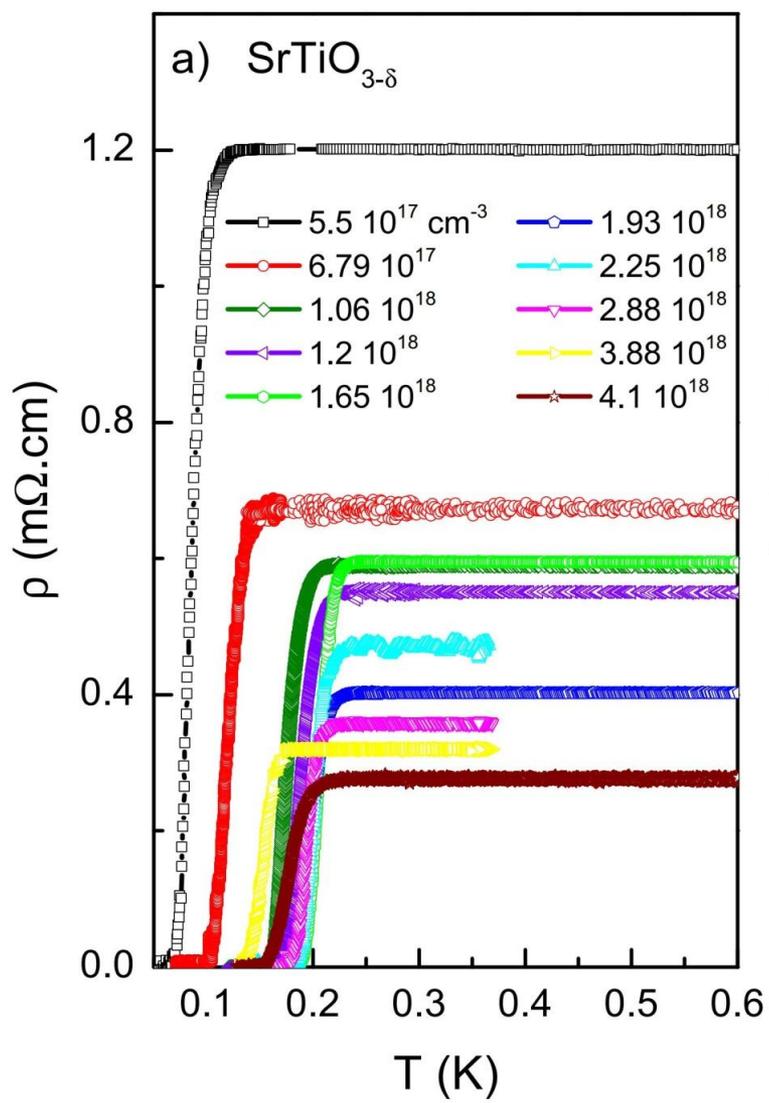
SnO



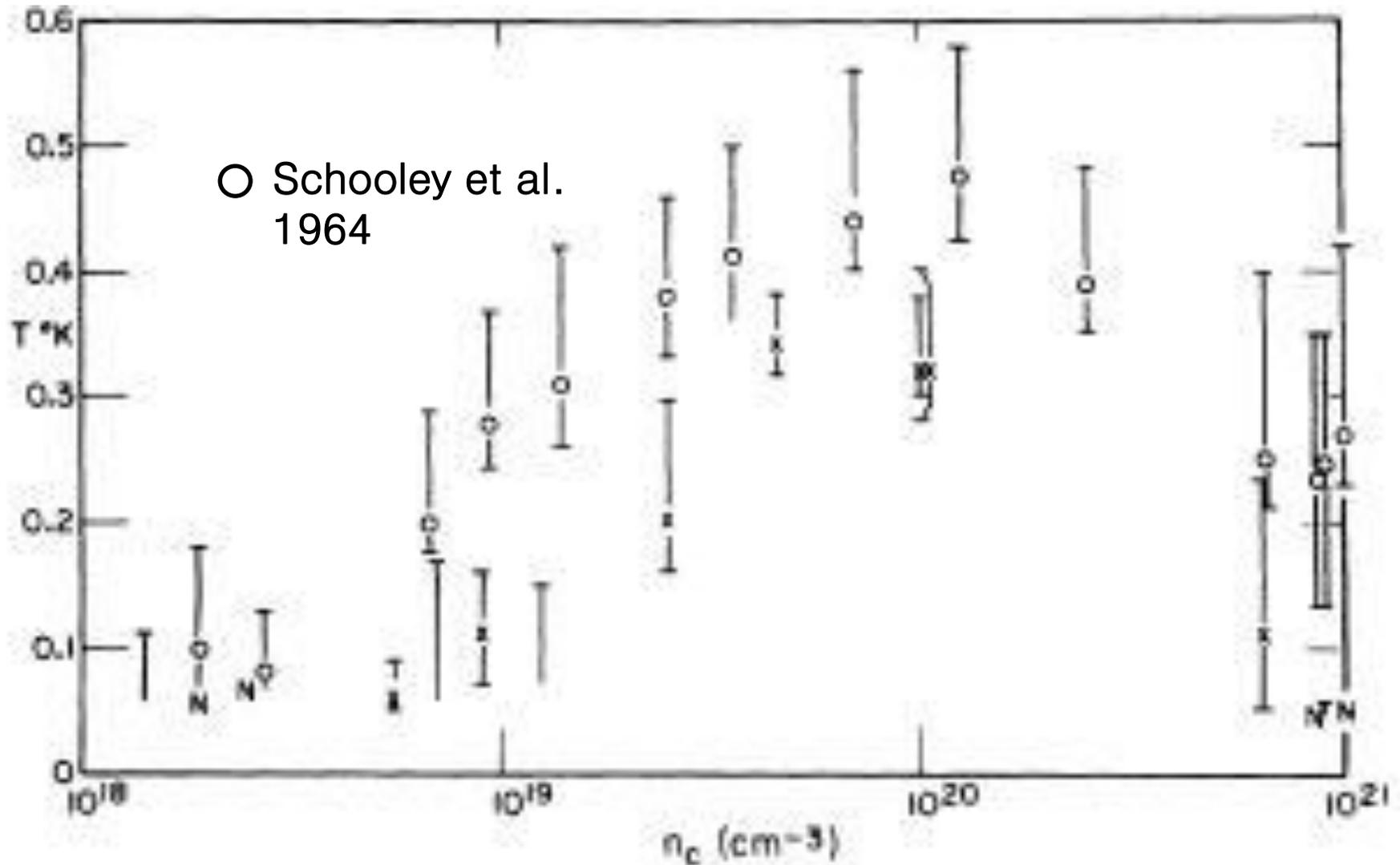
Doping can be tuned in commercially available crystals



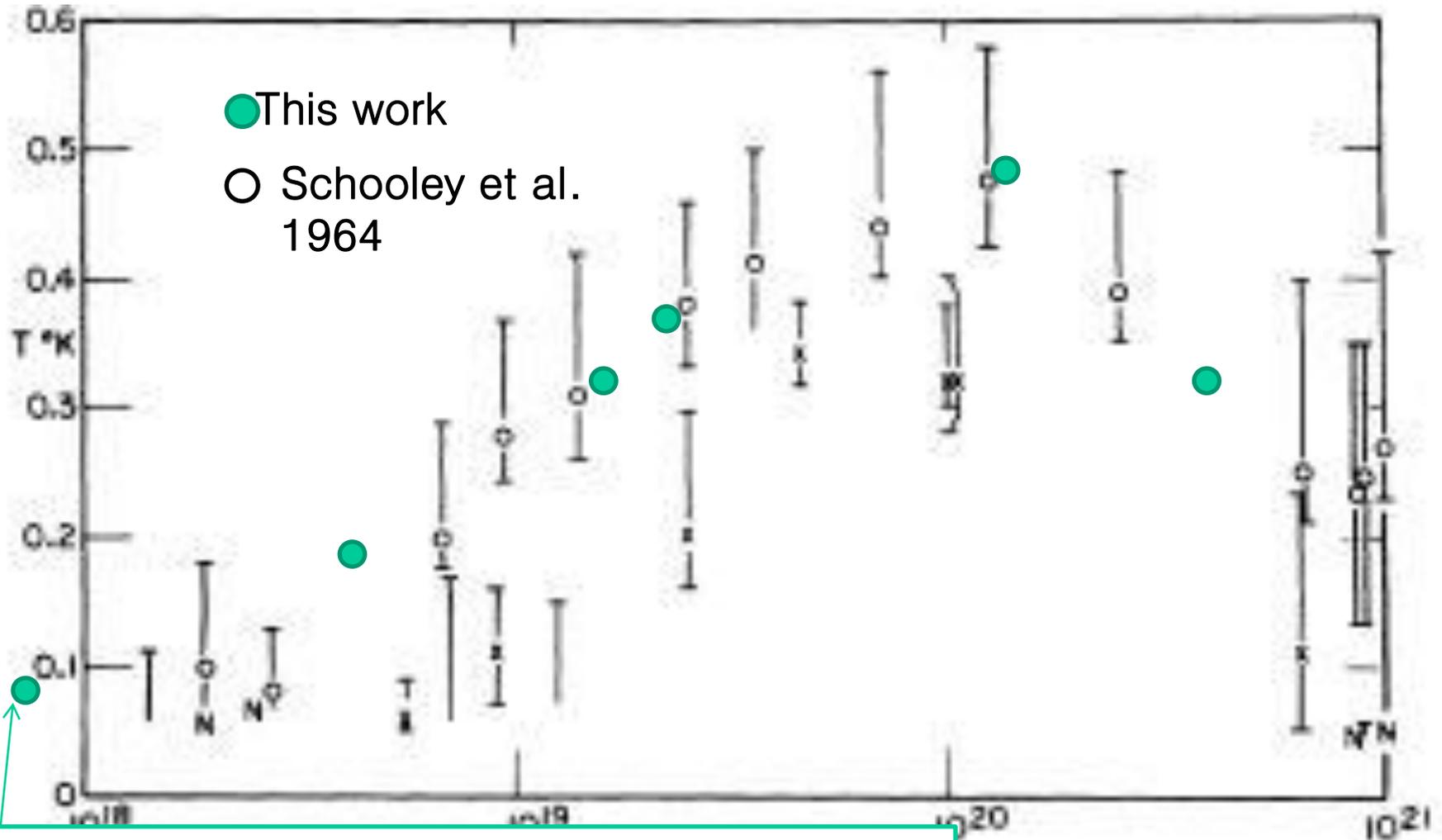
Resistive transitions



The superconducting dome

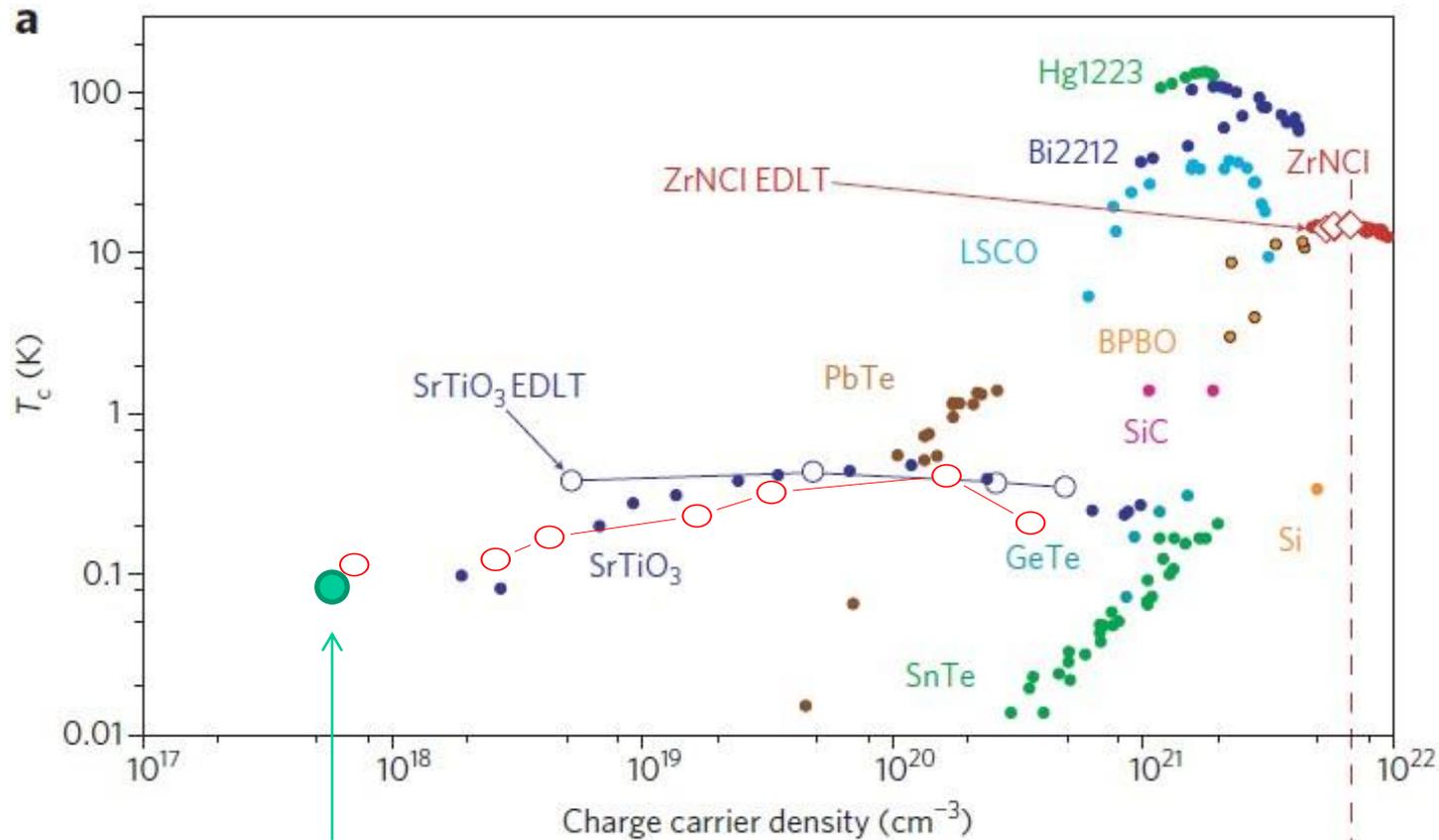


The superconducting dome



$T_c = 86 \text{ mK} @ n = 5.5 \times 10^{17}$

“Semiconducting” superconductors



$5.5 \times 10^{17} \text{ cm}^{-3}$

K Ueno et. al., Nature Nanotechnology 6, 408 2011

STO is the most dilute superconductor

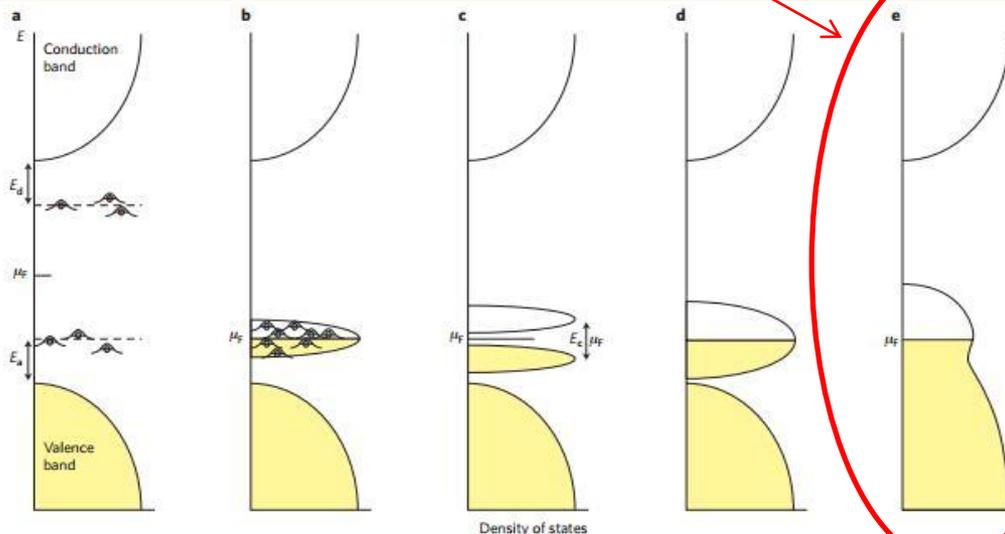
BAND

MOTT

system	STO	PbTe:TI	$\text{Cu}_x\text{Bi}_2\text{Se}_3$	Si:B	C:B	SiC:B	YBCO
x_c	10^{-5}	$3 \cdot 10^{-3}$	$9 \cdot 10^{-2}$	$\sim 10^{-2}$	$\sim 10^{-2}$	$\sim 10^{-2}$	$5 \cdot 10^{-2}$

Critical doping to induce superconductivity in doped insulators

X. Blase et al., Nature Materials 8, 375–382 (2009)



Is the normal state:

- An impurity-band metal?
- Or a metal with sharp Fermi surface?

