

## Electron transport : From nanoparticle arrays to single nanoparticles

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PbS, PbSe

LPEM - ESPCI

D. Portehault

C. Sanchez

$\text{Ti}_4\text{O}_7$

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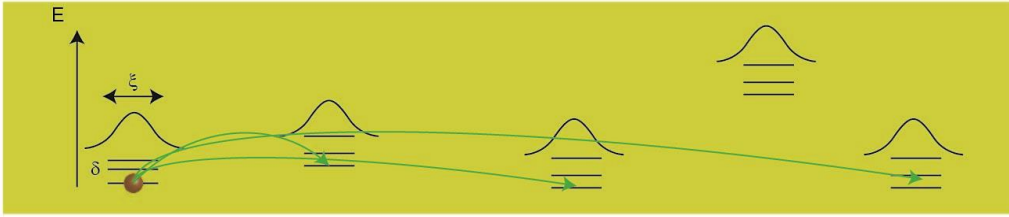
## Part I – Transport in nanoparticle arrays

- ▶ Electron transport in disordered systems
  - ▶ Doped semiconductors against granular metals
- ▶ Co-tunneling transport in gold nanoparticles arrays
  - ▶ Efros-Shklovskii and Middleton-Wingreen

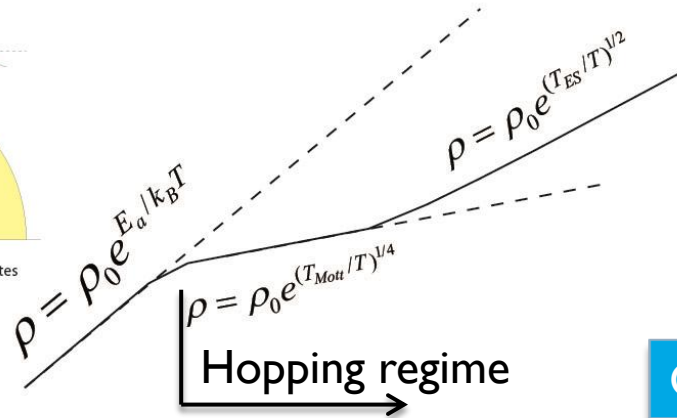
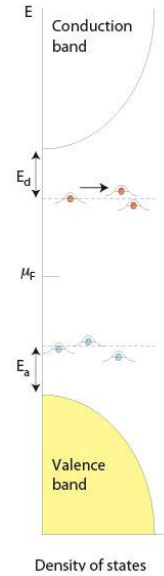
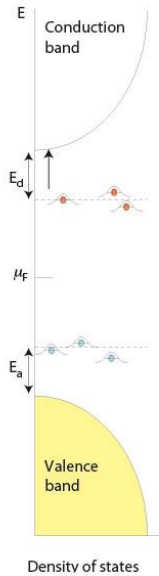
## Part II – Transport in single nanoparticle devices

- ▶ In-Vacuum projection of nanoparticles for on-chip tunneling spectroscopy
  - ▶ Verwey transition in single magnetite nanoparticles
-

# Variable Range Hopping in semiconductors



Log R



Hot

Cold

1/T

## VRH Laws

$$\sigma = \sigma_0 \exp - (T_0 / T)^\alpha$$

### Mott Law

Mean Level Spacing

$$T_{Mott} \propto \delta \propto \frac{1}{\xi^3}$$

$$\alpha = 1/4$$

### Efros-Shklovskii Law

Coulomb Energy

$$T_{ES} \propto \frac{e^2}{\xi}$$

$$\alpha = 1/2$$

# Efros-Shklovskii law in bulk semiconducting CdSe

Zhang, Y. et al. Probing the Coulomb Gap in Insulating n-Type CdSe.

*Physical Review Letters* **1990**, 64, 2687–2690.

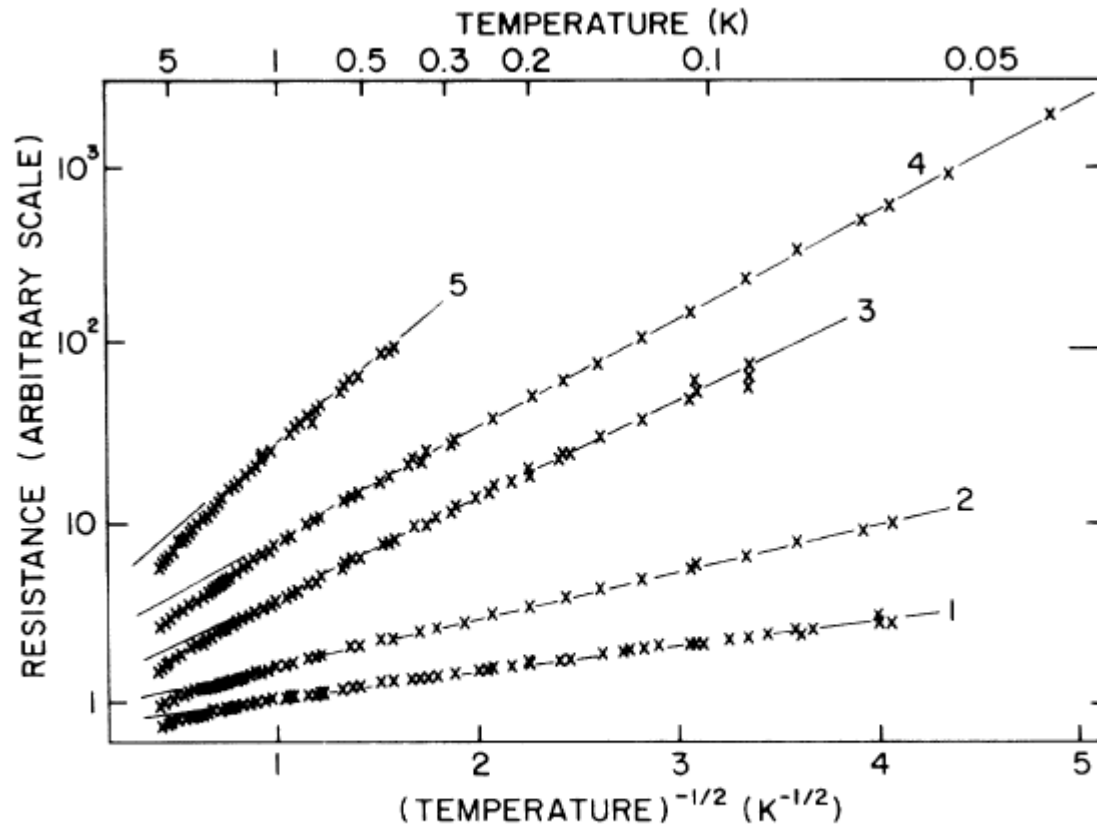
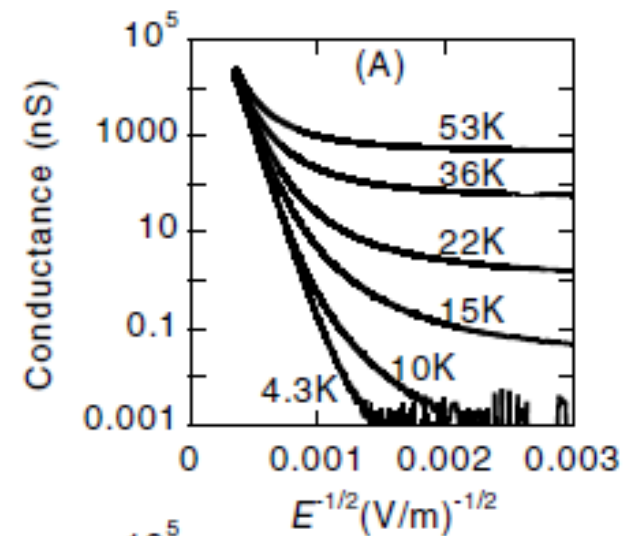
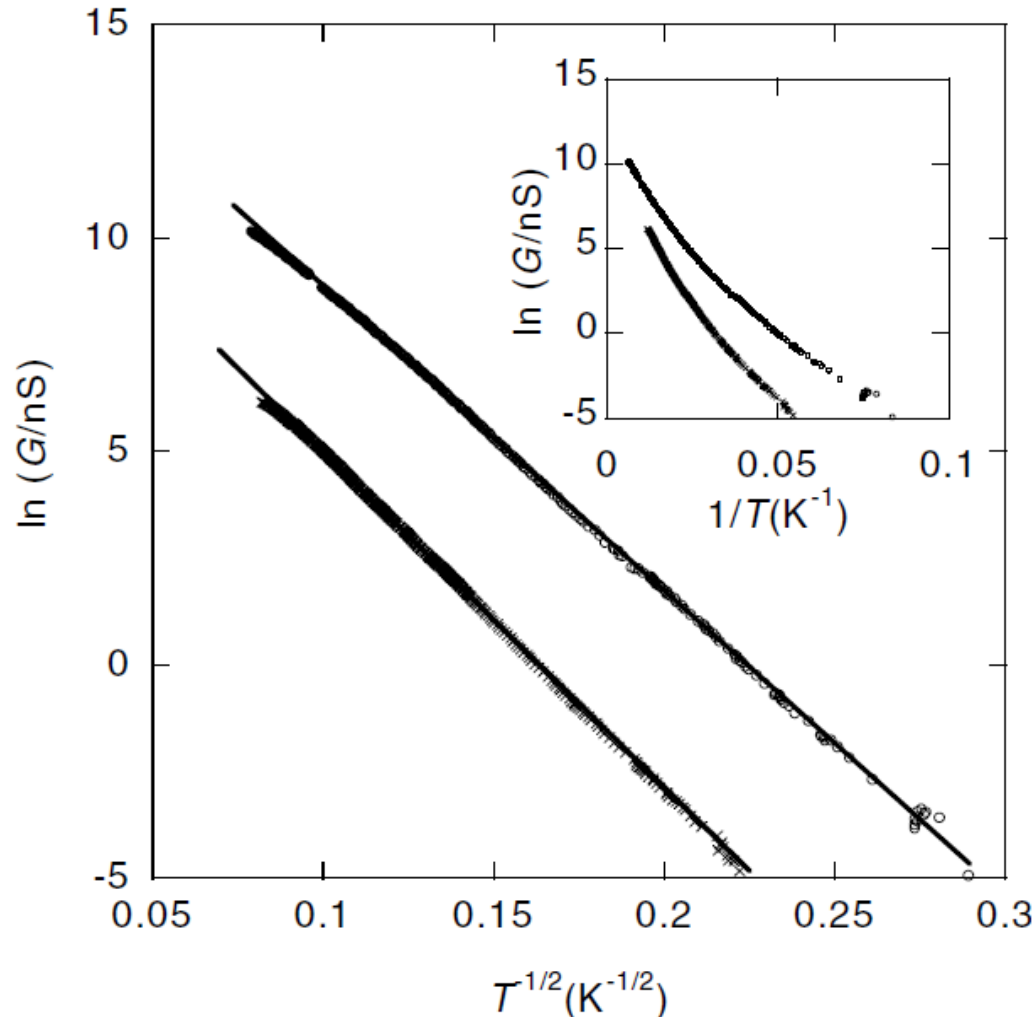


FIG. 2. Resistance of five insulating *n*-type CdSe samples plotted as a function of  $T^{-1/2}$  on a semilogarithmic scale.

