

Toward the theory of **strongly coupled Quark-Gluon Plasma** (sQGP)

Edward Shuryak

Department of Physics and Astronomy

State University of New York

Stony Brook NY 11794 USA

Outreach of the field is exponentially expanding...

- Why do we think we have **strongly coupled quark-gluon plasma (sQGP)** at $T=(1-2)T_c$?
(4 slides, a summary of main arguments)
- **Flows and near-perfect liquid**
- **classical strongly coupled non-Abelian plasma and its first molecular dynamics (MD)**
- **“New spectroscopy” at $T > T_c$: mesons, colored pairs, baryons, electric chains...**
- **Topology and “post-confinement”:** monopoles, instantons $\Rightarrow N_c$ dyons \Rightarrow flux tubes \Rightarrow large potentials at $T > T_c$? (connections to $N=2$ SUSY YM)
- **Summary**
- (Comment: lessons from AdS/CFT with strongly coupled $N=4$ theory are spread all over the talk)

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- 1d: very strong **jet quenching, including charm**, again well beyond pQCD, no Casimir scaling...

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- 2d: **Polymeric “electric” chains of gluons** $\bar{q} - g - g \dots q$

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- (3e: a **complete gravity dual to RHIC**, with black hole production => ES, Sin+Zahed, sorry no time on that)

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- **New conjecture: sQGP is a plasma of both electric and magnetic charges (to be studied)**

Flows and transport properties at RHIC

Magdeburg hemispheres 1656

(recall here
pumped out
Magdeburg
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- **We cannot pump the QCD vacuum out, but we can pump in something else, namely the Quark-Gluon Plasma**
- **QGP proposed in 1970's was expected to be simple near-ideal gas.**

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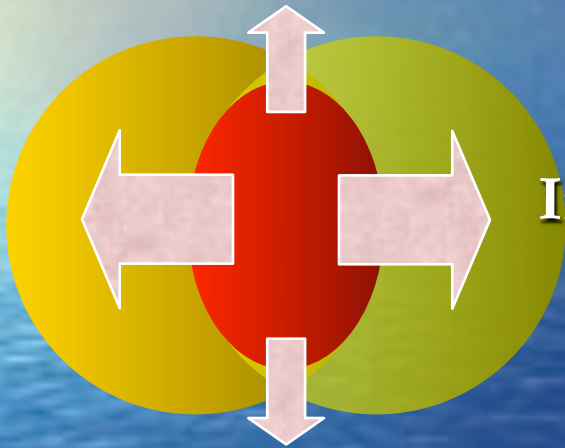
But something else was on the way...

We believed if we increase the energy density, we should eventually get weakly interacting QGP. But something else was found on the way...

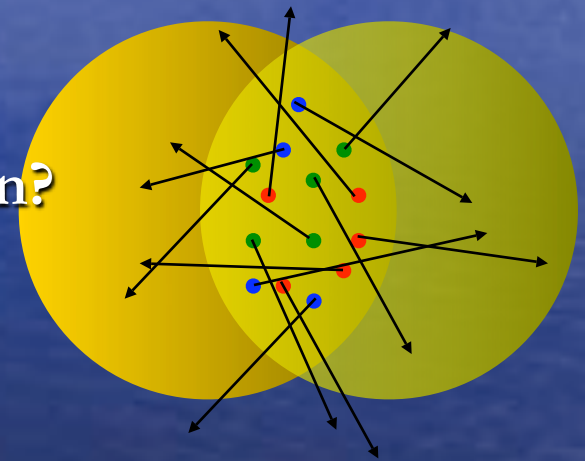
How Hydrodynamics Works at RHIC

Elliptic flow

How does the system respond to initial spatial anisotropy?