Figure B2 | Evolution of the electronic density of states and band structure with increasing p-type doping. Doping increases from a to e. Coloured area represents filled states.

Fermi surface truncated by Landau tubes

Shoenberg 1984

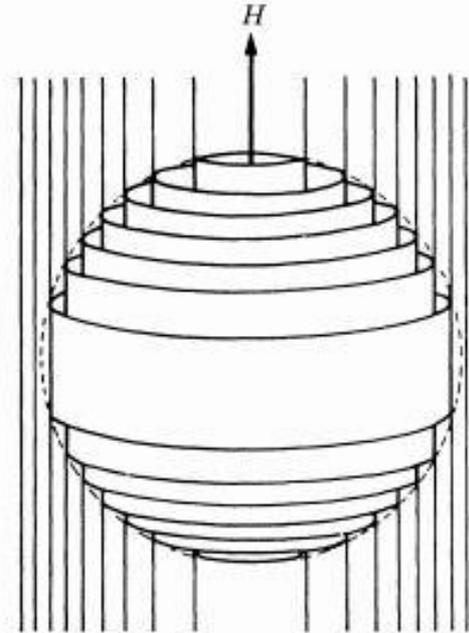


FIGURE 3. The permitted states in a magnetic field H lie on a series of discrete tubes specified by equation (1). At low temperature the occupied states lie within the Fermi surface (here supposed to be spherical). (After Chambers 1956.)

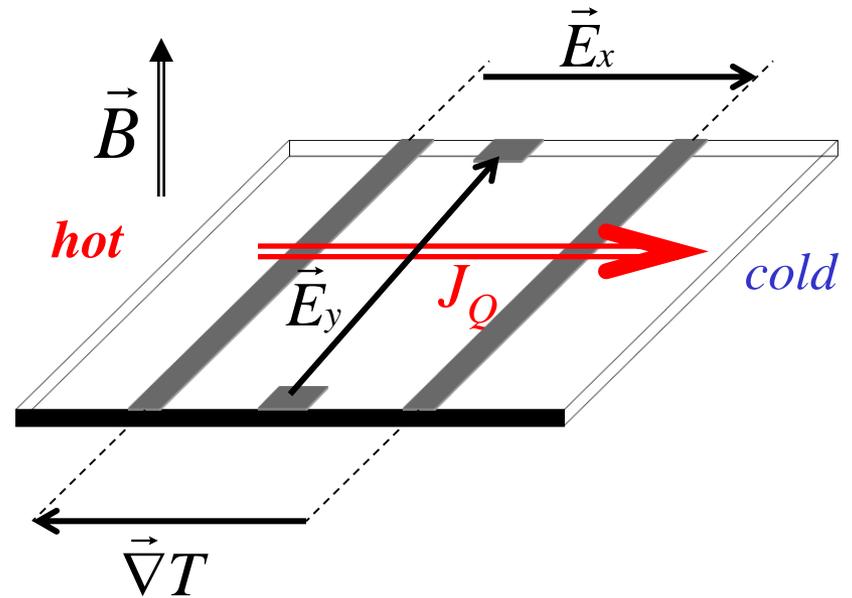
Quantum oscillations!



Electrons share the same Fermi-Dirac distribution!

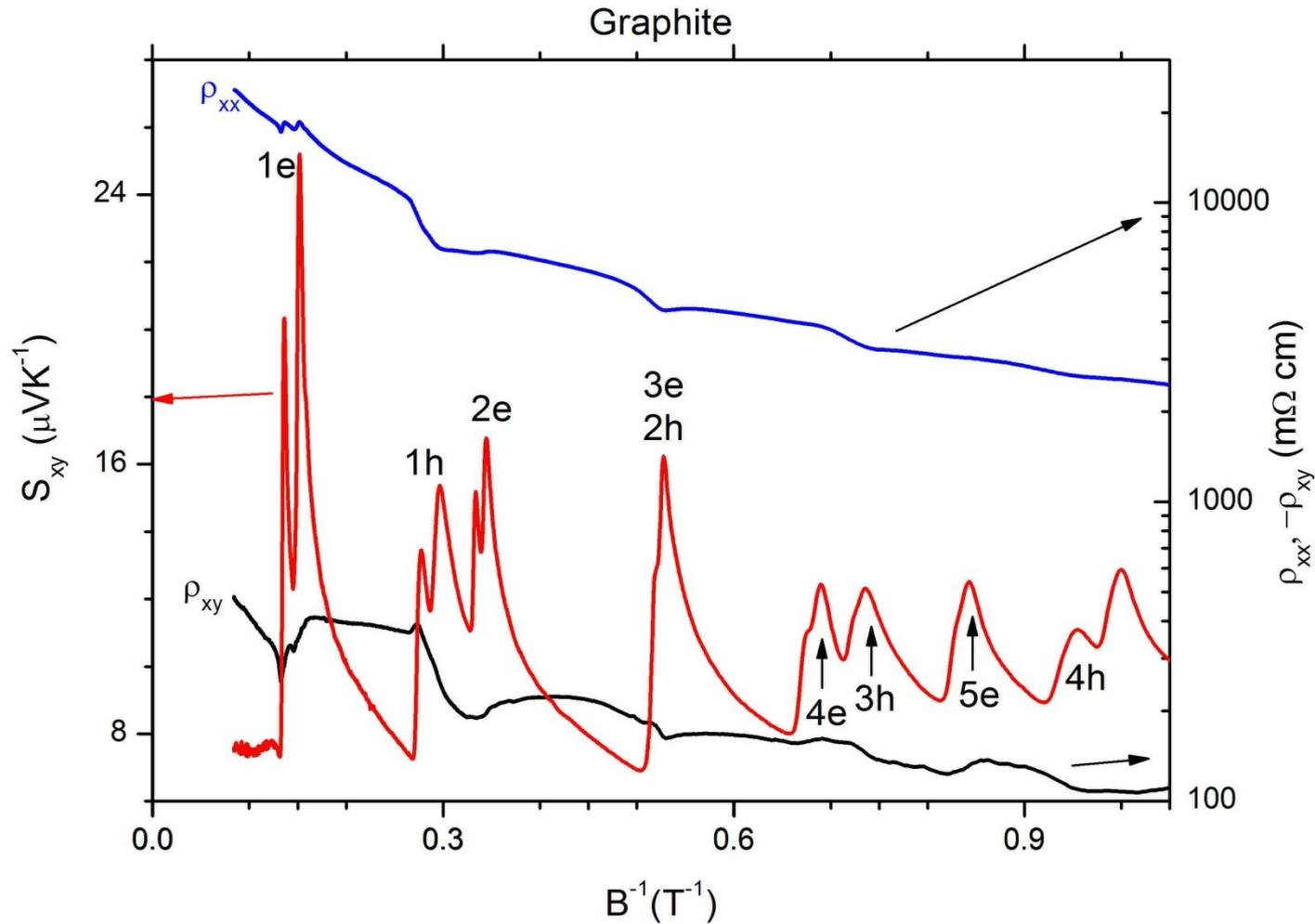
Nernst effect

- A thermal gradient, electrons produces an electric field.
- The Nernst effect refer to the transverse component of this field.

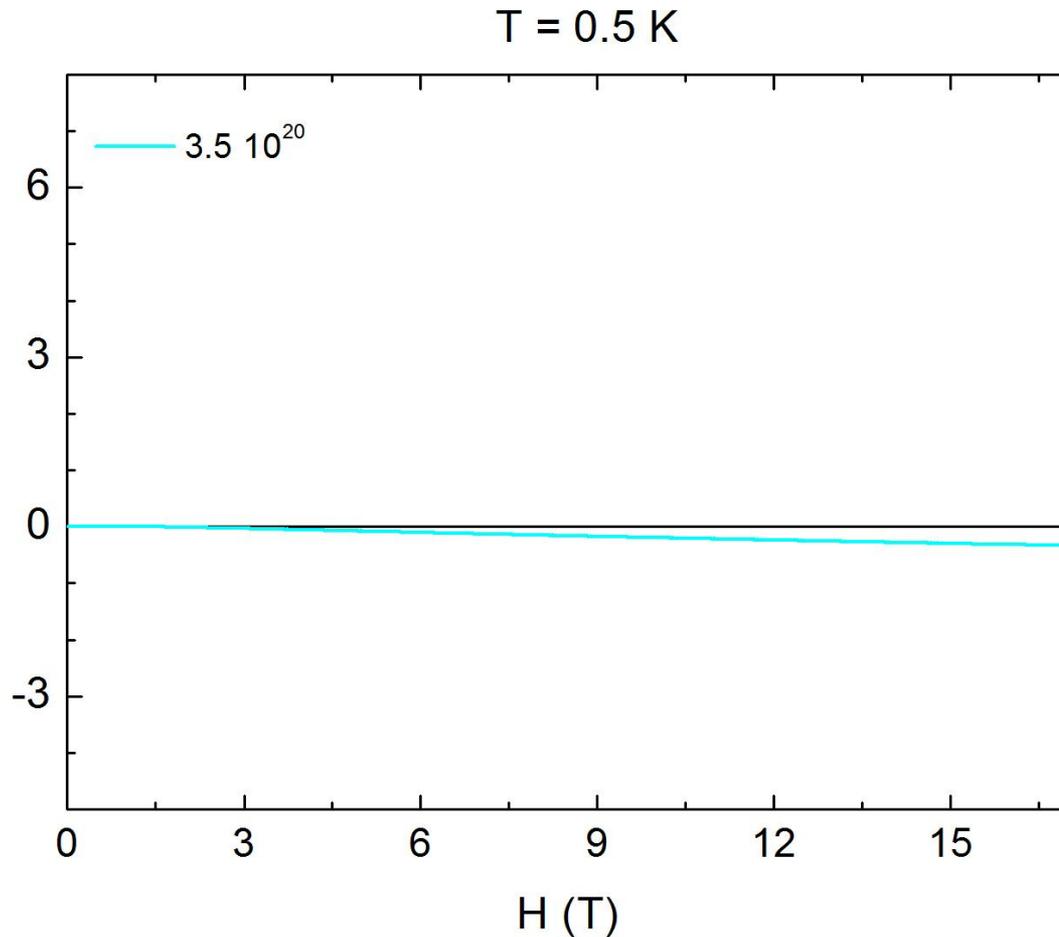
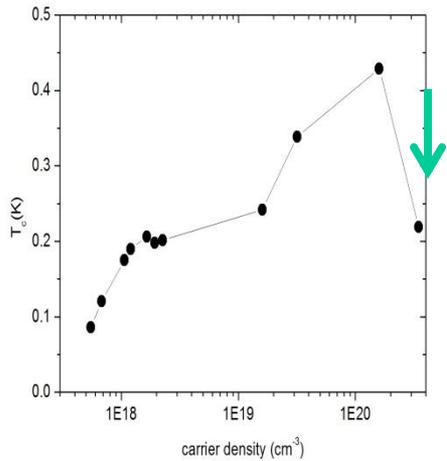


$$S = \frac{-E_x}{\nabla_x T} \quad N = S_{xy} = \frac{-E_y}{\nabla_x T} \quad \left[v = \frac{-E_y}{B_z \nabla_x T} \right]$$