# Efros-Shklovskii law in semiconducting CdSe nanoparticles films

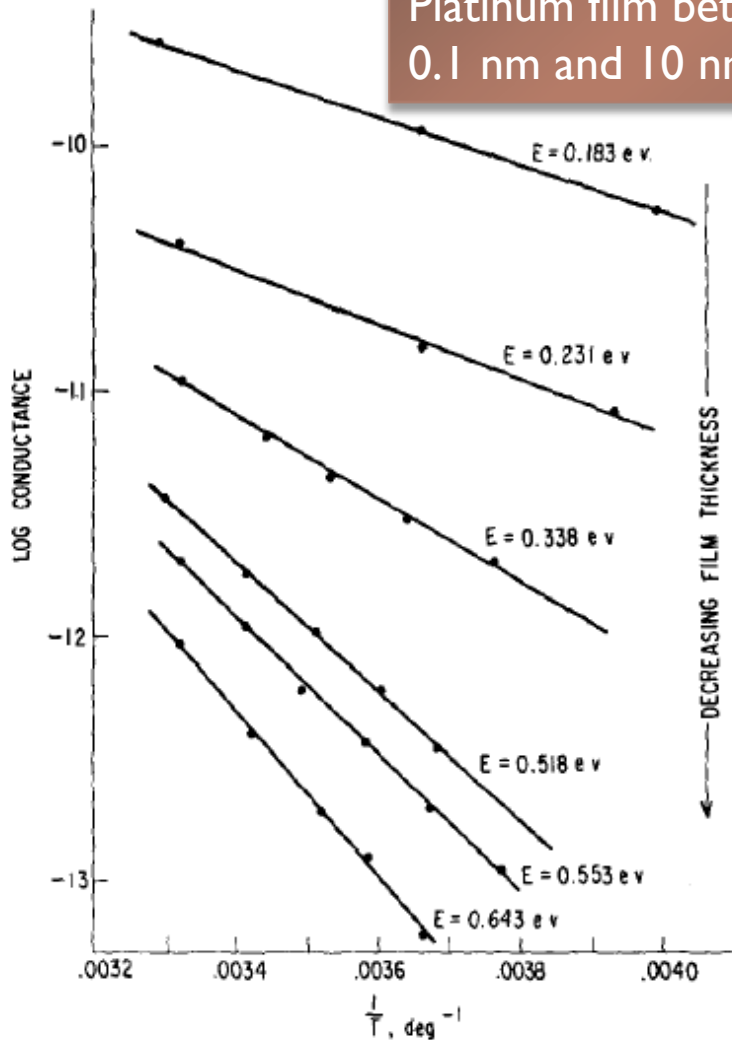
Yu, D. et al. Variable Range Hopping Conduction in Semiconductor Nanocrystal Solids. *Physical Review Letters* 2004, 92, 216802.



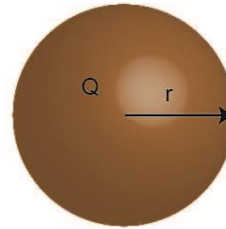
# Evaporated metal thin films

Platinum film between  
0.1 nm and 10 nm thick

I. Neugebauer et al. *JAP* **33**, 74 (1962).



Coulomb energy



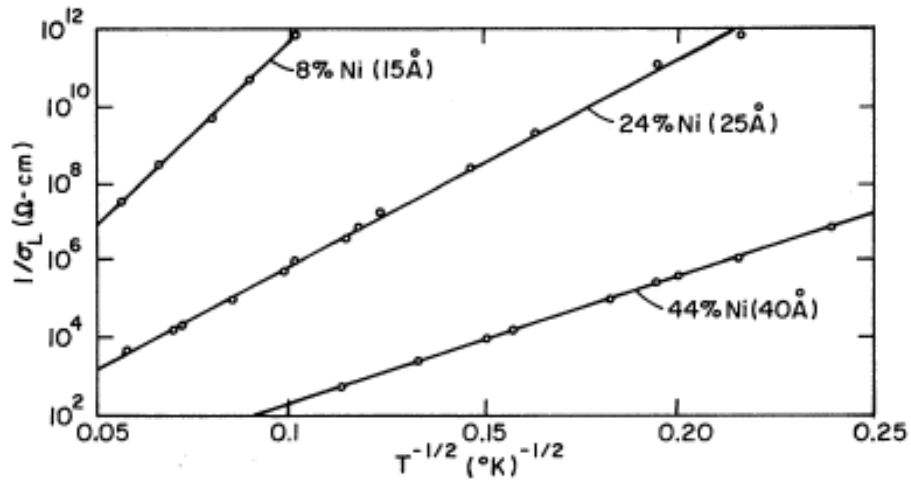
$$\phi(r) = \frac{Q}{4\pi\epsilon\epsilon_0 r}$$

$$C_{self} = Q = 4\pi\epsilon\epsilon_0 r$$

$$E_C = \frac{e\phi}{2} = \frac{e^2}{2 \times 4\pi\epsilon\epsilon_0 r} = \frac{e^2}{2C_{self}}$$

FIG. 8. Log conductance vs reciprocal temperature for platinum films of different thicknesses.

# Efros-Shklovskii law in disordered metal thin films !!!



I. Sheng, P. Abeles, Ni films  
*Physical Review Letters* **31**, 44-47 (1973).

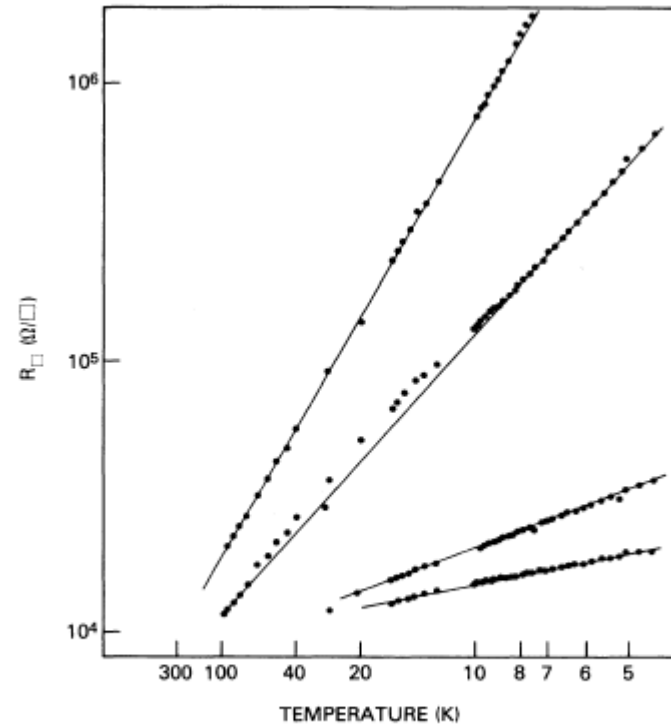


FIG. 4. The logarithm of the sheet resistance as a function of  $1/\sqrt{T}$  for a variety of the nonsuperconducting samples. The lines are guides to the eye.

$$\sigma = \sigma_0 \exp(-(T_0 / T)^{1/2})$$

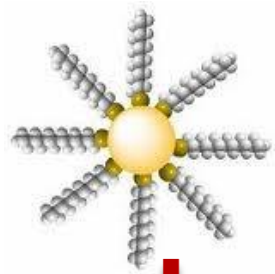
Simon, R. et al. granular niobium nitride cermet films  
*Physical Review B* **36**, 1962-1968 (1987).



# Electron transport in metallic nanocrystals arrays - sample preparation

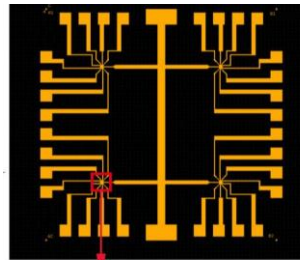
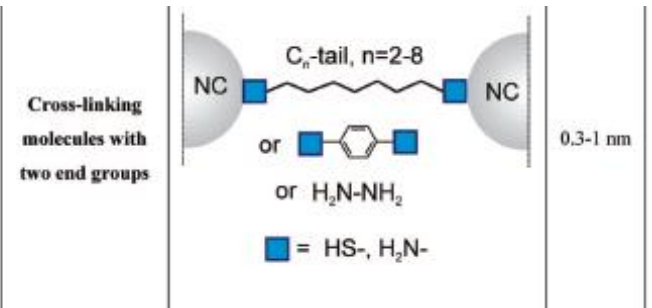
## Synthesis

- Brust method (1992)
- Revisited by Klabunde (1998)

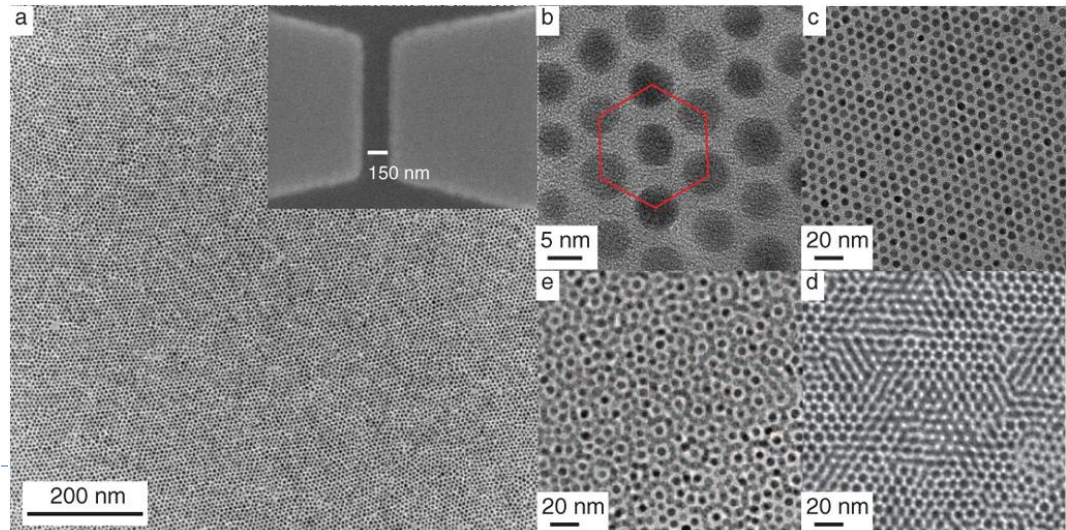
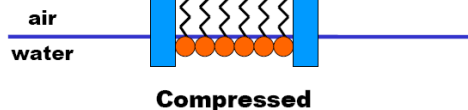
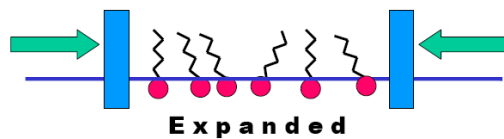


$\varnothing \sim 5\text{nm}$

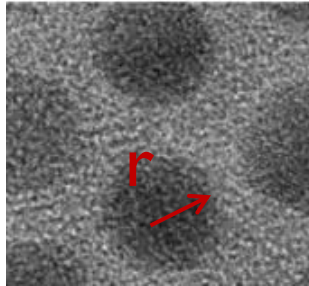
Arrays crosslinked by  
alcane dithiol molecules