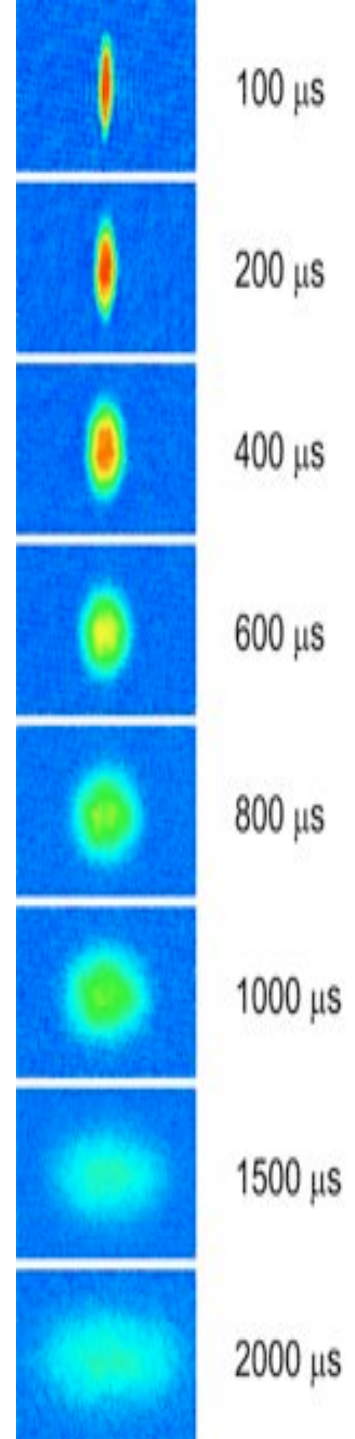


Dense or dilute?
If dense, thermalization?
If thermalized, EoS?

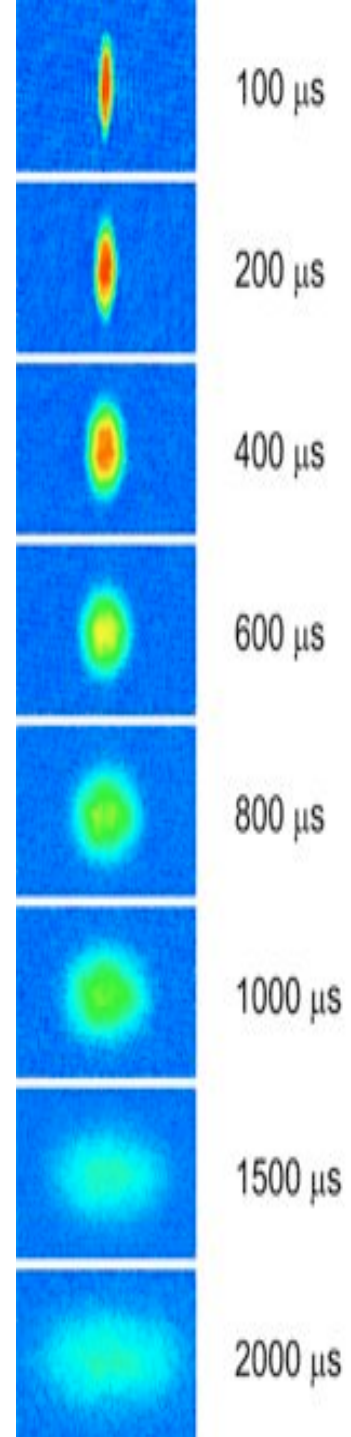


$$\frac{dN}{p_T dp_T dy d\phi} = \frac{1}{2\pi} \frac{dN}{p_T dp_T dy} (1 + 2v_1 \cos(\phi) + 2v_2 \cos(2\phi) + \dots)$$

$$v_2(p_T, y) = \frac{\int d\phi \cos(2\phi) \frac{dN}{p_T dp_T dy d\phi}}{\int d\phi \frac{dN}{p_T dp_T dy d\phi}} = \langle \cos(2\phi) \rangle$$



The coolest thing on Earth, $T=10$ nK or $10^{(-12)}$ eV can actually produce a **Micro-Bang !** (O'Hara et al, Duke)