Sensitivity of the Nernst effect as a probe of Landau spectrum

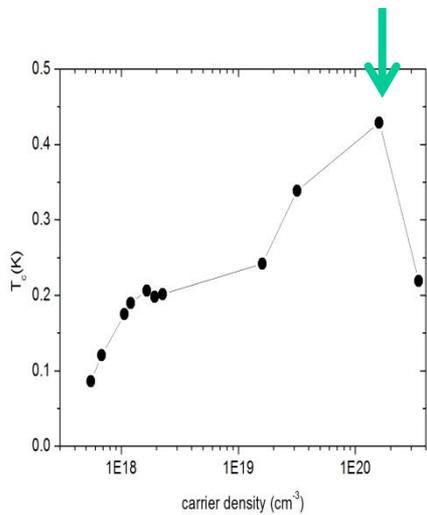


Emergence of Nernst oscillations with underdoping

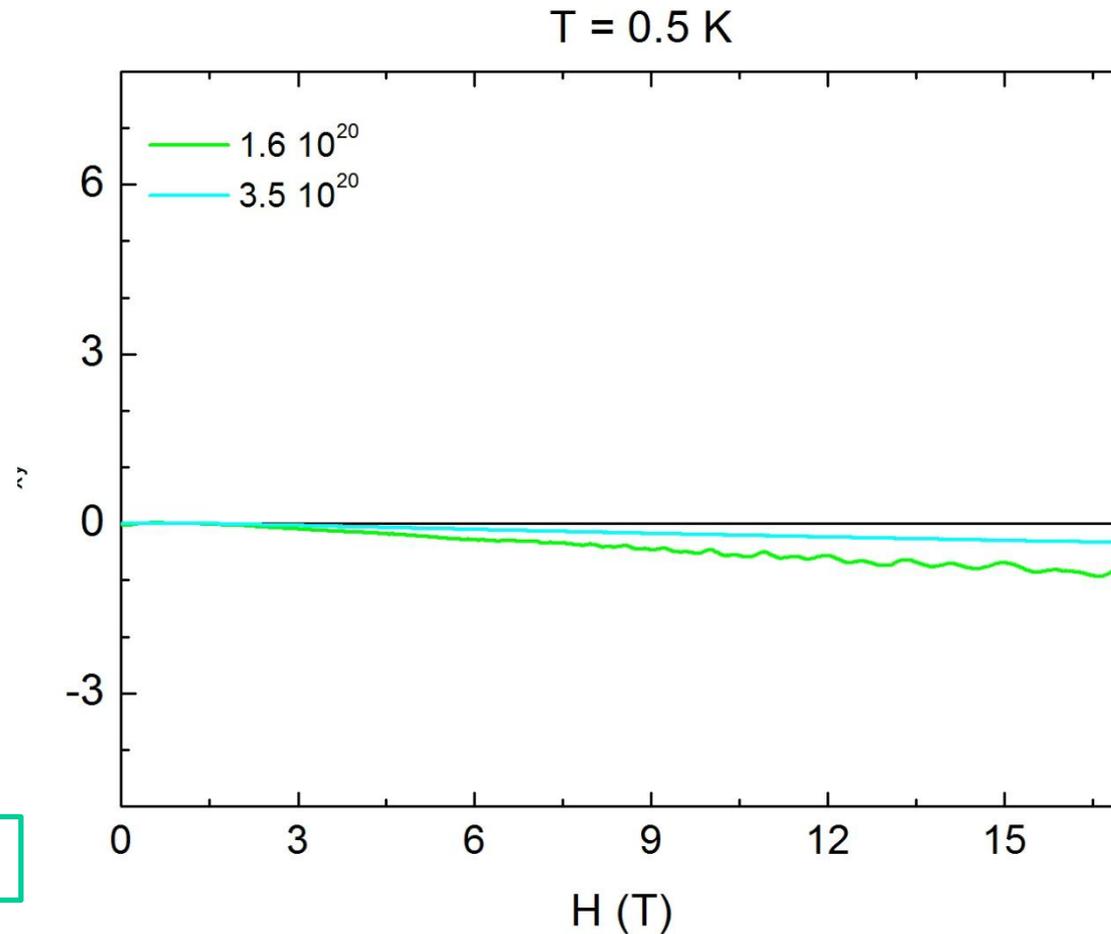


Lin et al., PRX 2013

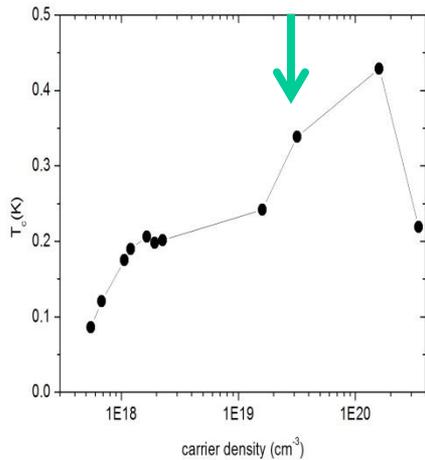
Emergence of Nernst oscillations with underdoping



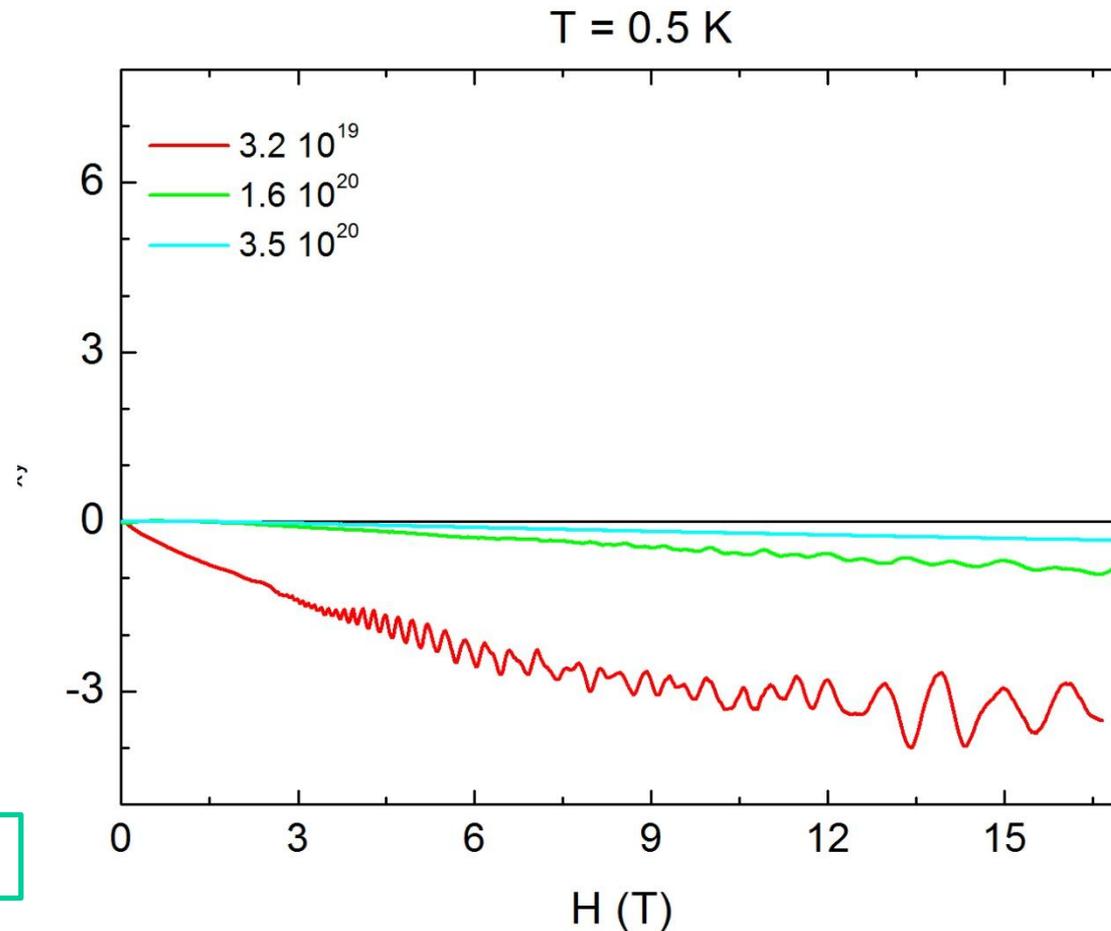
Lin et al., PRX 2013



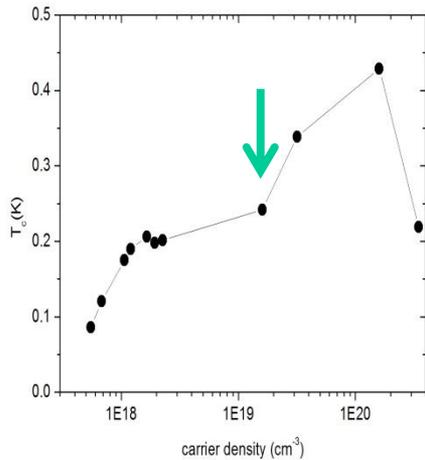
Emergence of Nernst oscillations with underdoping



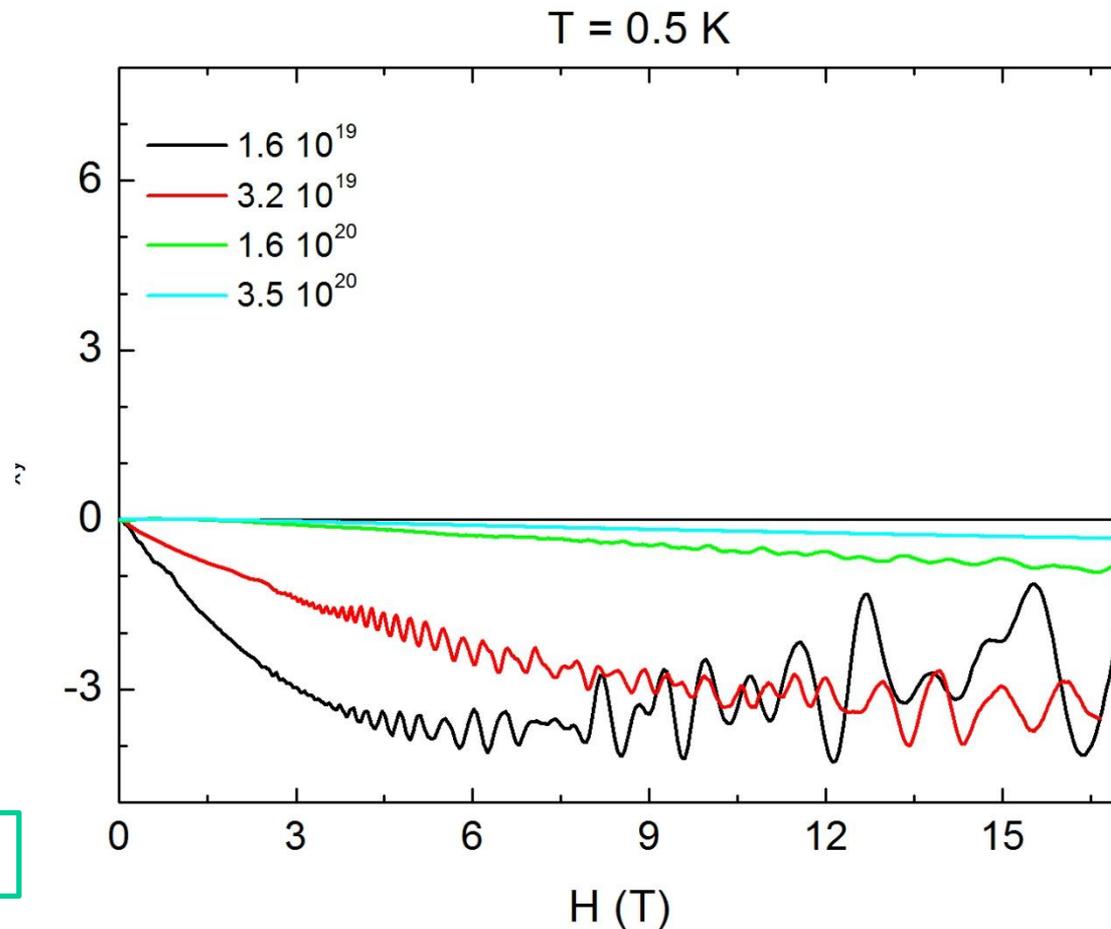
Lin et al., PRX 2013



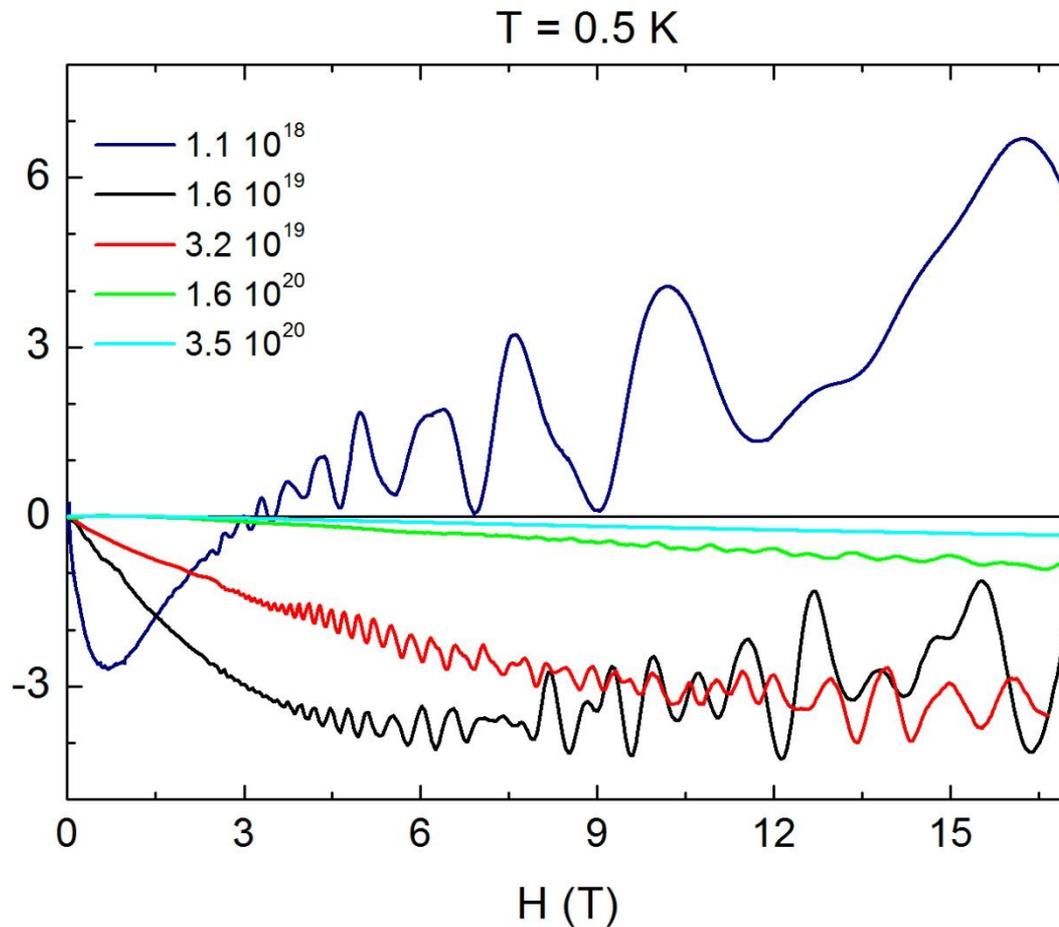
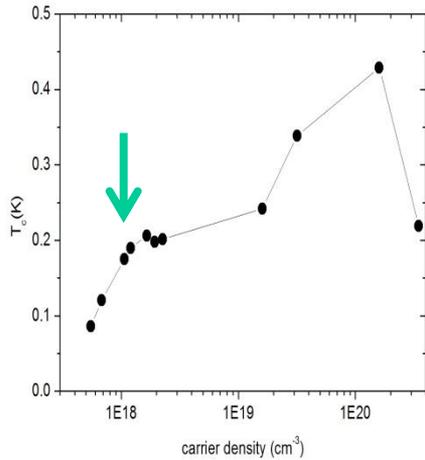
Emergence of Nernst oscillations with underdoping