Arrays formed by the  
Langmuir method



# Electron transport in nanocrystals arrays (as function of temperature)



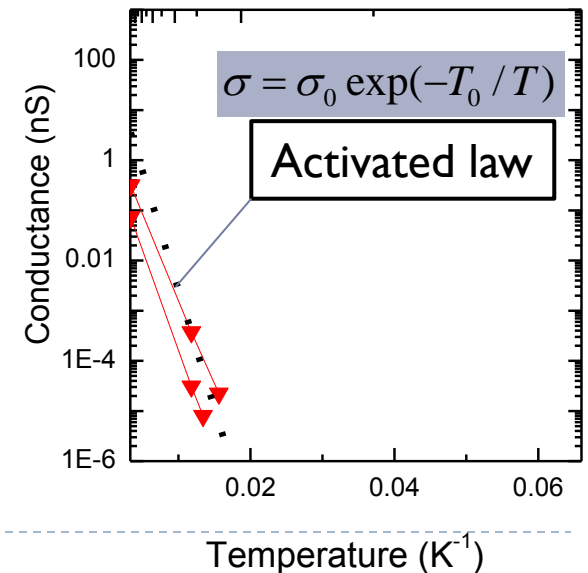
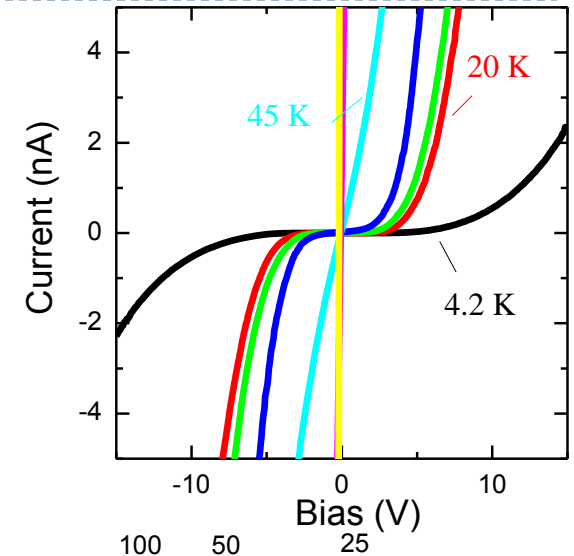
$$C_{self} = Q = 4\pi\epsilon\epsilon_0 r$$

Coulomb energy

$$E_C = \frac{e^2}{2C_{self}} = k_B T_0 = e^2 / 4\pi\epsilon\epsilon_0 r$$

$$\approx 1100K$$

$$(r \approx 2.5nm, \epsilon \approx 3)$$



# Efros-Shklovskii law in nanocrystals arrays (as function of temperature)

- At larger quantum tunnel coupling, and low temperature, the conductance follows the variable range hopping law of Efros-Shklovskii.

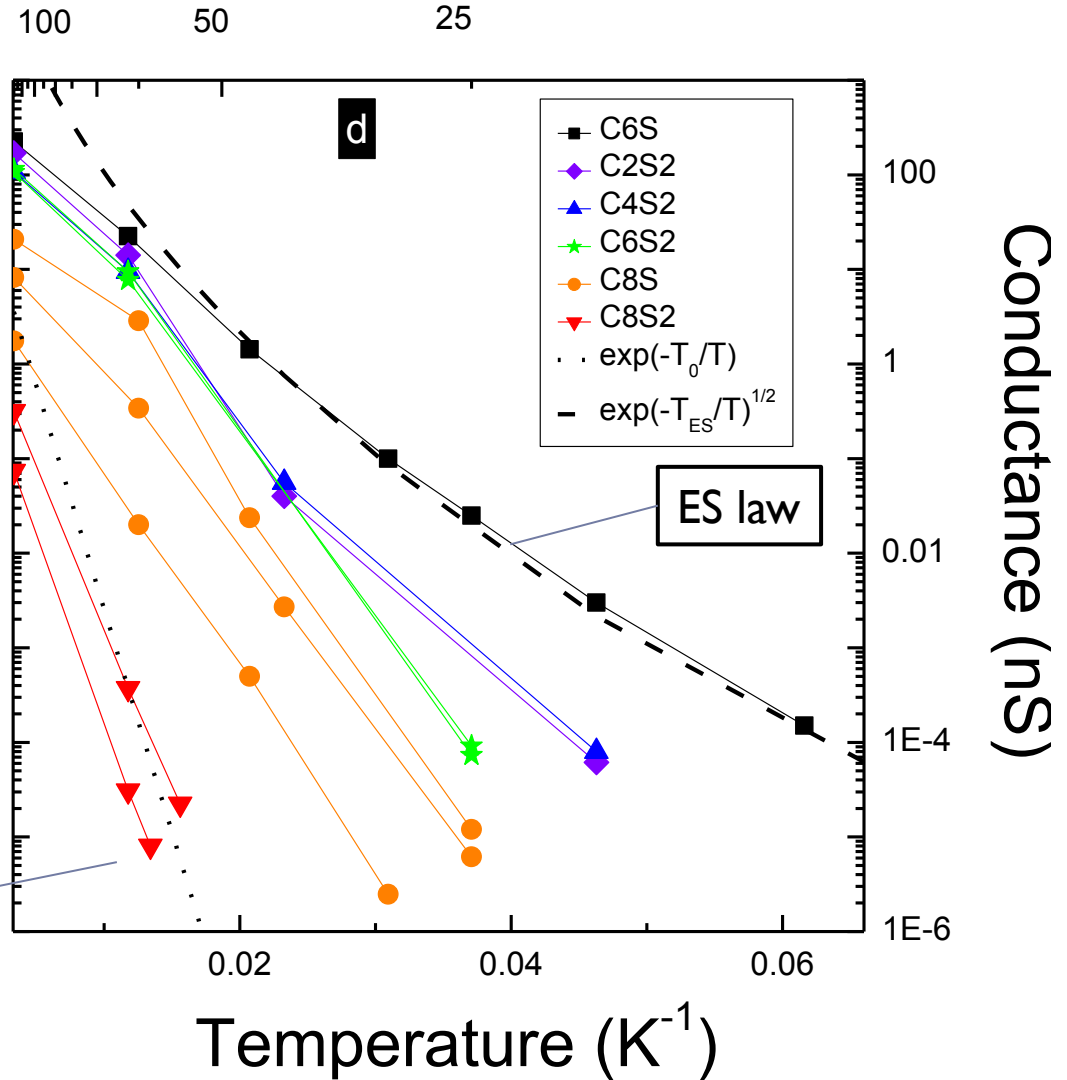
$$\sigma = \sigma_0 \exp(-T_{ES} / T)^{1/2}$$

$$T_{ES} \approx 8000 K$$

$$T_{ES} = e^2 / (4\pi\epsilon\epsilon_0 \langle \xi \rangle k_B) \simeq 8000 K$$

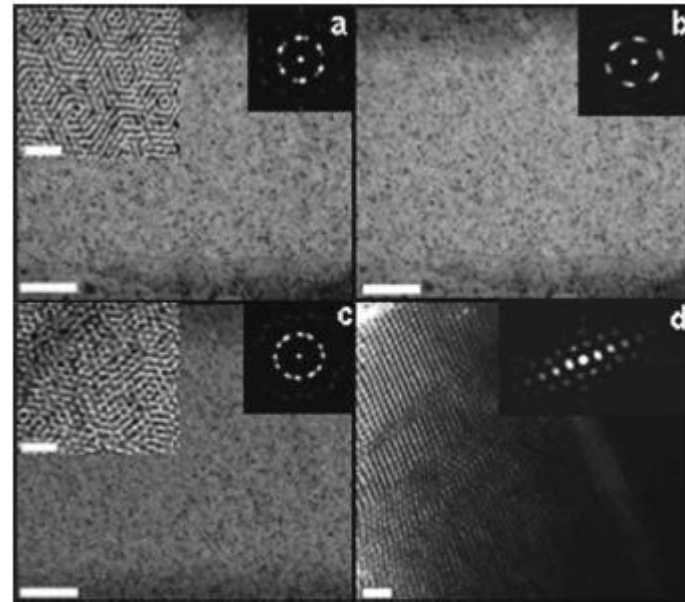
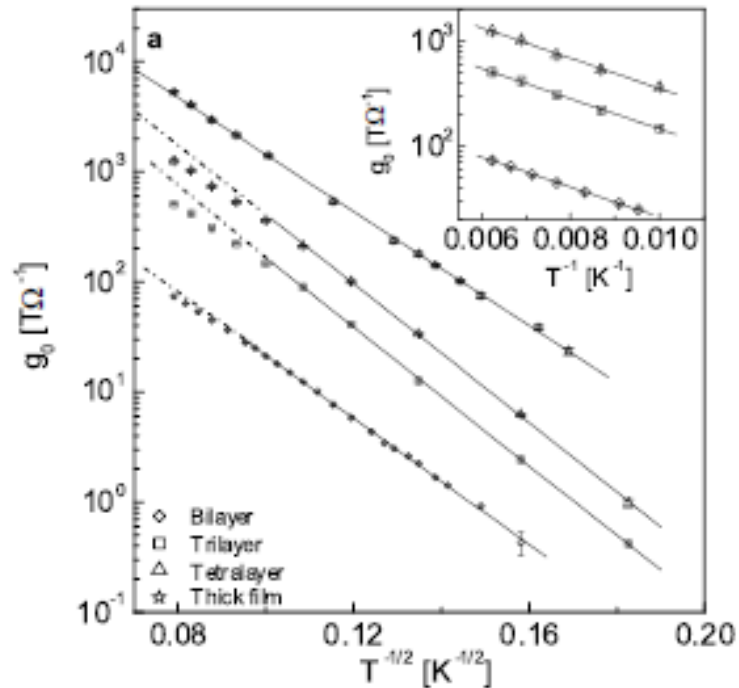
$$\xi = \frac{2r}{\ln [E_C^2 / 16\pi(k_B T)^2 g]}$$

Activated law



# Efros-Shklovskii law in nanocrystals array

H. Jaeger's group (Chicago)



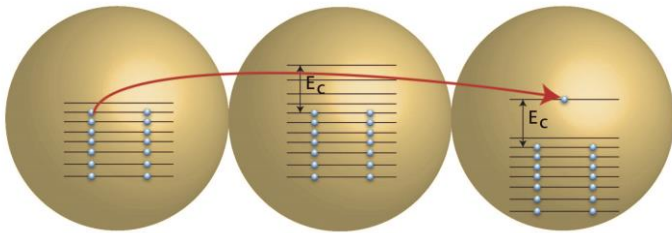
I. Tran, T.B. et al. *Physical Review Letters*  
95, 076806 (2005).