Lin et al., PRX 2013

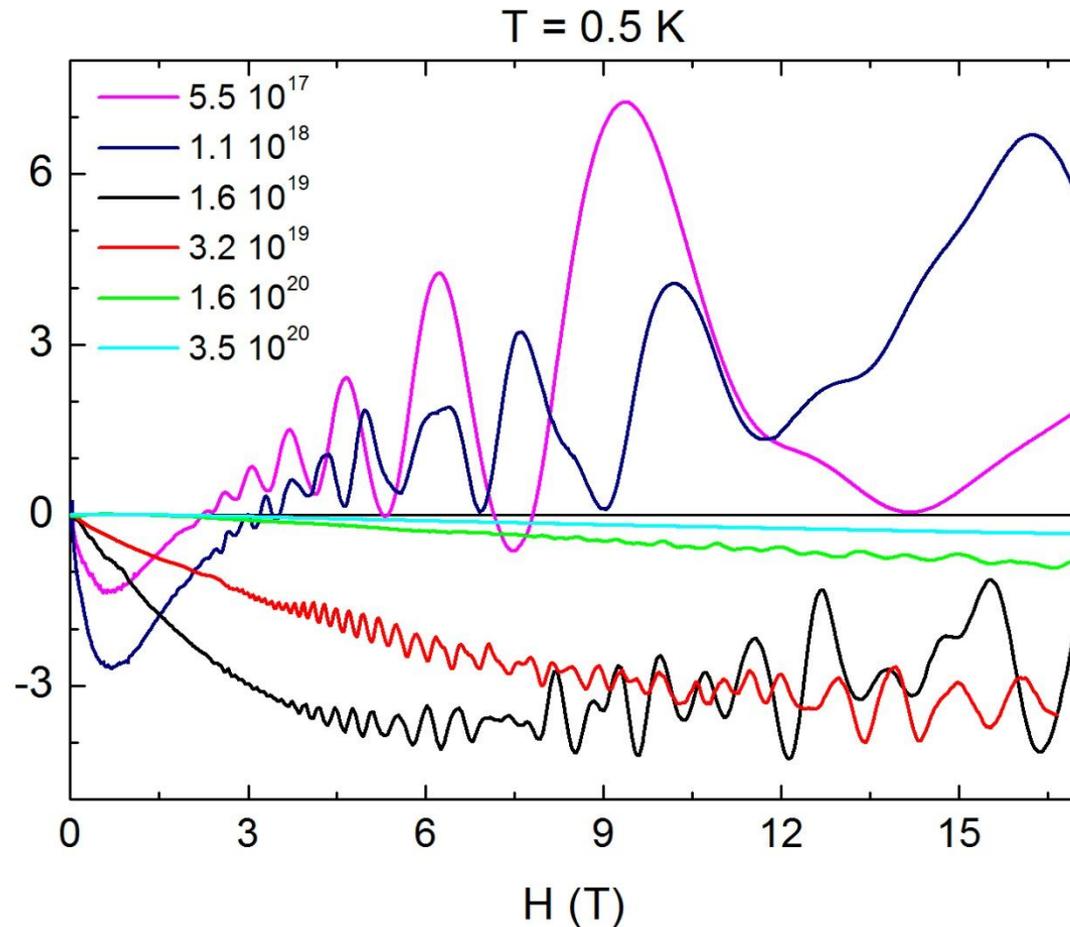
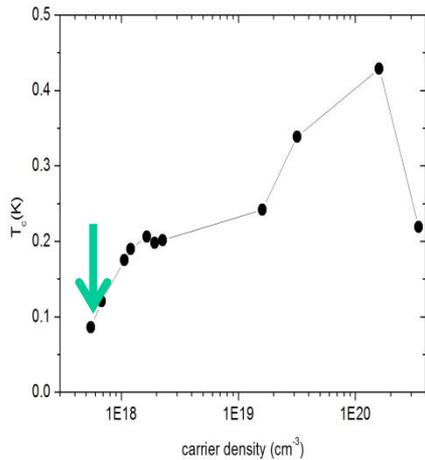


Emergence of Nernst oscillations with underdoping



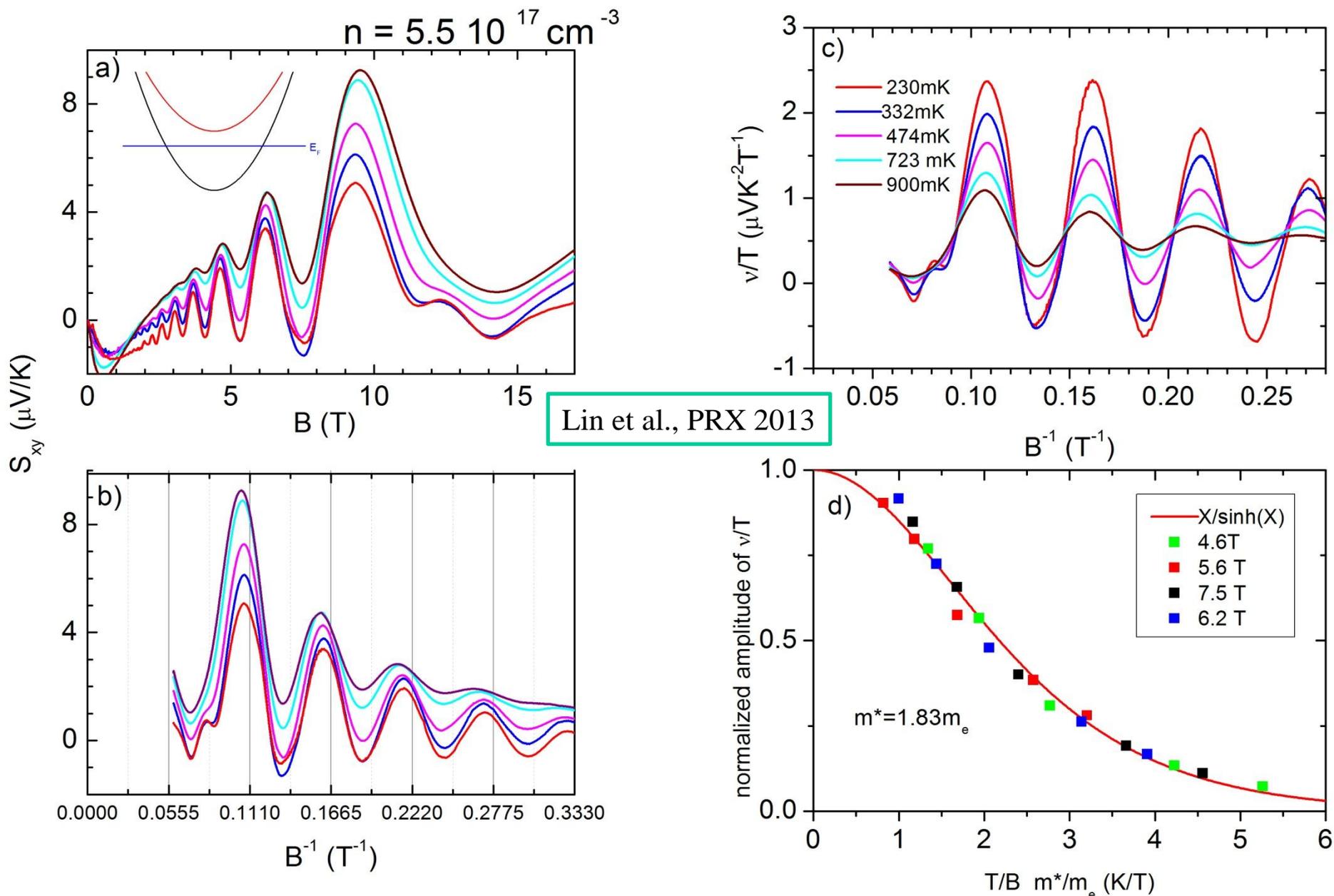
Lin et al., PRX 2013

Emergence of Nernst oscillations with underdoping

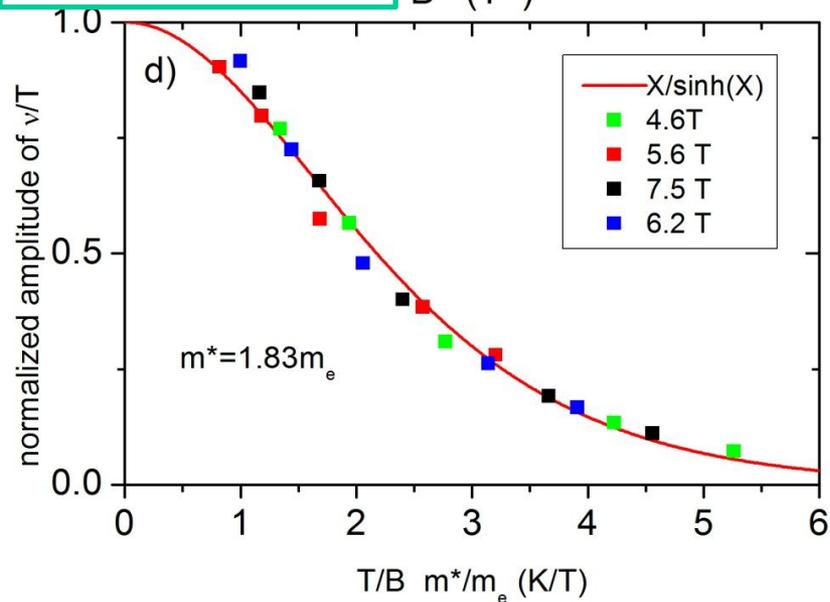
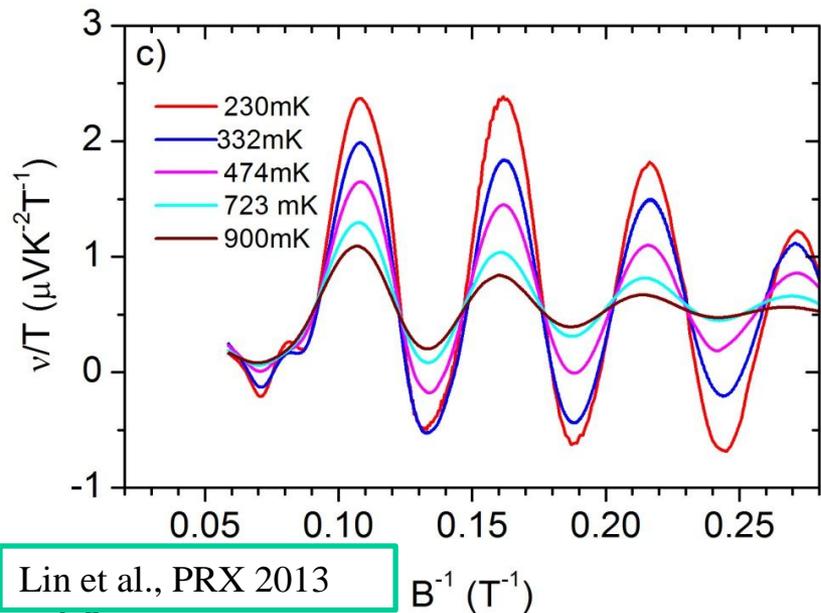


Lin et al., PRX 2013

A single frequency at the lowest concentration



A single frequency at the lowest concentration



Frequency (=18.2 T)



$$F = \frac{\hbar}{2\pi e} A$$

FS Cross section

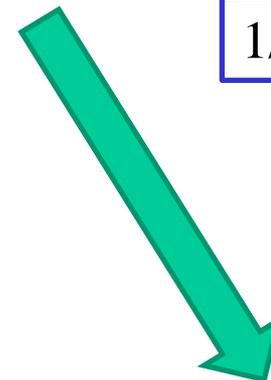
$$A = \pi k_F^2$$



FS volume

$$(n=4.4 \cdot 10^{17} \text{ cm}^{-3})$$

$$1/eR_H = 5.5 \cdot 10^{17} \text{ cm}^{-3}$$



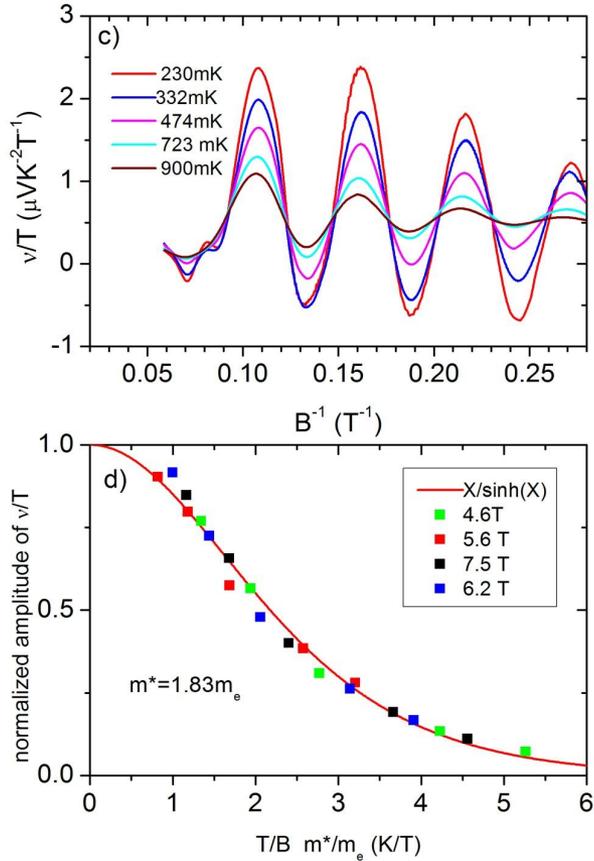
Effective mass
($m^*=1.8m_e$)



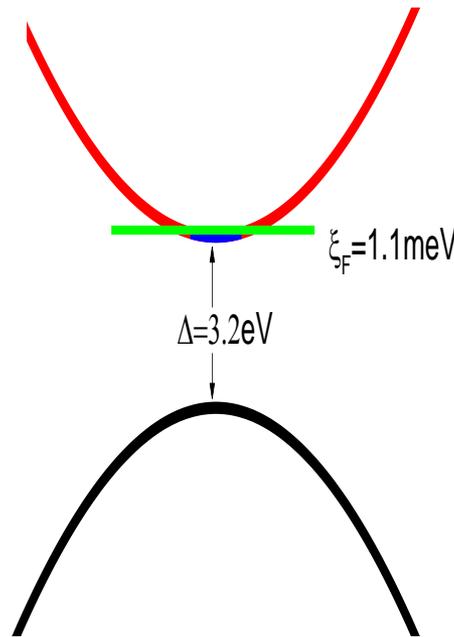
$$E_F = \frac{\hbar^2 k_F^2}{m^*} = 13\text{K}$$

Two ways to estimate the Fermi energy

Quantum oscillations

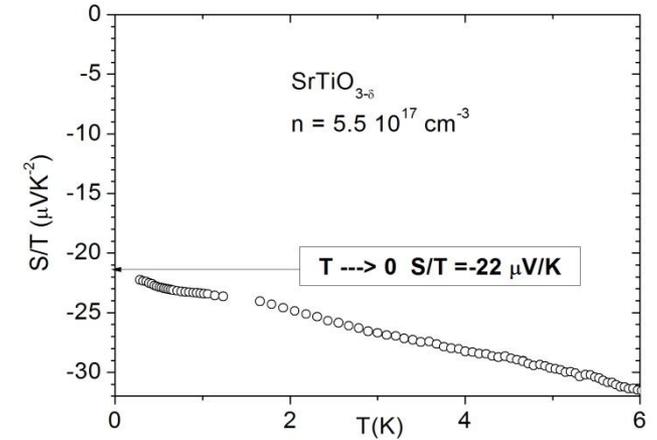


$T_F = 13 \text{ k}$



Lin et al., PRX 2013

Low-temperature
Seebeck coefficient



$$S/T = (\pi^2/3)(k_B/e) 1/T_F$$

$T_F = 12.9 \text{ k}$

A serious challenge for phonon-mediated superconductivity!