# Why is Efros-Shklovskii law in granular metallic systems surprising ?

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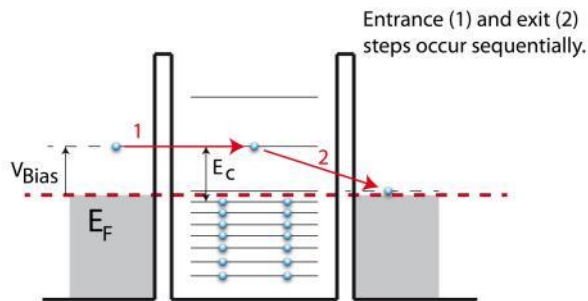
- ▶ In semiconductors, direct long distance tunneling is possible



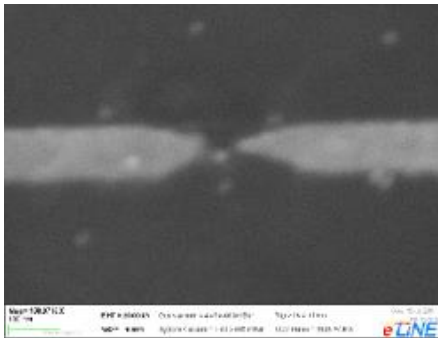
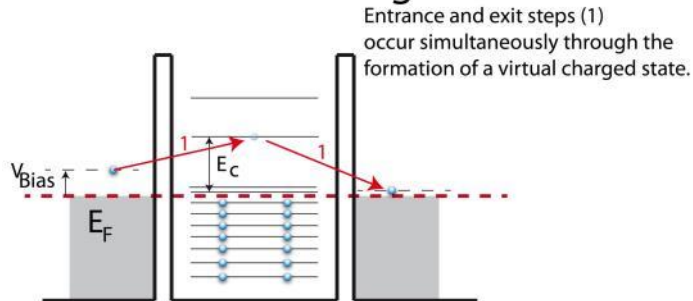
- ▶ Long distance tunneling between metallic grains is not possible
-

# « co-tunneling »

## Sequential tunneling



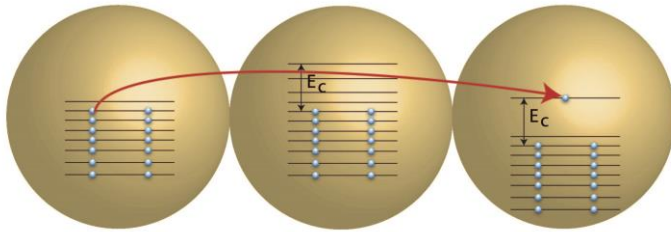
## Co-tunneling



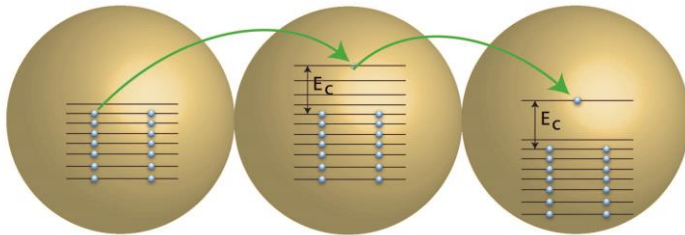
- ▶ At low temperature, electron transport is blocked because of the large Coulomb energy  $E_C = e^2/2C$
- ▶ As tunnel coupling between the nanocrystal and the electrodes becomes large, electron tunneling through virtual charged states become possible. This is cotunneling.

# Efros-Shklovskii law in granular metals explained by « co-tunneling »

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- ▶ Single long distance tunneling is not possible



- ▶ Simultaneous multiple short distance tunneling events is possible

- ▶ [1] Jingshan Zhang and Boris I. Shklovskii, *Physical Review B* **70**, 115317 (2004)
  - ▶ [2] M.V. Feigel'man and A.S. Ioselevich, *Jetp Letters* **81**, 277 (2005)
  - ▶ [3] I. Beloborodov, A. Lopatin, and V. Vinokur, *Physical Review B* **72**, 125121 (2005).
  - ▶ [4] I. S. Beloborodov, A. V. Lopatin, V. M. Vinokur, and K. B. Efetov, *Reviews of Modern Physics* **79**, 469-518 (2007).
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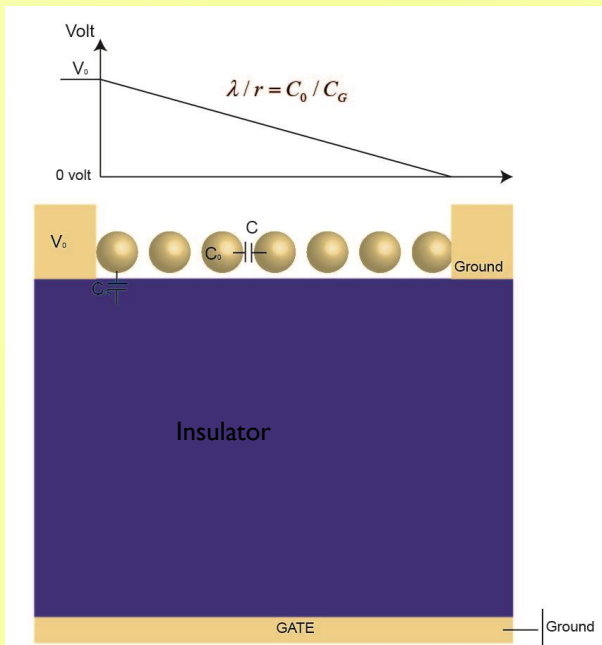


# Electron transport in nanocrystals arrays (as function of electric field)

## Long Screening length

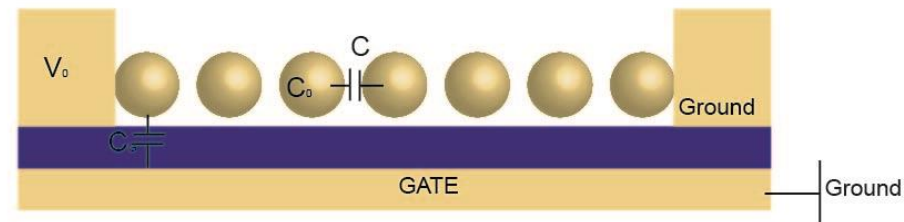
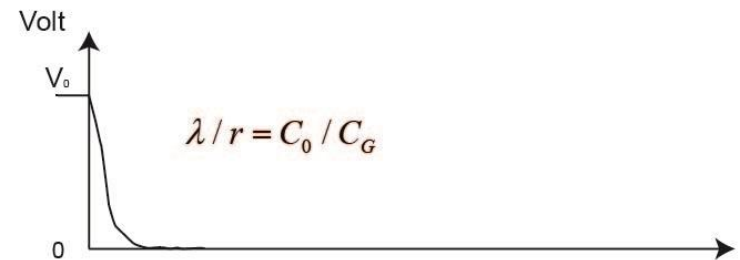
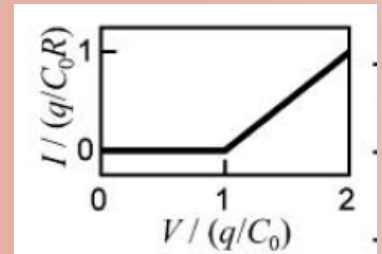
$$I = I_0 \exp(- (E_{Coulomb} / k_B T)^\alpha)$$

$$I = I_0 \exp(- (E_{Coulomb} / eV)^\alpha)$$



## Short Screening length → Middleton-Wingreen

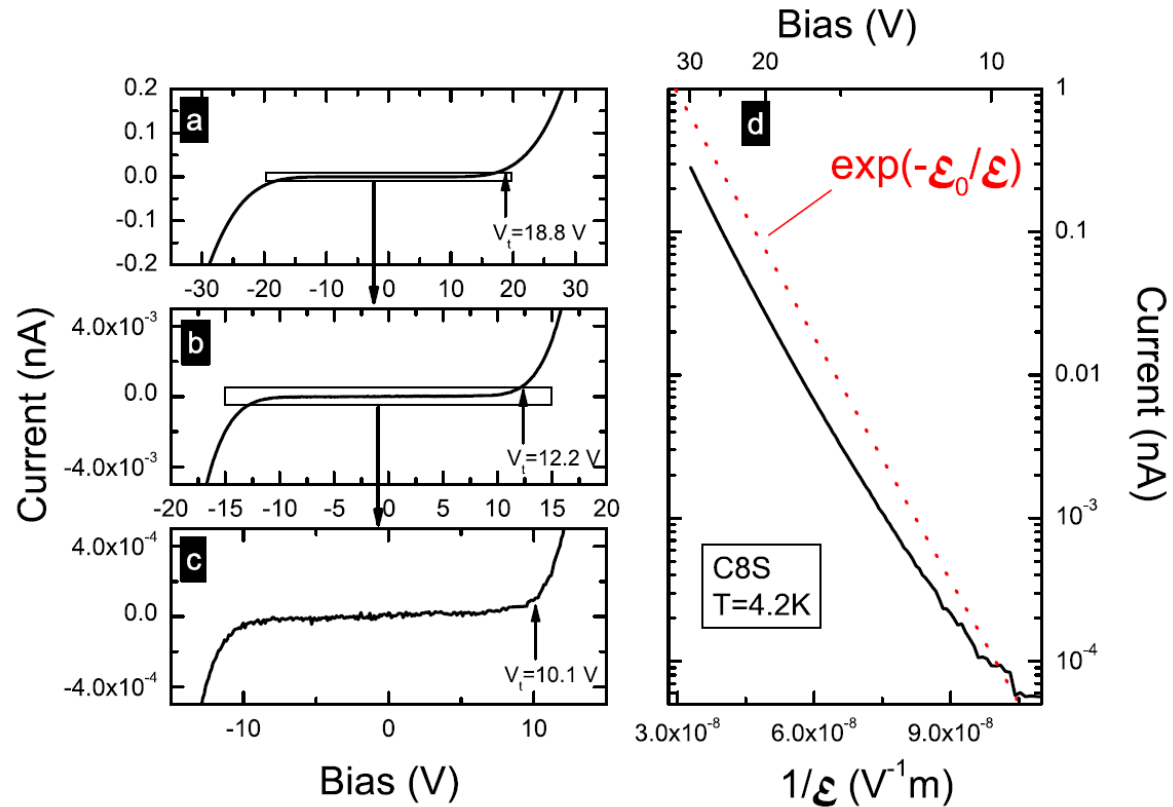
$$I \propto (V - V_T)^\alpha$$





# In our arrays, Long Screening length model applies

- ▶ Weak capacitive coupling with the gate
- ▶ Short distance between electrodes  $\sim 150$  nm
- ▶ Threshold voltage is not relevant



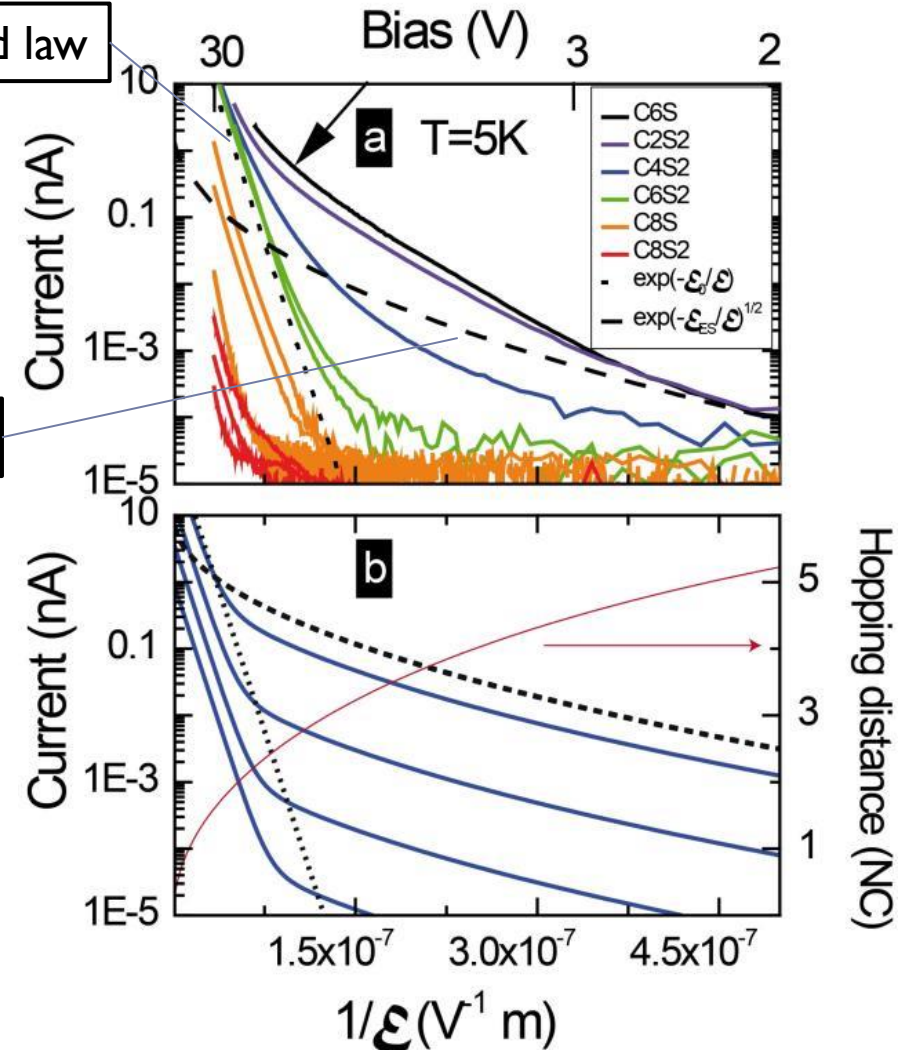
# Electron transport in nanocrystals arrays (as function of electric field)

- ▶ For weakly conducting NC arrays, i.e. small tunnel barrier transparency, the  $I(V)$  curve follows an activated law, dotted line.

Activated law

- ▶ For better conducting arrays, i.e. for larger tunnel barrier transparency, the  $I(V)$  curve follows an ES-type law, dashed line

ES law



H. Moreira et al. *Physical Review Letters*  
107, 176803(2011)

# Toward single nanoparticle spectroscopy

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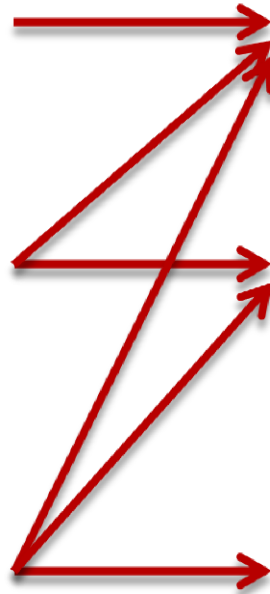
## Bulk transitions

## Spectral characteristics of single nanoparticles

▶ Anderson Localization

▶ Mott Localization

▶ Superconductor-Insulator  
Transition



▶ Thouless energy

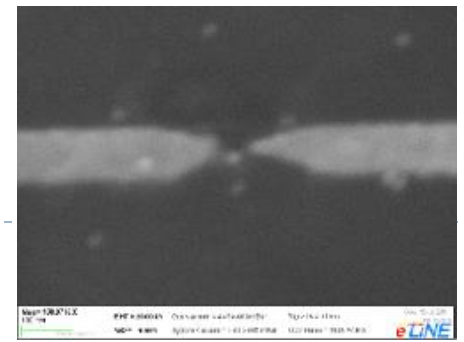
▶ Coulomb energy

▶ Superconducting gap

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# Nanoparticles Trapping

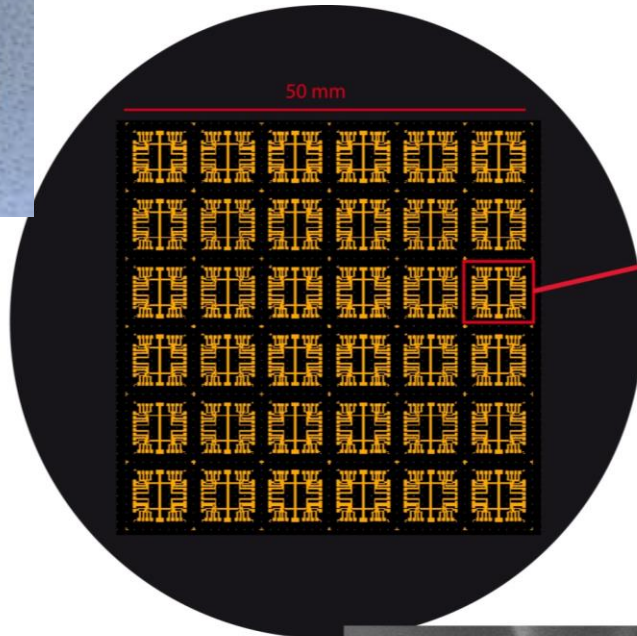
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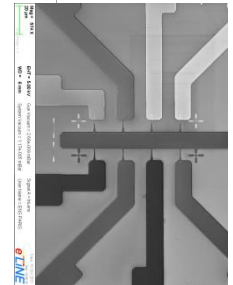
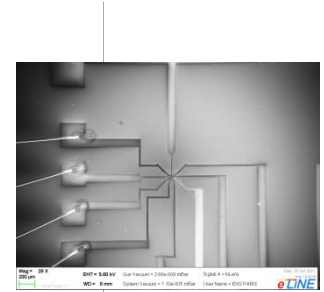
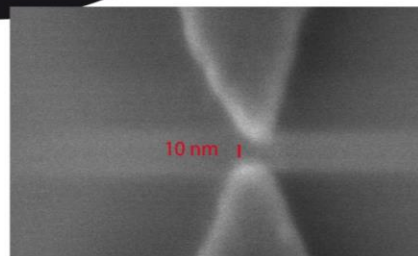
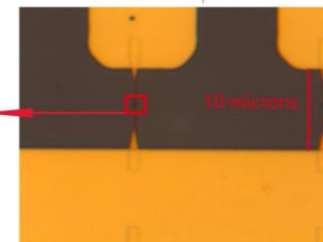
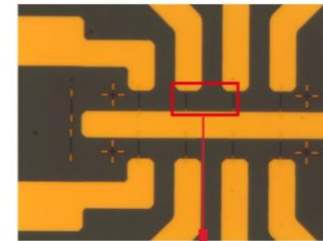
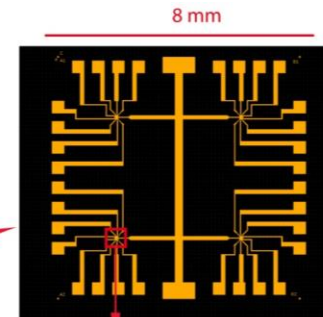
## ▶ Goal

- ▶ Trapping a single nanoparticle within the nanogap, (with no parasitic current path)
  - ▶ The success rate should be high enough so that the technique can be applied to many different chemically synthesized nanoparticles
  - ▶ Can be done in inert atmosphere (argon)
- 
- ▶ Method 1 : Electrostatic or molecular assembly in solution
  - ▶ Method 2 : Method 1+ Dielectrophoretic Force
  - ▶ Method 3 : nanolithography + one of the other method
    - avoid methods in solution, because of the impossibility of checking tunnel current during assembly
- 
- ▶ Method 4 : High vacuum projection of nanoparticles
-

# Wafer de nanogaps (LPN – Microfab facility)

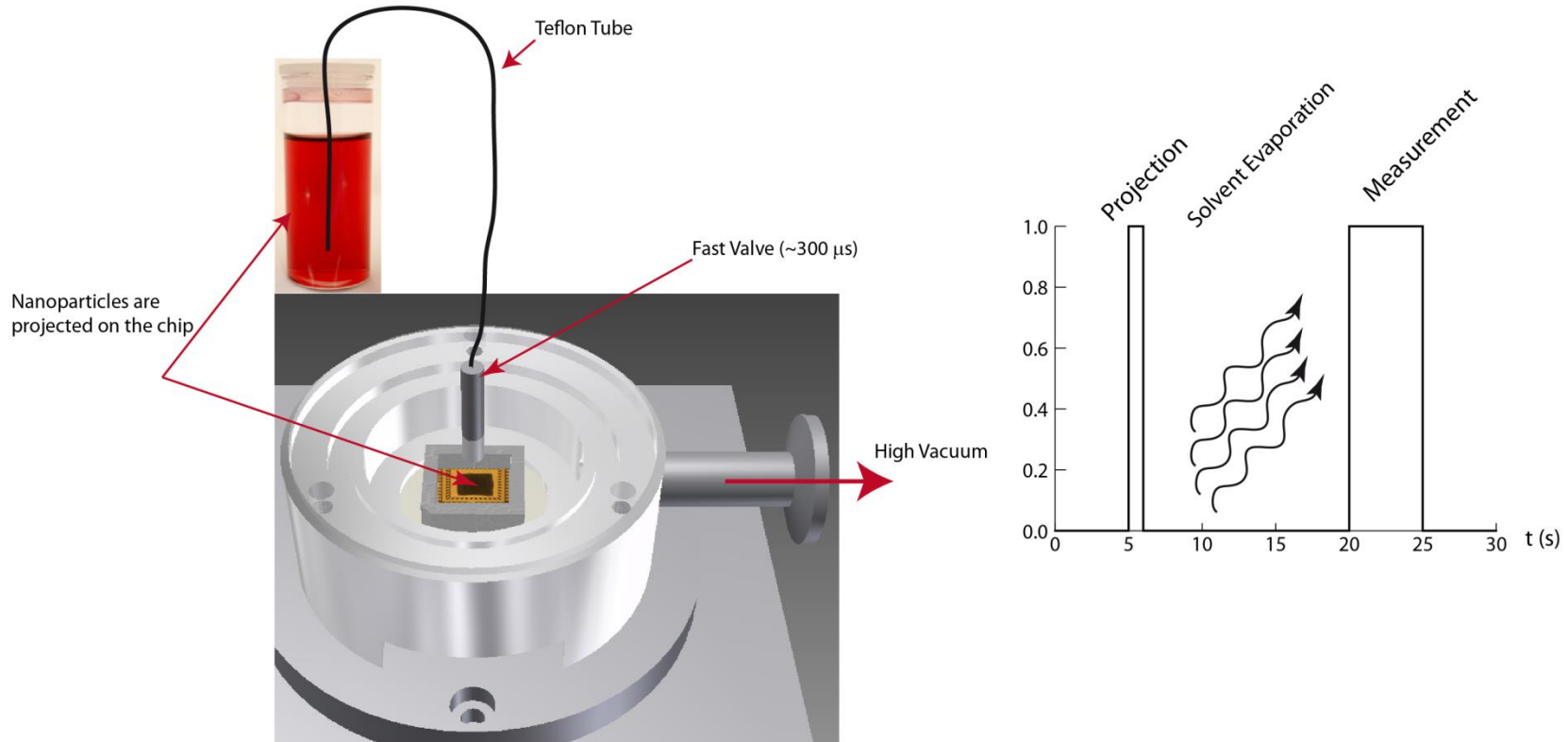


36 chips \* 32  
= 1152 nanogaps



# Method 4: In-vacuum projection of nanoparticles

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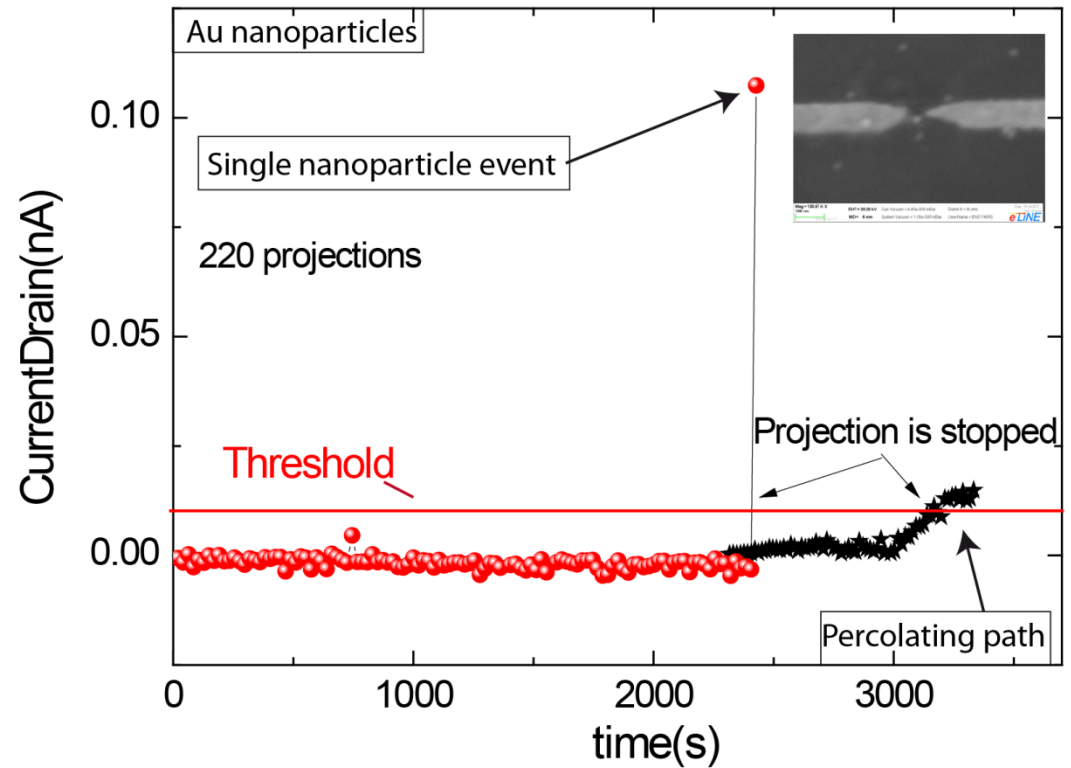


High vacuum chamber used for the projection of nanoparticles on the chip, using a fast pulsed valve (response time  $\sim 1 \text{ ms}$ ).