@n= $5.5 \cdot 10^{17} \text{ cm}^{-3}$

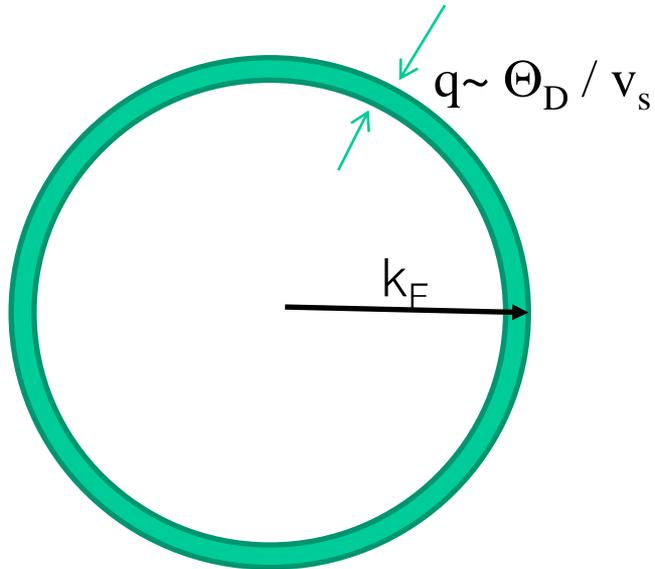
$$T_F (13 \text{ K}) \ll \Theta_D (400 \text{ K})$$

The standard BCS scenario needs $T_F \gg \Theta_D$!

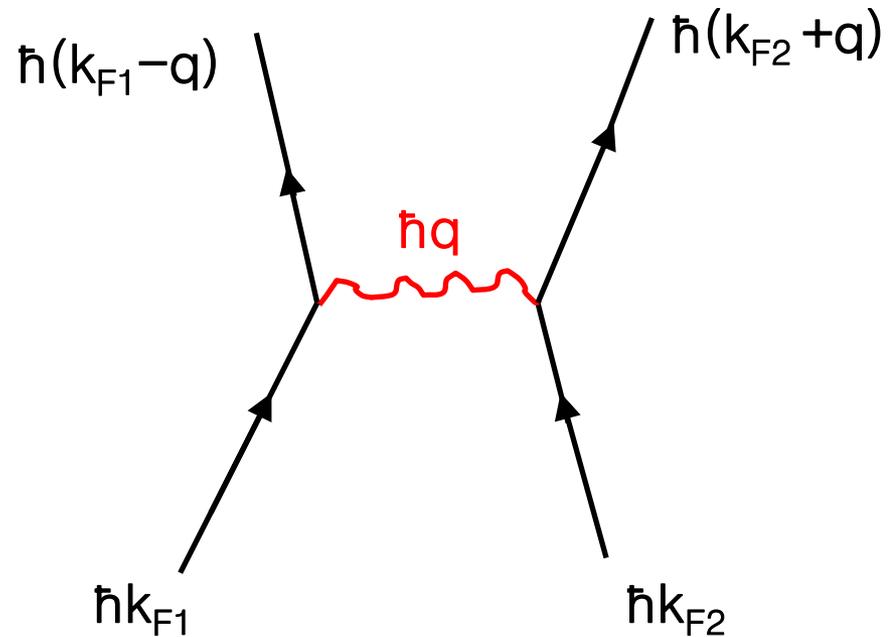
In all conventional (and most unconventional) superconductors, this inequality holds!

But the opposite is true in STO (as in most heavy-fermion superconductors)!

BCS Superconductivity



The attractive interaction is confined to a thin layer of electrons near the Fermi energy!



If not, Cooper pairs would not be stable!

Which low-energy boson is the glue?

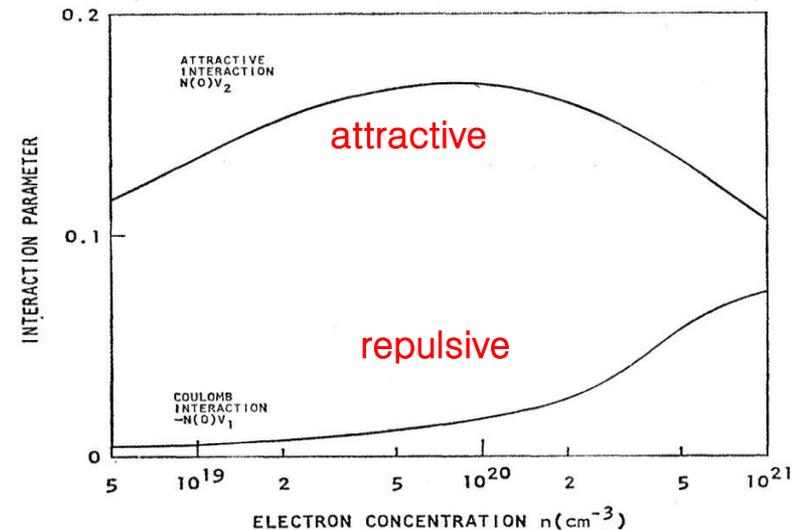
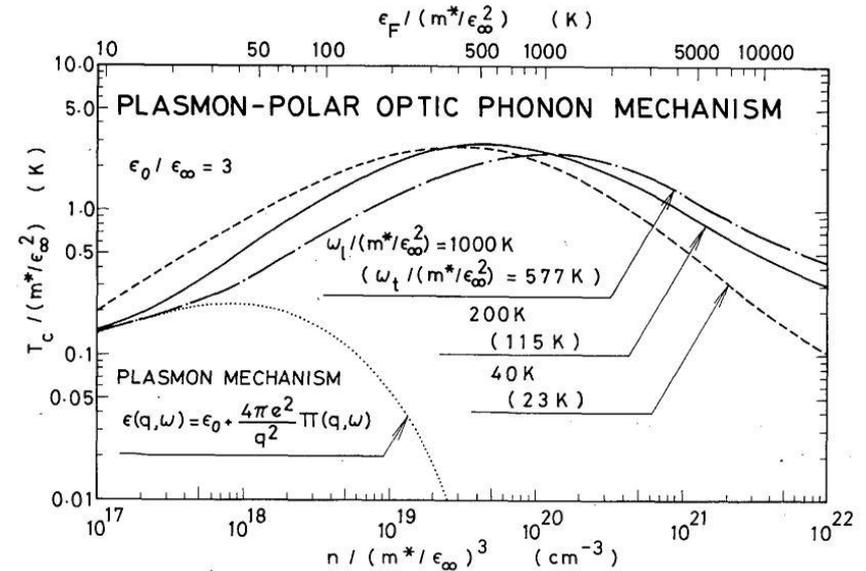
• Plasmons?
(cf. Takada)



• A phonon Soft mode ?
(cf. Appel)

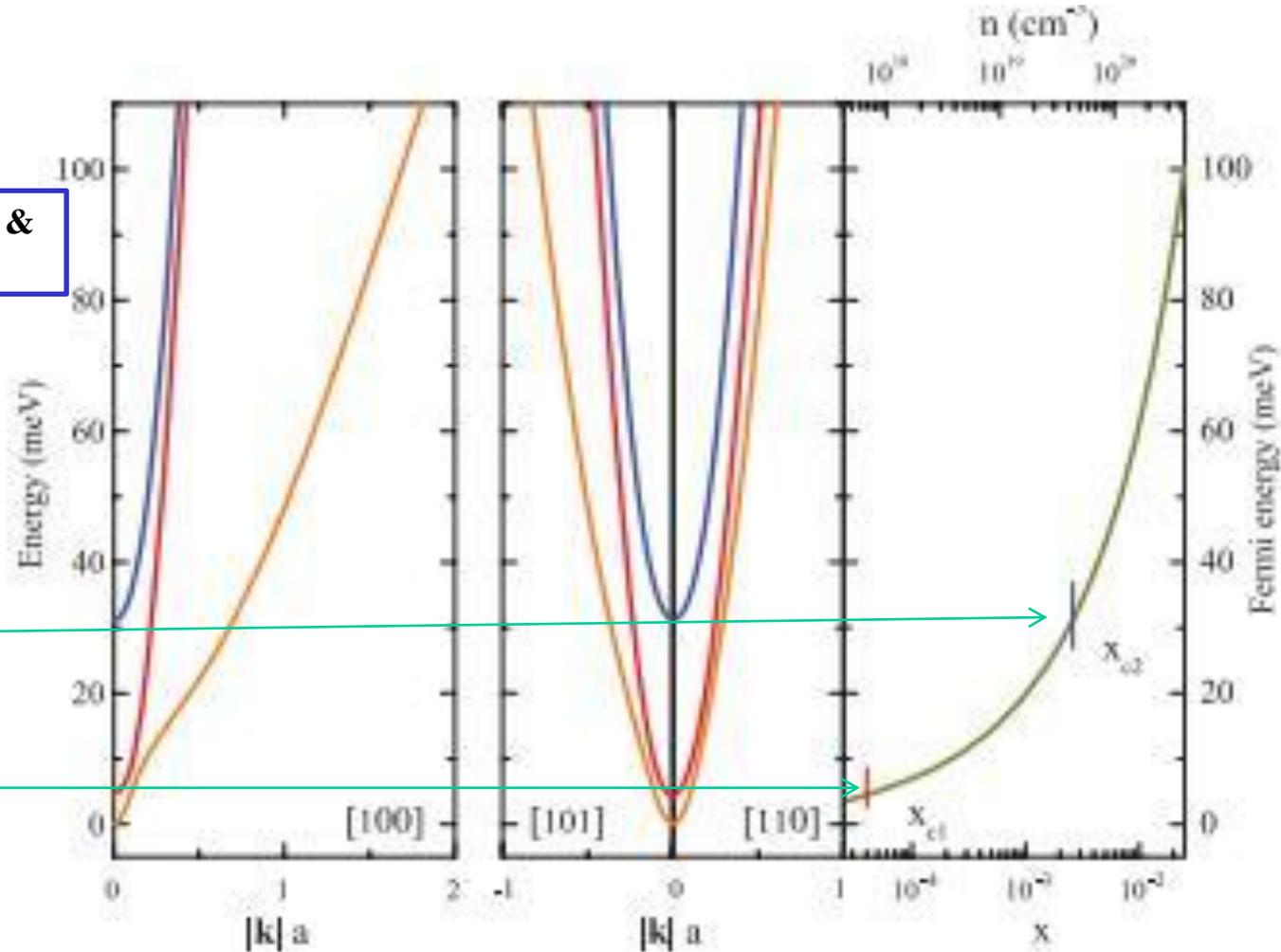


• Ferroelectric quantum criticality?
(cf. Lonzarich)



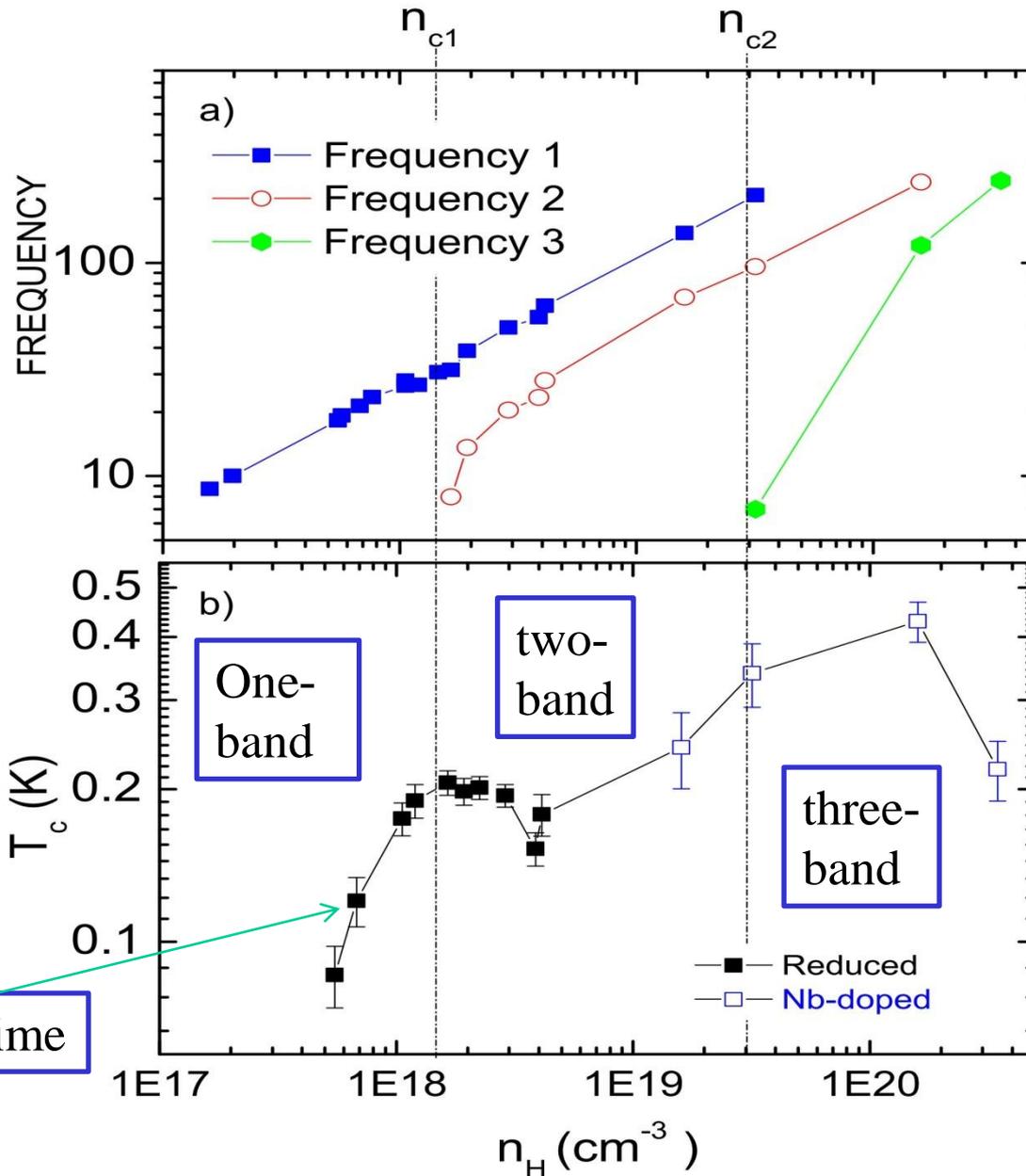
Theoretical band structure in SrTiO₃ by virtual crystal approximation

van der Marel, van Mechelen & Mazin, (2011)



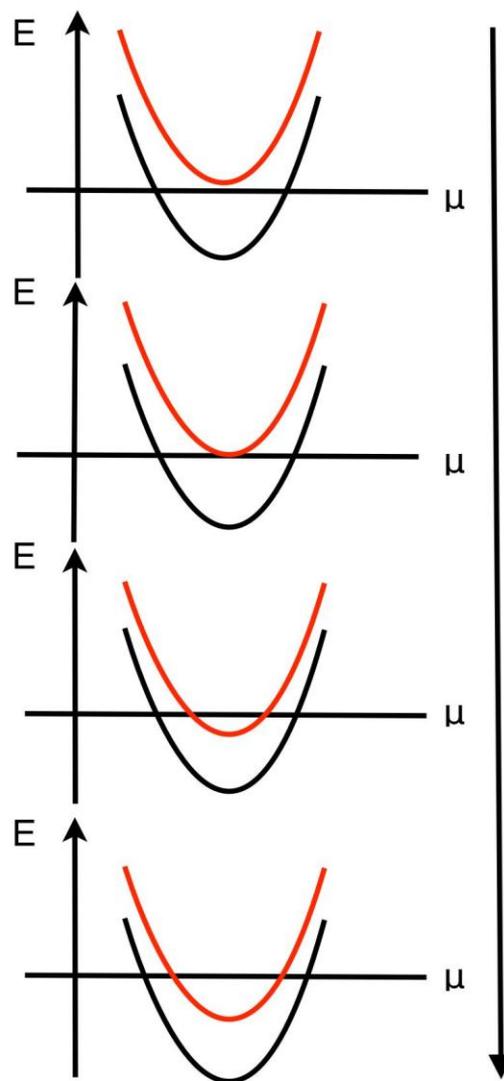
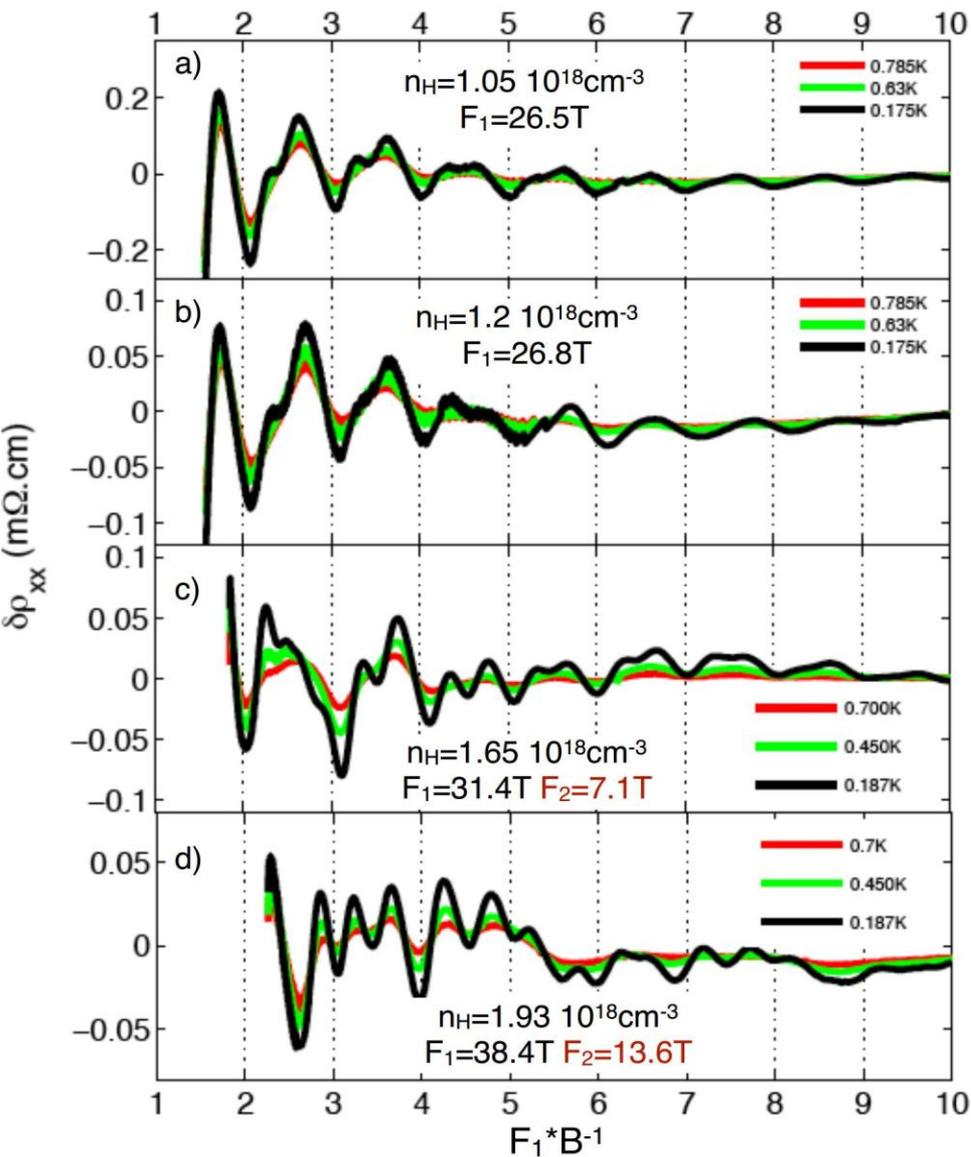
- Threefold degeneracy of a band centered at Γ -point is lifted.
- The three bands are to be successively filled.

Bands and domes!



Large T_c/T_F regime

The first critical doping

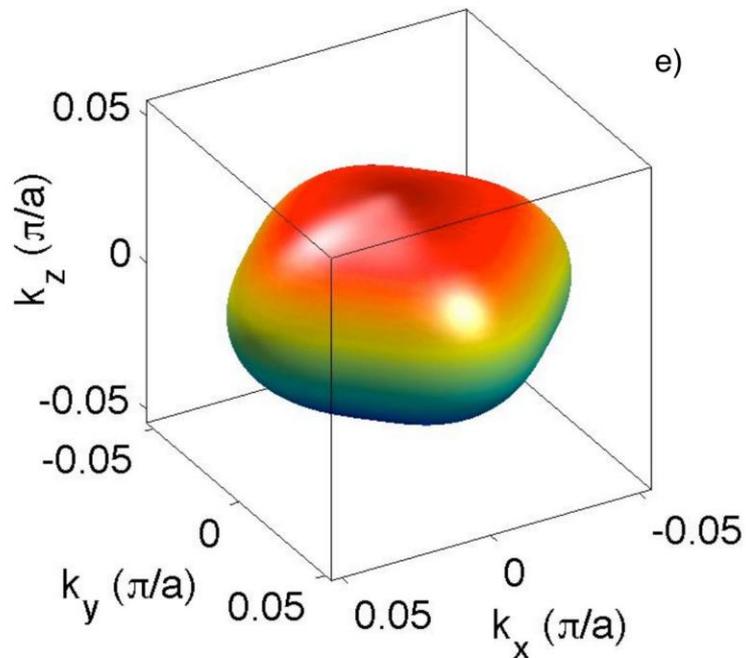


Emergence
of a new
frequency !

Increasing doping

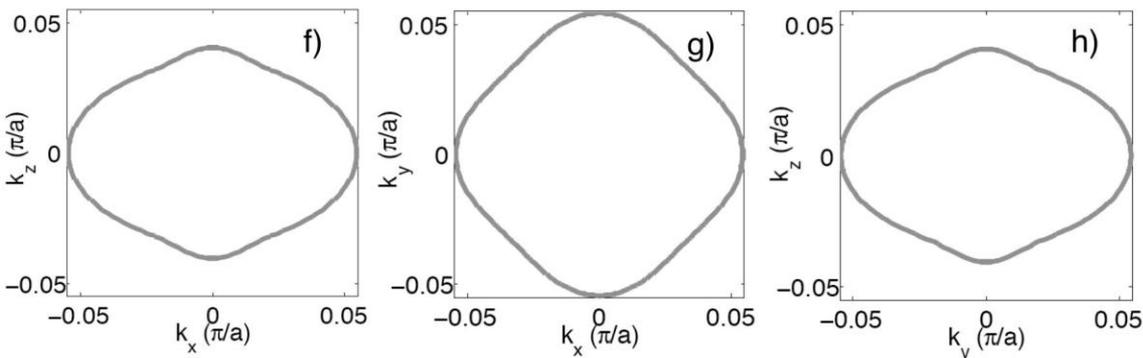
Lin *et al.*
PRL in press
(2014)

Origin of split peaks



Anisotropy of Fermi surface ~ 1.3
S. J. Allen *et al.*
PRB (2013)

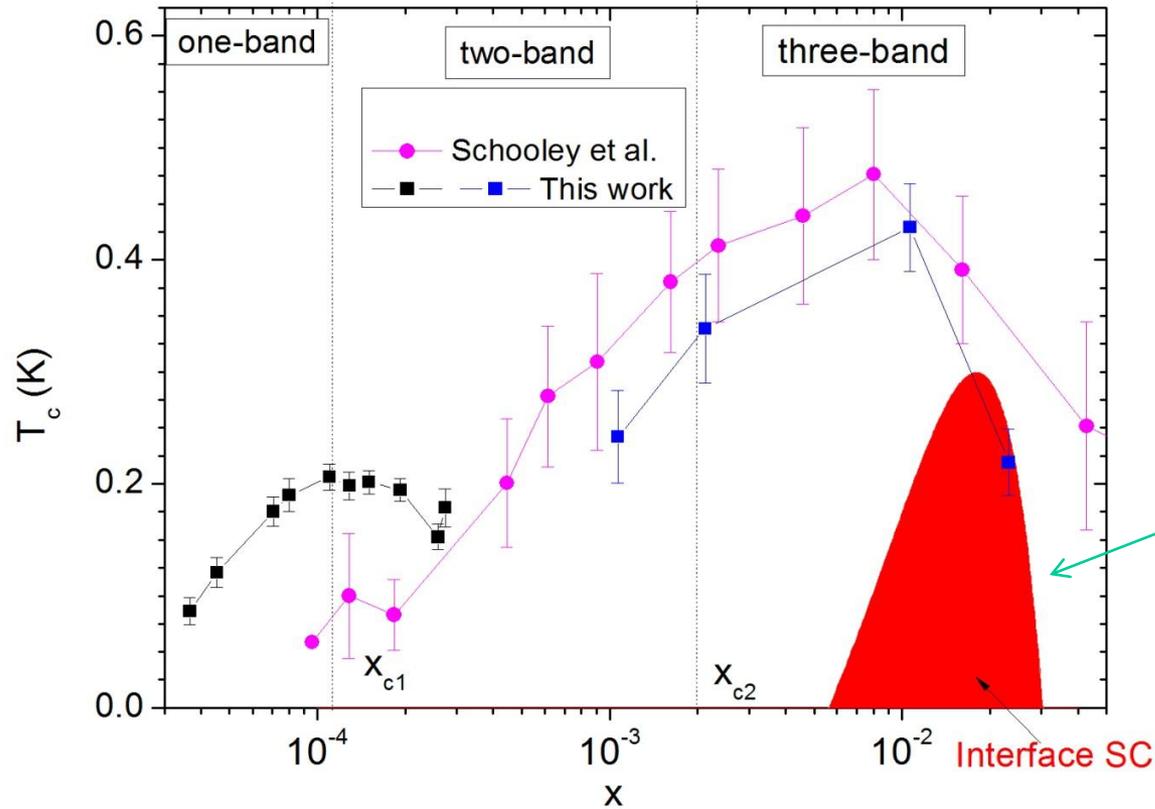
Increasing doping



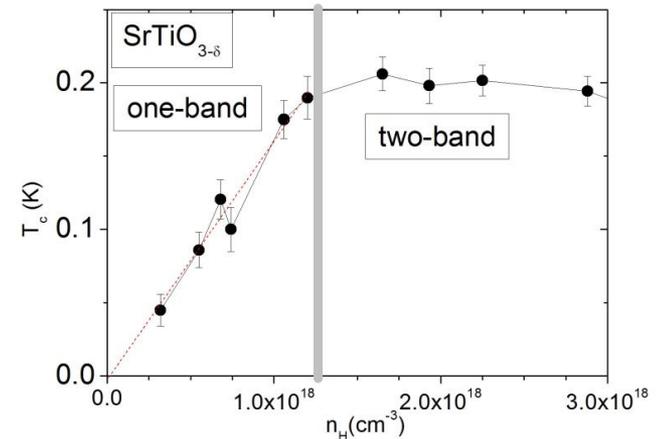
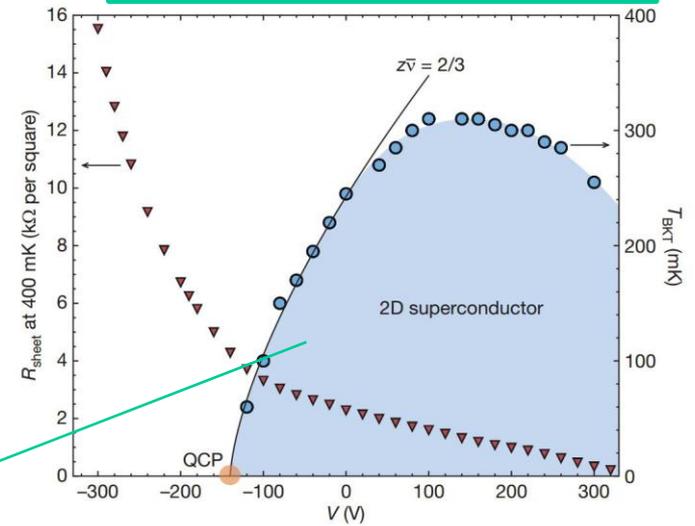
The three faces of the Fermi surface in a multi-domain sample.