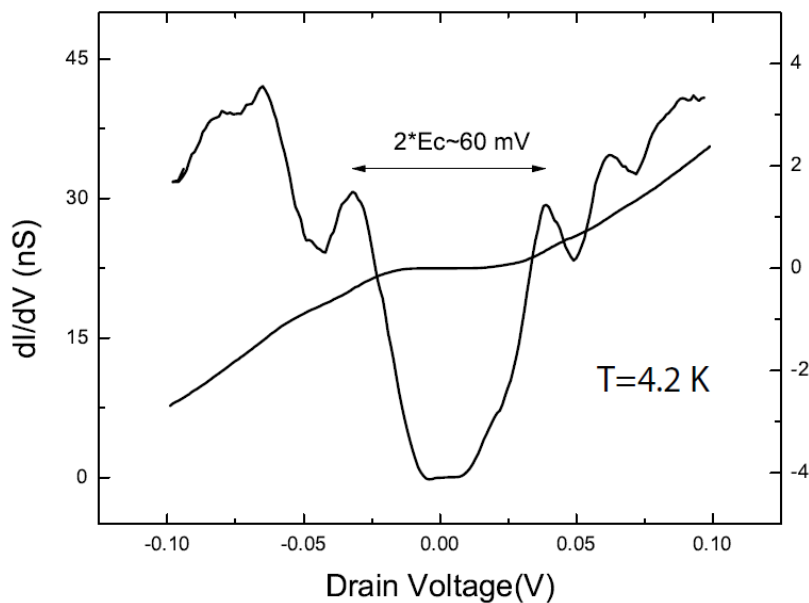
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# Projection curve

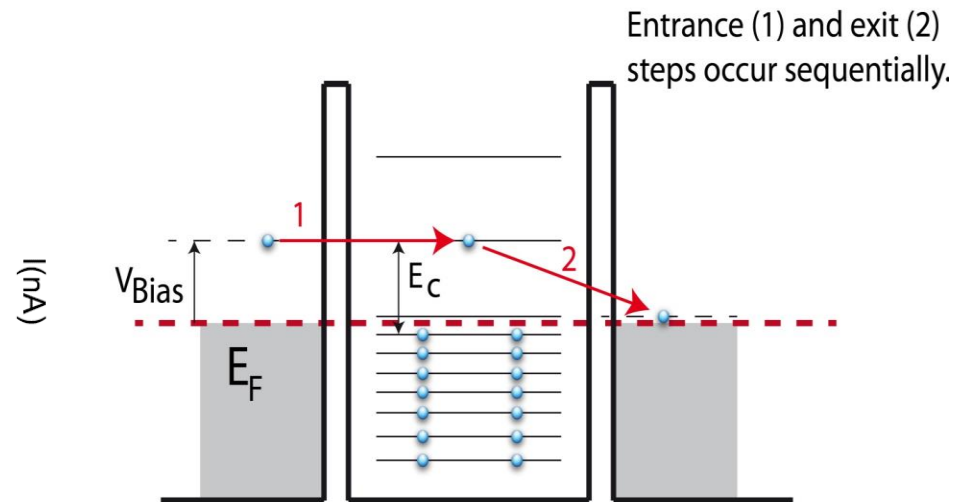
- opening of the valve < 1 ms
- bias voltage = 0.1 V
- Current measured 10s after the projection
- Threshold=0.01 nA



# Single gold nanoparticle trapped within the nanogap $\rightarrow$ signatures of Coulomb blockade

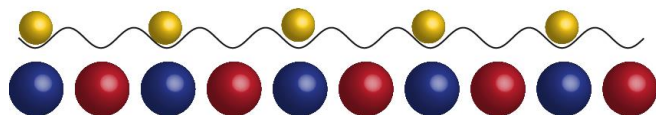
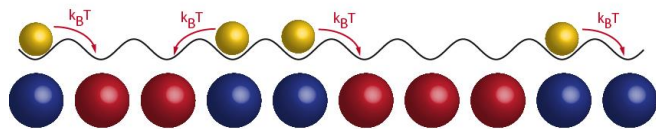
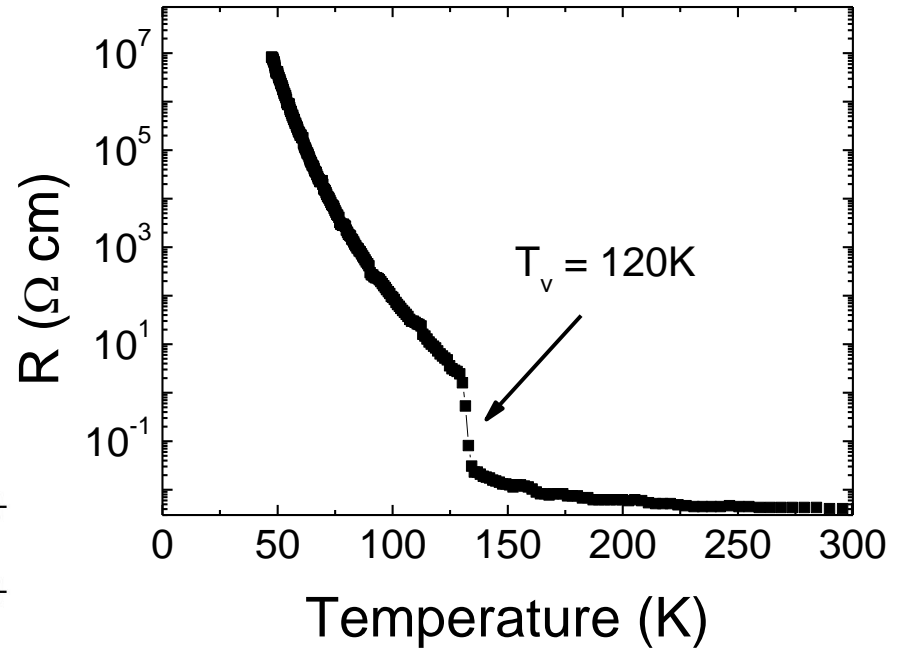
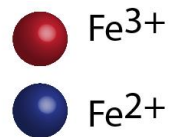
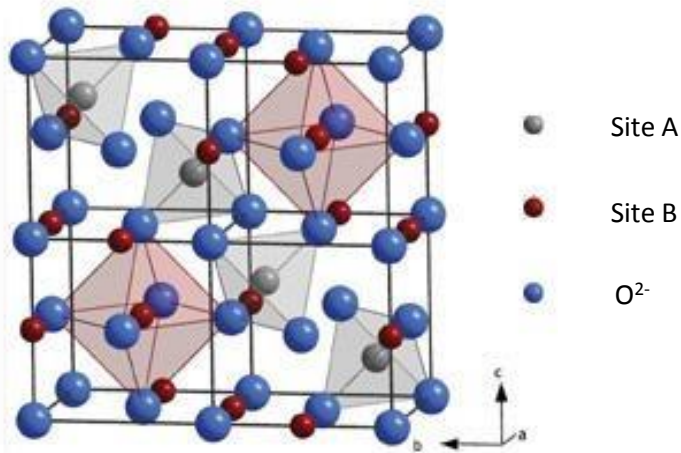


Yu, Q et al. *ACS nano* 2013, 7, 1487–94.



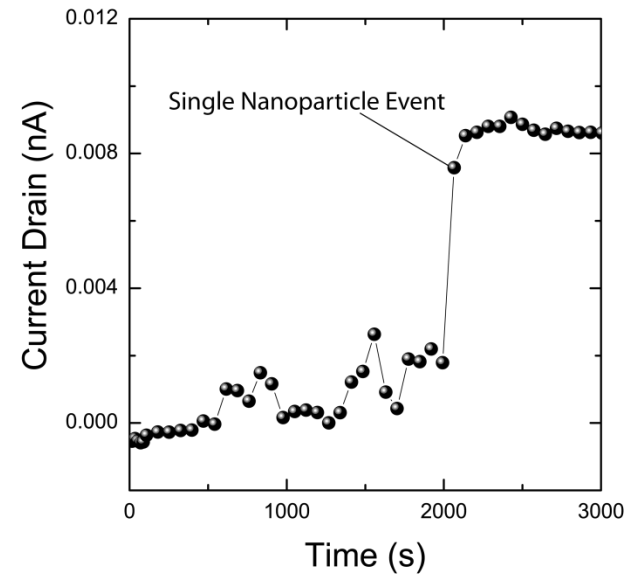
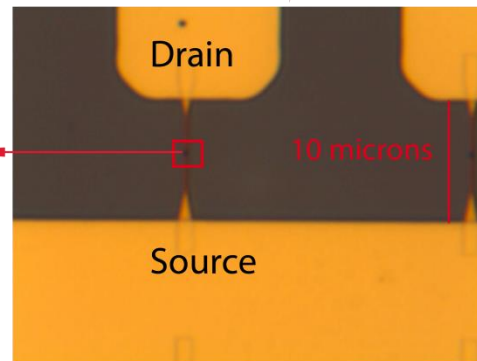
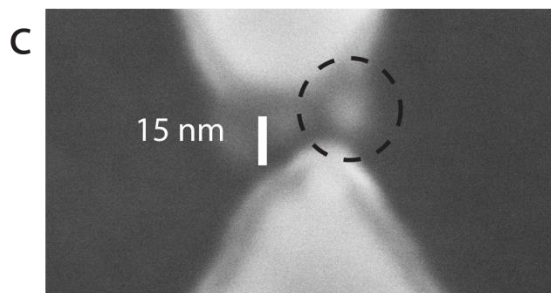
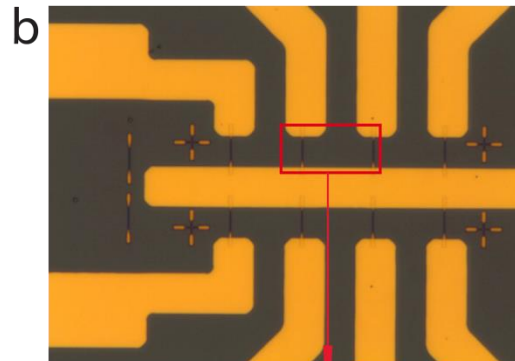
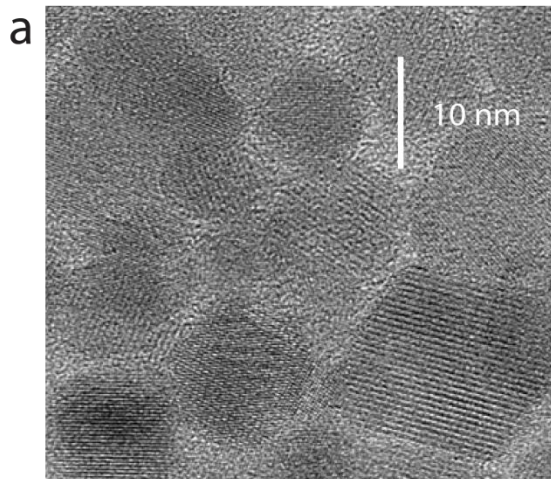