Old and new phase diagrams

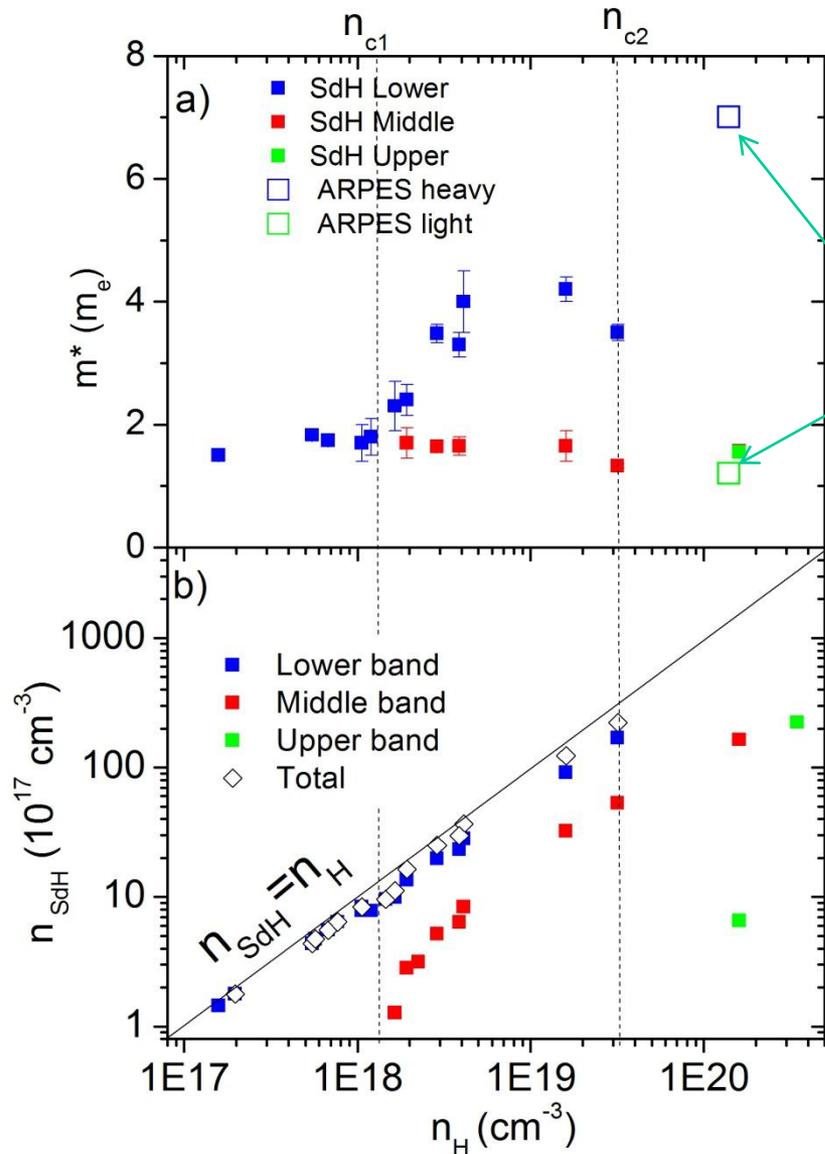
Lin *et al.* PRL in press (2014)



Cavaglia *et al.*, Nature (2008)



Evolution of cyclotron mass with doping

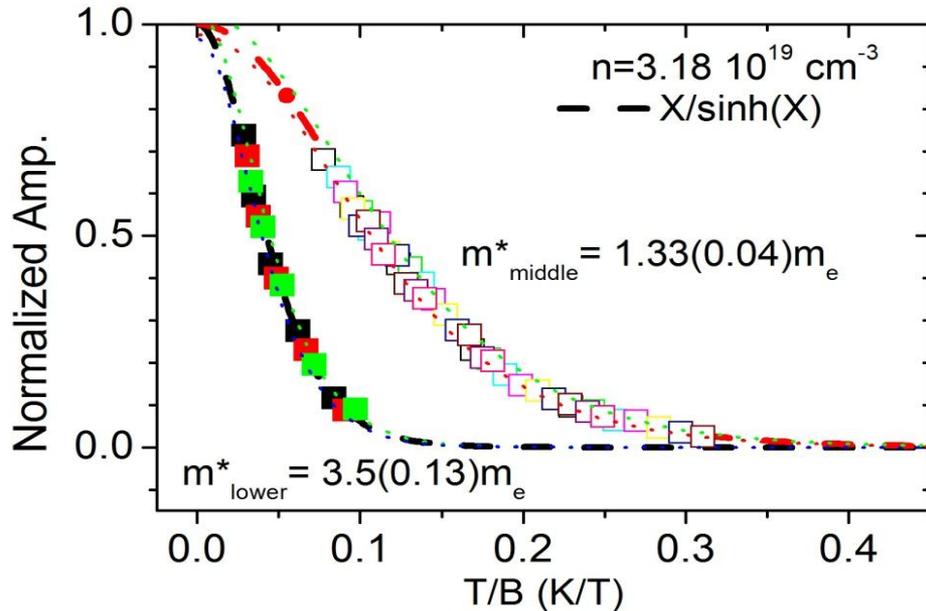


The effective mass in the lower band suddenly rises above n_{c2} !

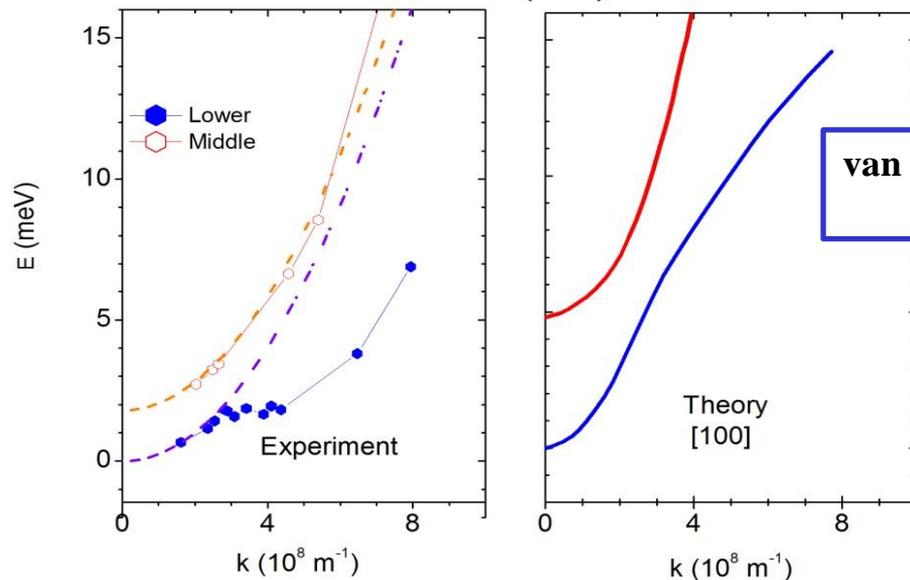
ARPES data

The number of carriers in each band!

Non-parabolic dispersion of the lower band



	Experiment	Ab initio Theory
$m^* (m_e)$	1.8	0.7-0.9
$n_{c1} (10^{17} \text{ cm}^{-3})$	12	6.8
Δ (meV)	2.2	5

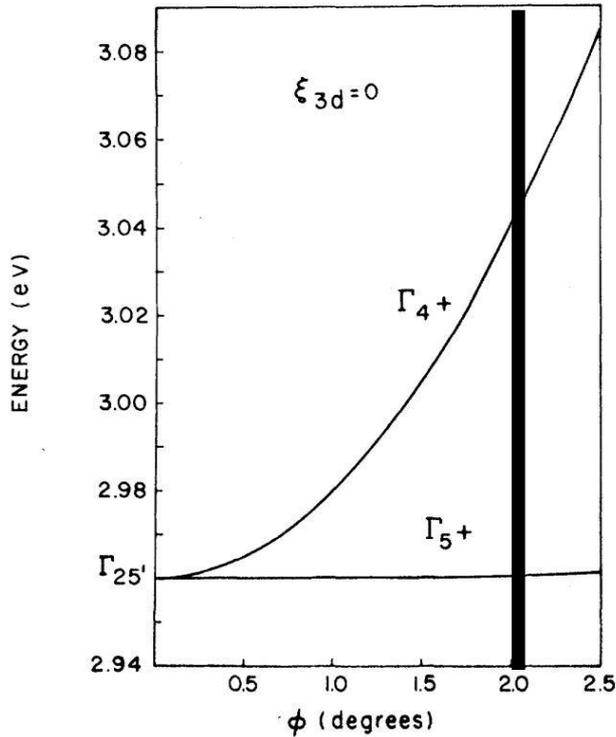


van der Marel, van Mechelen
& Mazin, (2011)

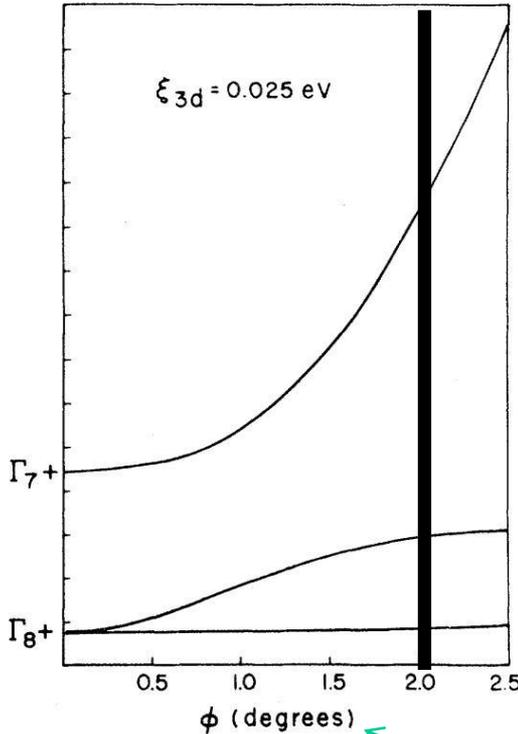
**Where does the mass
enhancement come from?**

Band hierarchy crucially depends on the sign of the crystal field parameter

Without spin-orbit



With spin-orbit



Matheiss PRB 1972

FIG. 3. Splitting of the SrTiO₃ conduction-band minimum as a function of the rotation angle ϕ with $\xi_{3d}=0$ and $\xi_{3d}=0.025$ eV.

Matheiss' crystal field parameters would make the middle band non-parabolic!

Tetragonal distortion

Summary

- When one oxygen out of 10^5 is missing in SrTiO_3 , it superconducts and has a sharp Fermi surface.
- The smallest Fermi surface to suffer a superconducting instability emerges in the context of an extremely long Bohr radius.
- Mechanism of superconductivity and symmetry of the order parameter remain open issues. Superconductivity is strong coupling at small wave-vector and small energy.

What is a metal?

“EVERYONE KNOWS WHAT A METAL IS AND CAN DESCRIBE MANY OF ITS CHARACTERISTICS.

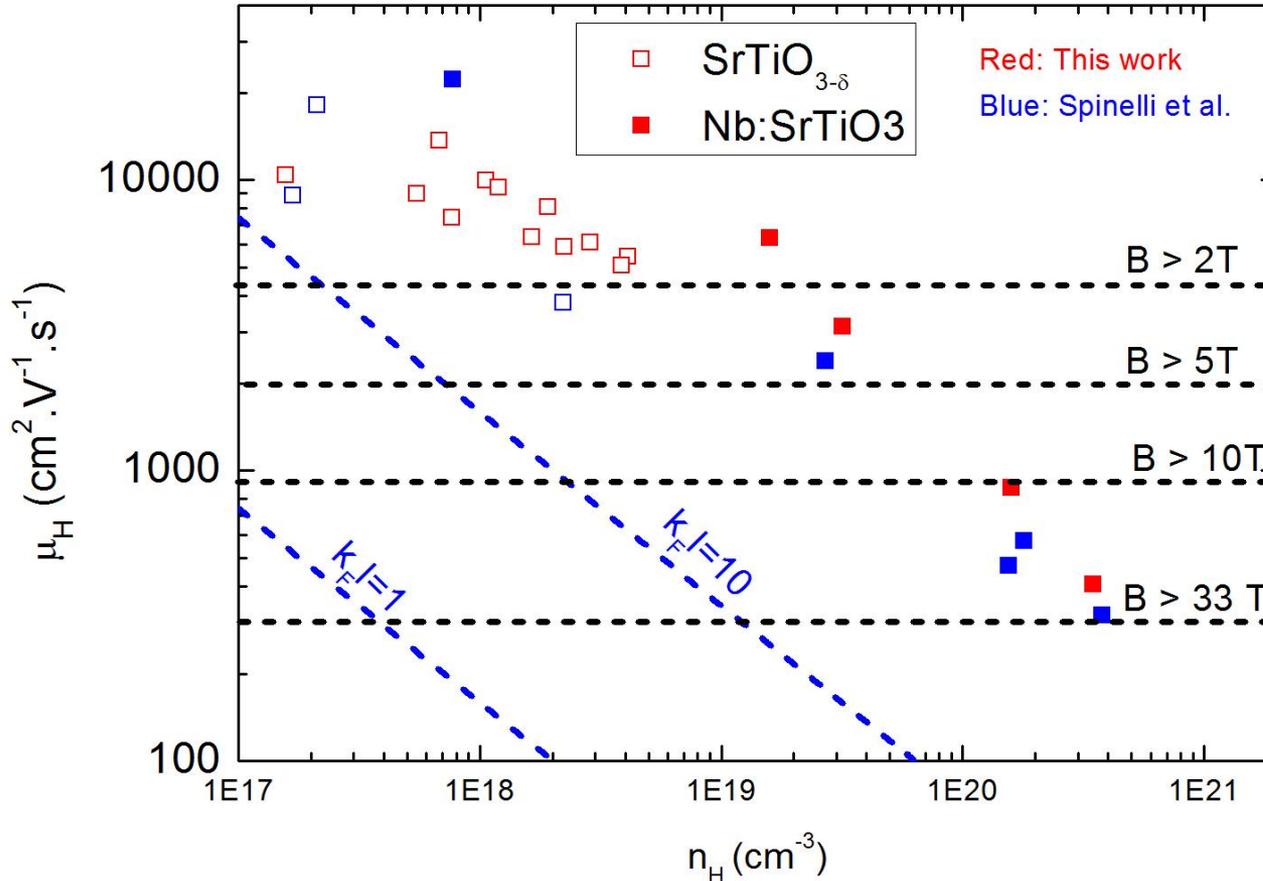
IT IS SAFE TO SAY, HOWEVER, THAT FEW PEOPLE WOULD DEFINE A METAL AS A ‘SOLID WITH A FERMI SURFACE’.

THIS MAY NEVERTHELESS BE THE MOST MEANINGFUL DEFINITION OF A METAL AND PROVIDES A PRECISE EXPLANATION OF THE MAIN PHYSICAL PROPERTIES ”

A. R. Mackintosh

Scientific American 1963

Consequences of high mobility



- Quantum oscillations visible at accessible magnetic fields
- Localisation is avoided at low concentration

Two-Band Superconductivity in Nb-Doped SrTiO₃

G. Binnig and A. Baratoff

IBM Zurich Research Laboratory, CH-8803 Rüschlikon, Switzerland

and

H. E. Hoenig

Institut für Physik, Universität Frankfurt, D-6000 Frankfurt, West Germany

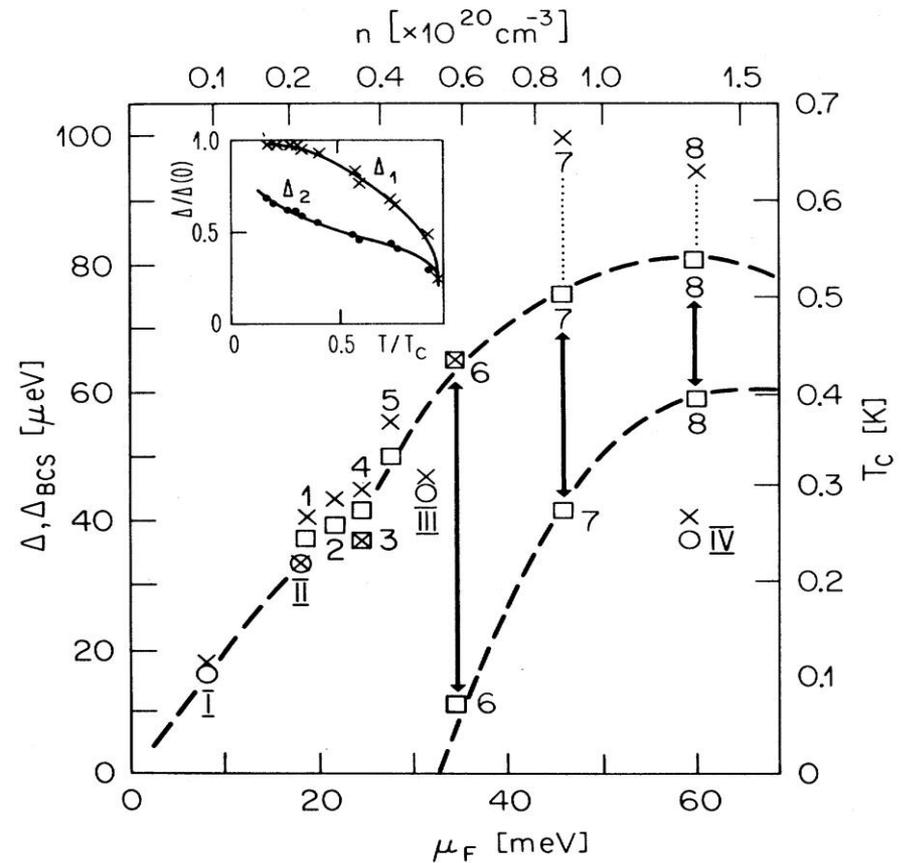
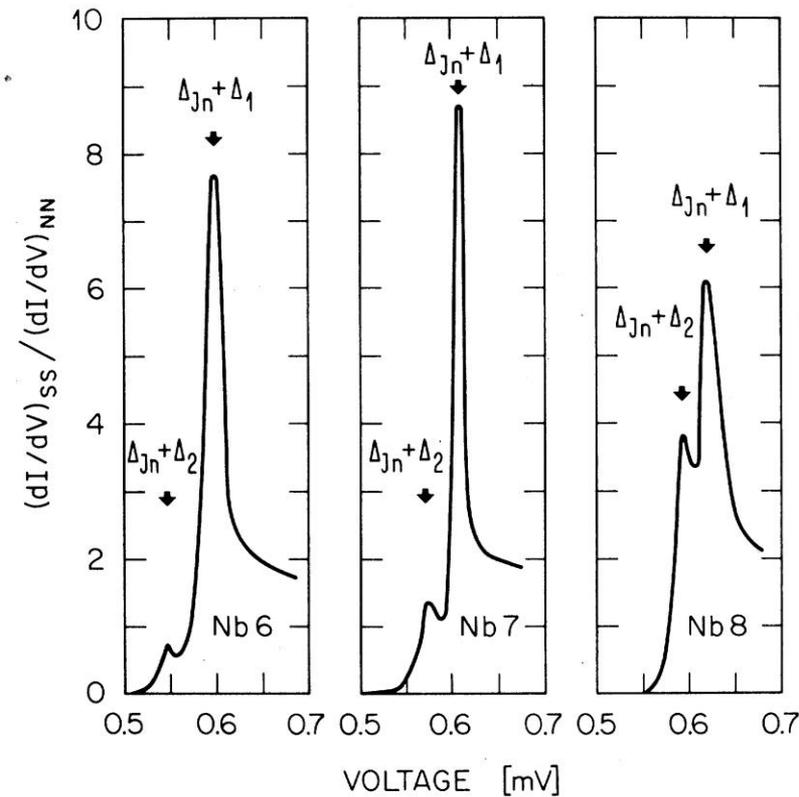
and

J. G. Bednorz

Eidgenössische Technische Hochschule, Hönggerberg, CH-8049 Zürich, Switzerland

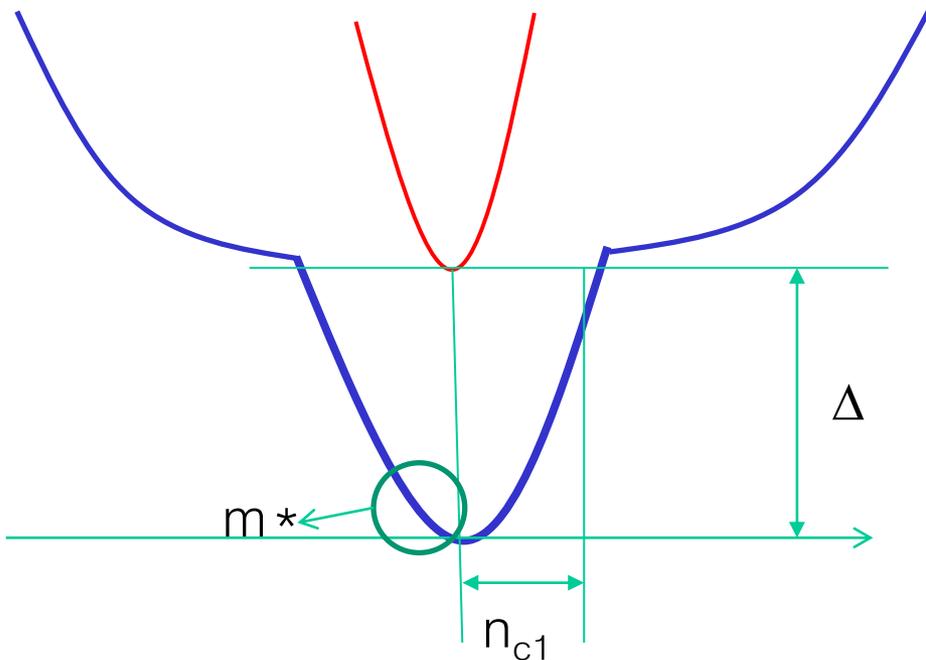
(Received 8 April 1980)

Two-band
superconductivity
seen by tunneling!



Theory and experiment

	Experiment	Ab initio Theory	References
m^* (m_e)	1.8	0.7-0.9	1, 2, 3
n_{c1} (10^{17}cm^{-3})	12	6.8	1
Δ (meV)	2.2	5	1



Theoretical references:

1. van der Marel, van Mechelen & Mazin, PRB (2011)
2. Janotti, Steiauf & Van de Walle, PRB (2011)
3. Shirai & Yamanaka, JAP

Where does the mass enhancement come from?

The $\text{Sr}_{1-x}\text{La}_x\text{TiO}_3$ system

Metal close to the band insulator

Okuda et al., 2001

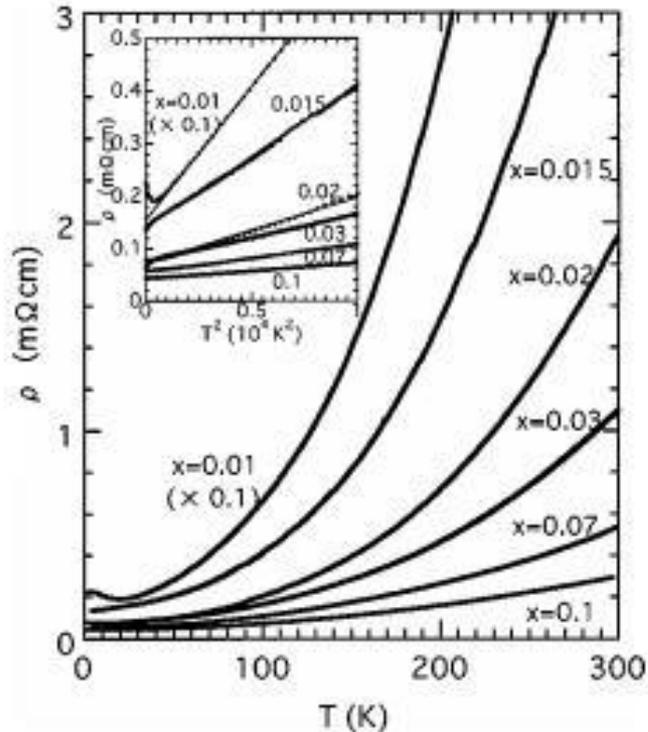
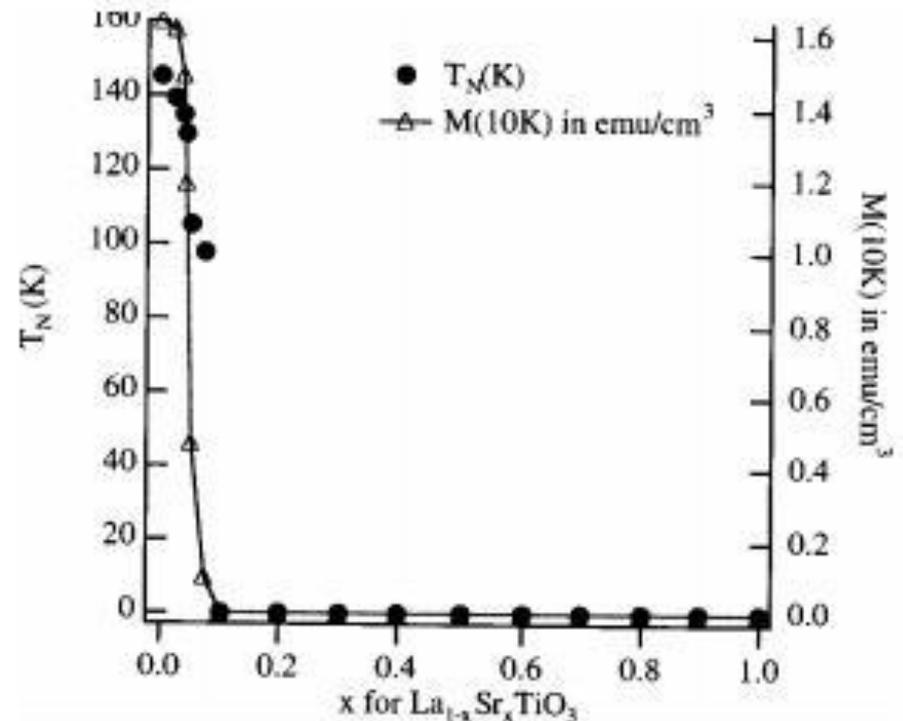


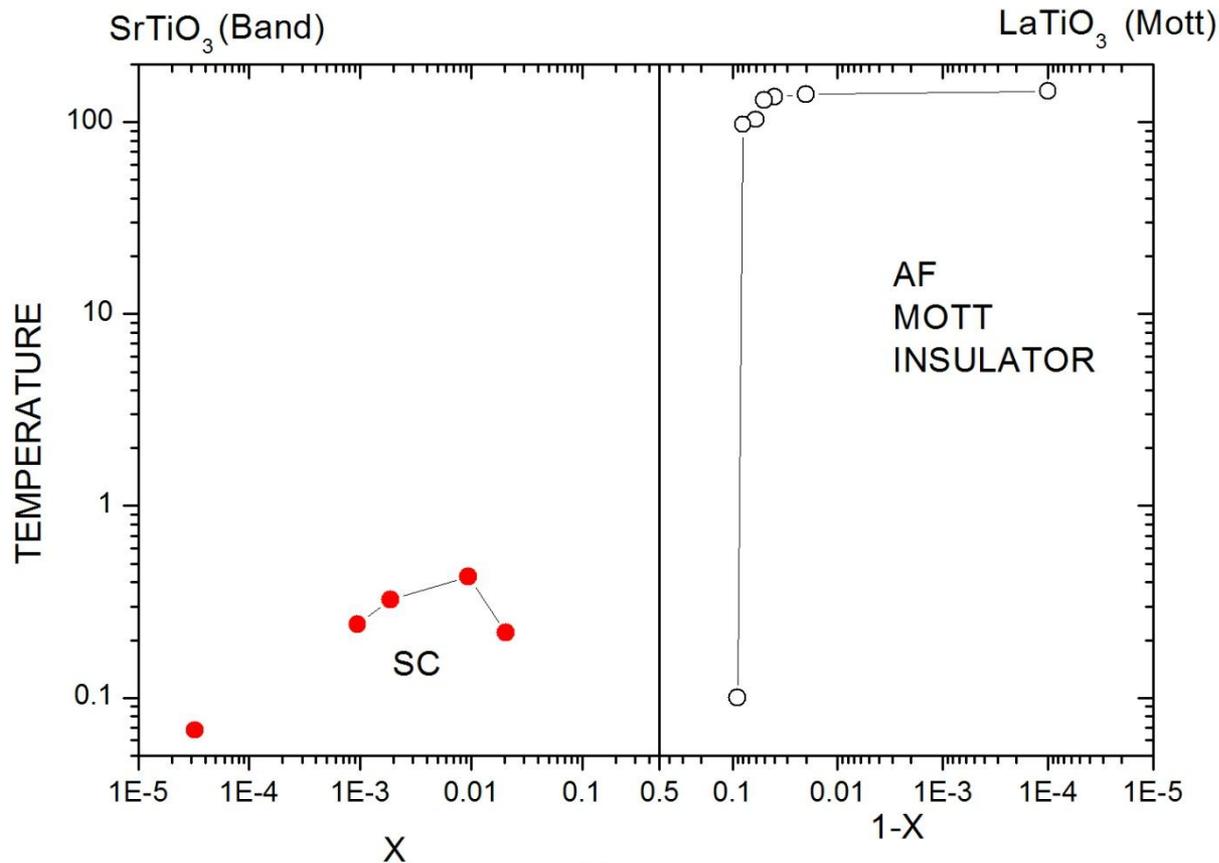
FIG. 1. Temperature (T) dependence of resistivity (ρ) for $\text{Sr}_{1-x}\text{La}_x\text{TiO}_3$ with various x values. Below 100 K, the resistivities for all compounds are almost proportional to T^2 . The inset shows a ρ vs T^2 plot below 100 K.

Robust AF close to the Mott insulator

Hayes et al., 1999



The $\text{Sr}_{1-x}\text{La}_x\text{TiO}_3$ system



The Fermi surface grows and then suddenly vanishes!