# Verwey transition in magnetite ( $\text{Fe}_3\text{O}_4$ )

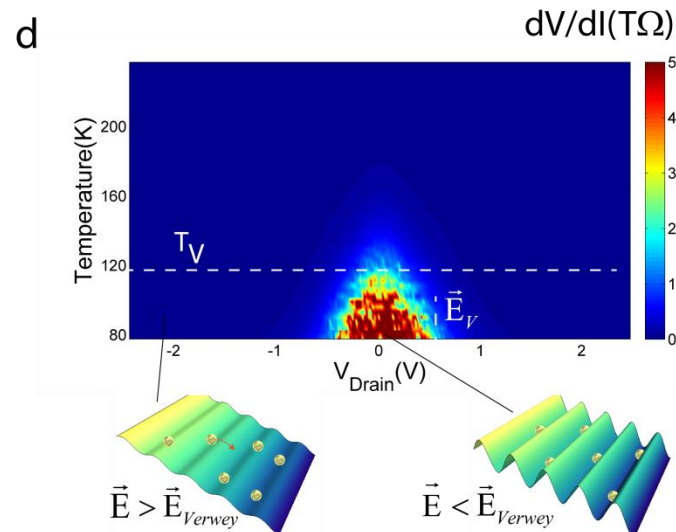
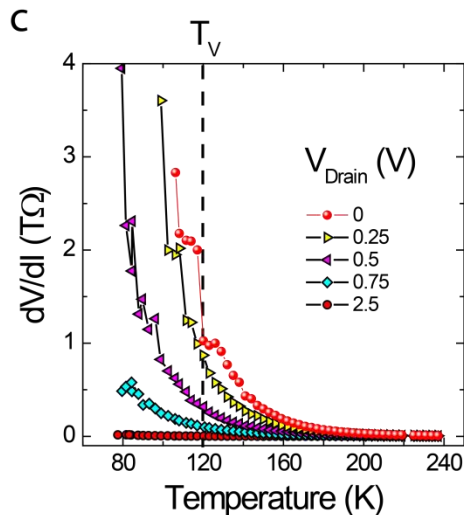
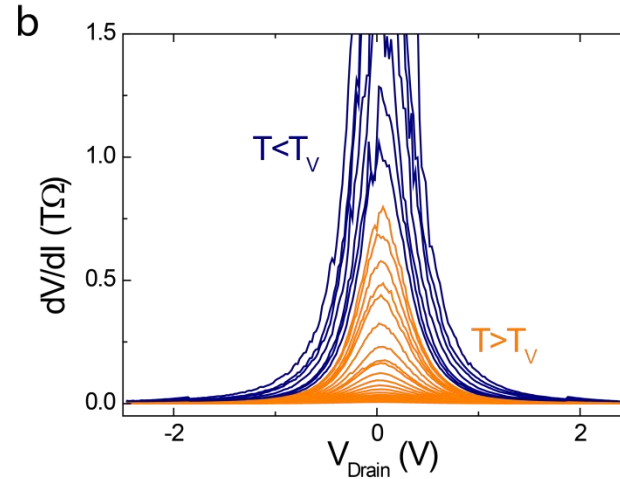
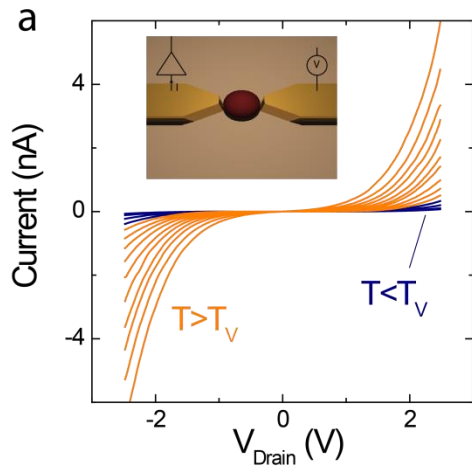


# Verwey transition in single magnetite nanoparticles

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# Verwey transition in single magnetite nanoparticles



$$d \approx 15 \text{ nm}$$

$$|\vec{E}_V| = V_V/d = 3.3 \cdot 10^5 \text{ V cm}^{-1}$$

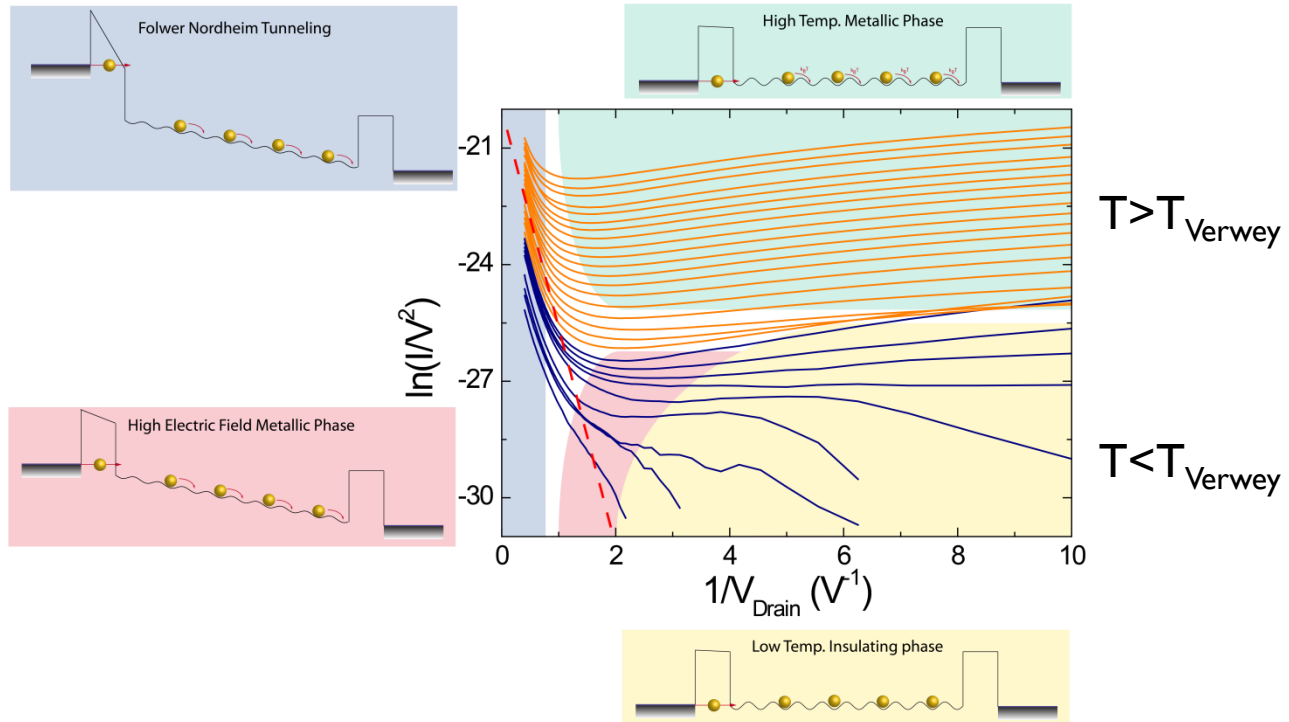
$$a = 0.295 \text{ nm}$$

potential depth :

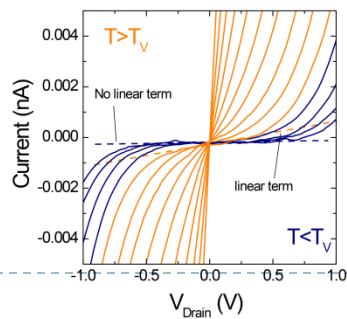
$$V_t = |\vec{E}_V| \times a \approx 9.8 \text{ meV}.$$

# Fowler-Nordheim Plot

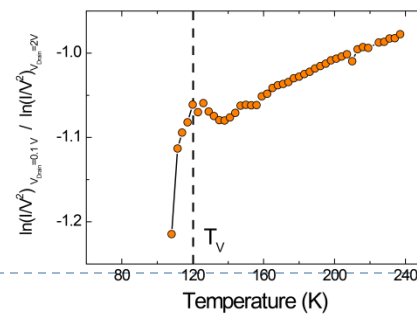
a



b

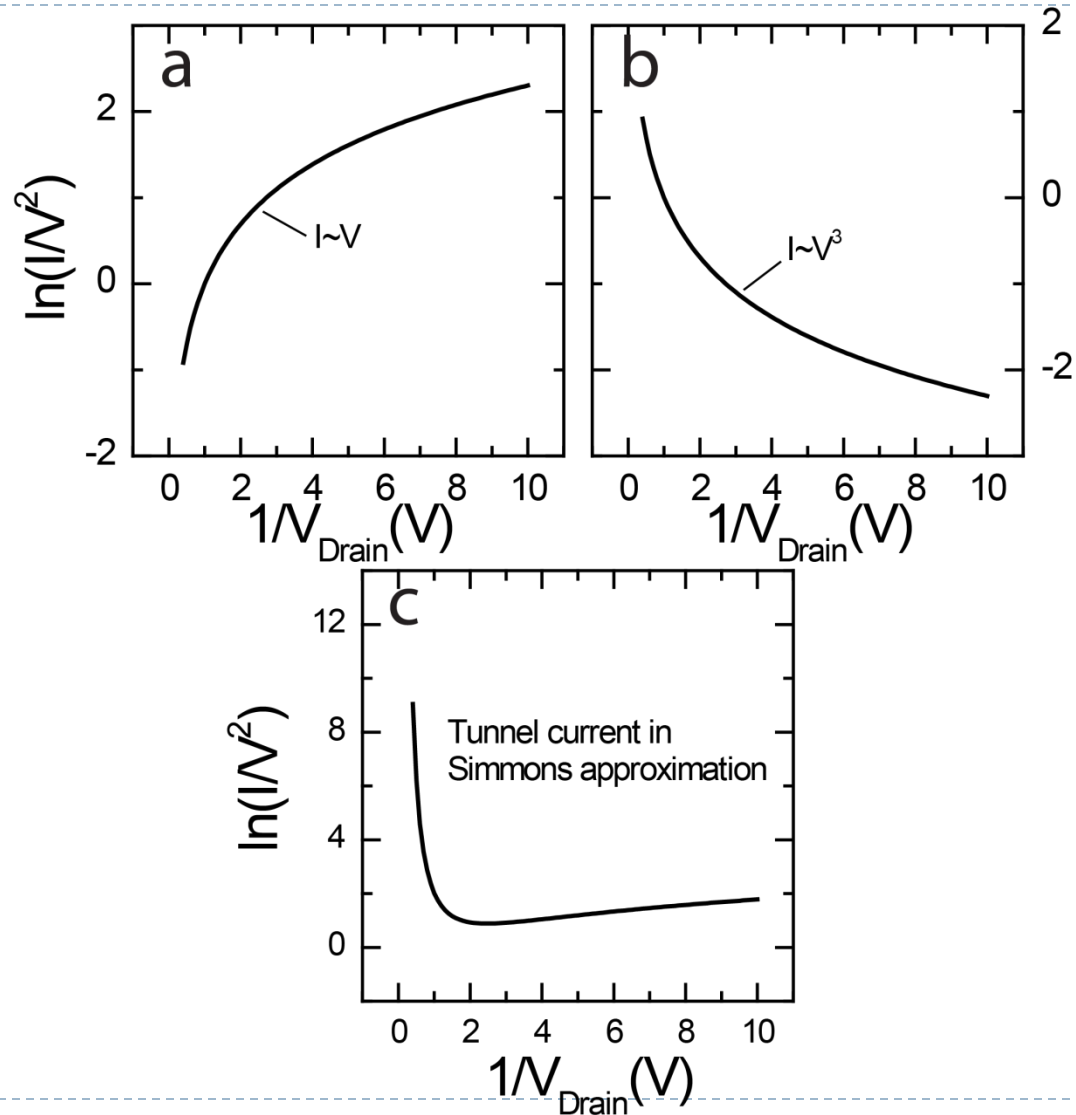


c

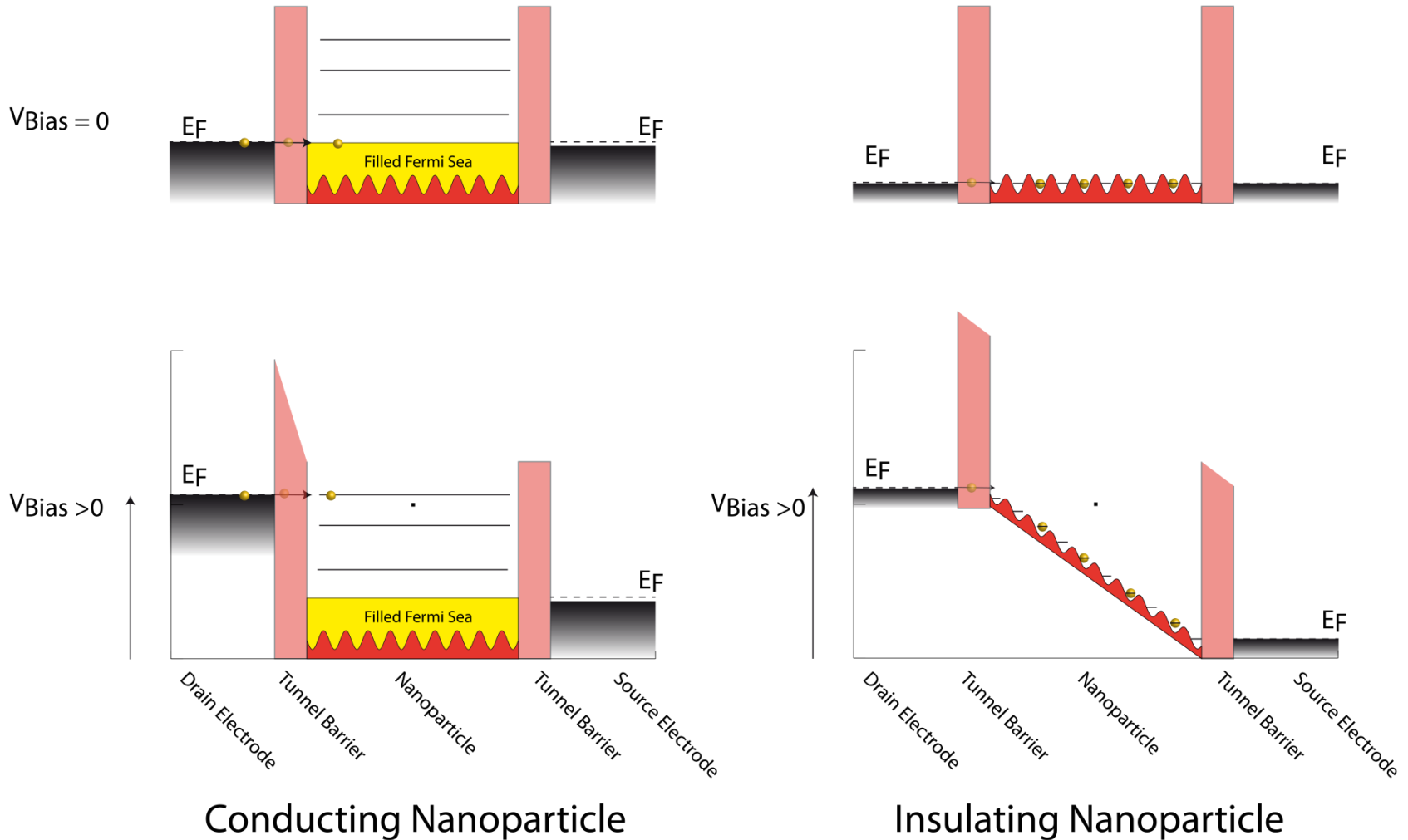


- ▶ Effective long distance hopping in metallic nanoparticles arrays is possible because of cotunneling
  - ▶ Efros-Shklovskii laws applies in metallic nanoparticles arrays as a function of temperature, but also as function of electric field.
  - ▶ A new projection method of preparing single nanoparticles devices
  - ▶ Allows to study non-equilibrium Verwey transition in magnetite
-

# Contributions to Folwer-Nordheim plot



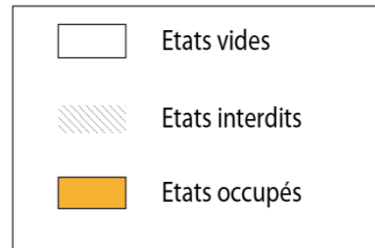
# Verwey transition in single magnetite nanoparticles



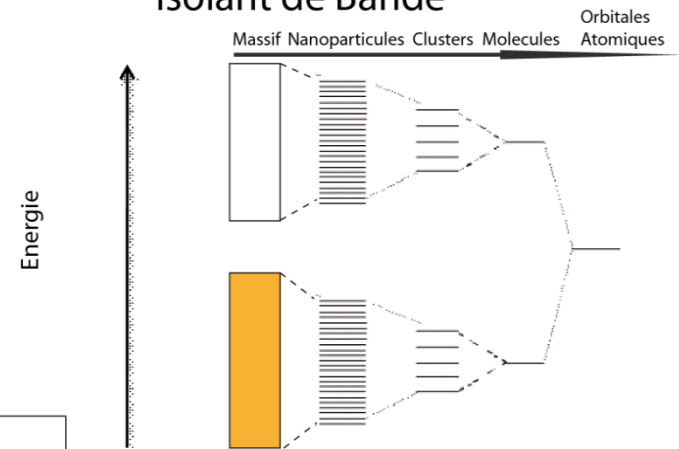
# Tunneling spectroscopy of nanoparticles

## ▶ To study the construction of band structures with discrete electronic levels

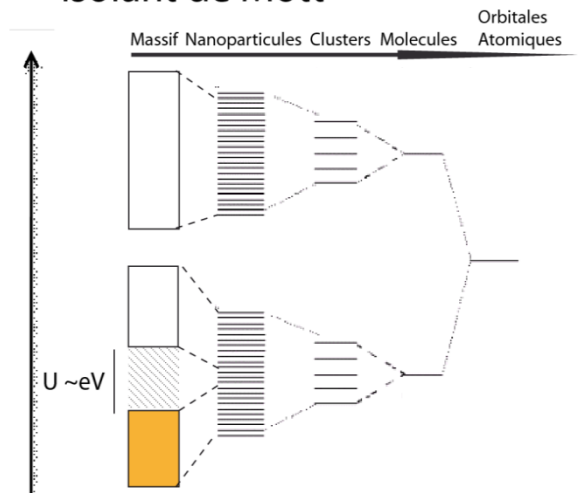
- ▶ Semi-conductors (strong quantum confinement effects)
- ▶ Metals (fractal wave functions, random matrix theory and relation with Anderson localization)
- ▶ Semi-metals (no studies so far)
- ▶ Mott Insulator (no studies so far)
- ▶ Superconductors (only a few works)



## Isolant de Bande



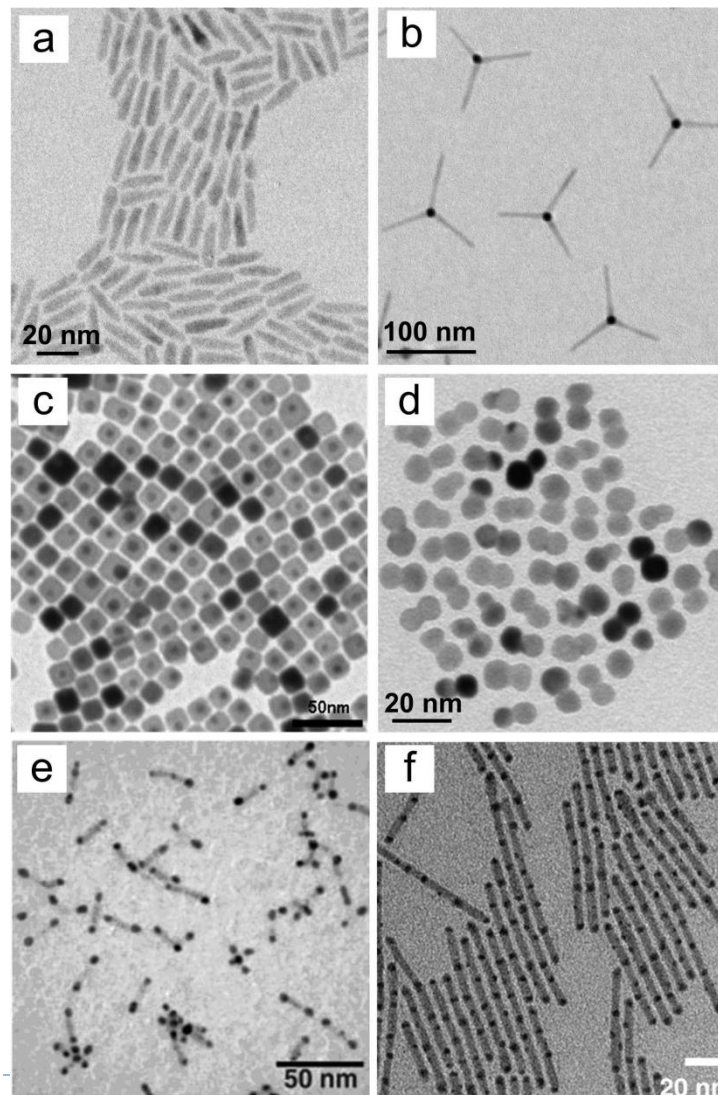
## Isolant de Mott





# A plethora of nanoparticles

- (a) CdSe/CdS nanorods
- (b) CdSe/CdS
- (c) Au/PbS core-shells
- (d) CoPt<sub>3</sub>-Au dumbbells
- (e) Au-CdSe-Au rods
- (f) CdS-Au<sub>2</sub>S segmented nanoheterostructures.



Talapin et al.  
*Chem. Rev.* 2010, **110**, 389

# Electron transport in granular films (Ni-SiO<sub>2</sub>) as function of electric field

Sheng, P. & Abeles, B.  
*Physical Review Letters* **28**, 34-37(1972).

Activated law as function of electric field

$$I = I_0 \exp(-E_{Coulomb} / eV)$$