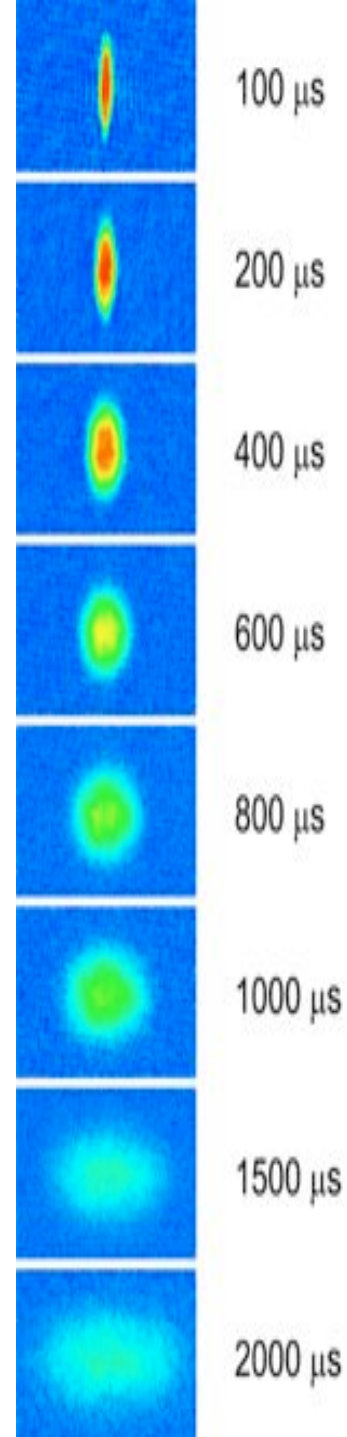


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Elliptic flow with ultracold trapped Li6 atoms, $a \Rightarrow$ infinity regime

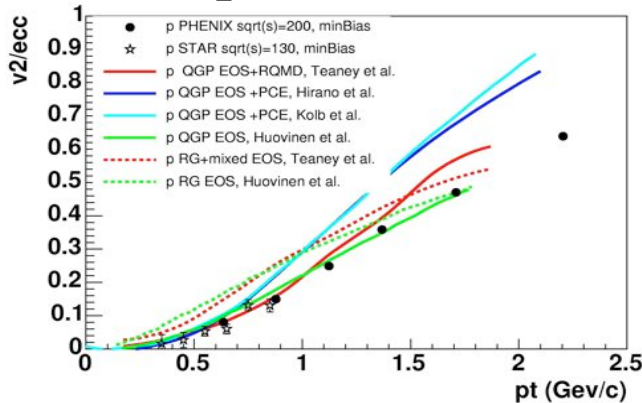
The system is extremely dilute, but can be put into a hydro regime, with an elliptic flow, if it is specially tuned into a strong coupling regime via the so called Feshbach resonance

Similar mechanism was proposed (Zahed and myself) for QGP, in which a pair of quasiparticles is in resonance with their bound state at the "zero binding lines"

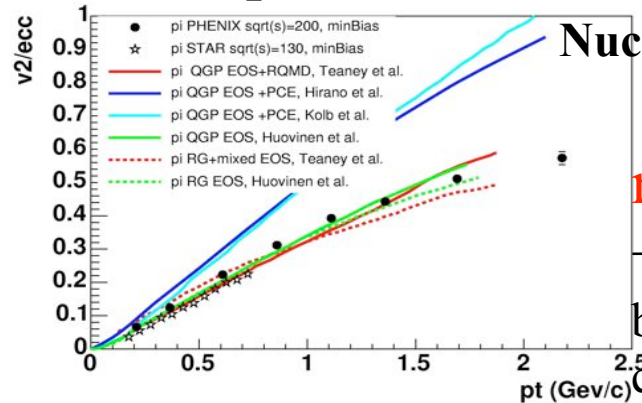


2001-2005: hydro describes radial and elliptic flows for **all secondaries** , $p_T < 2 \text{ GeV}$, centralities, rapidities, A (Cu,Au)...
 Experimentalists were very sceptical but were

proton



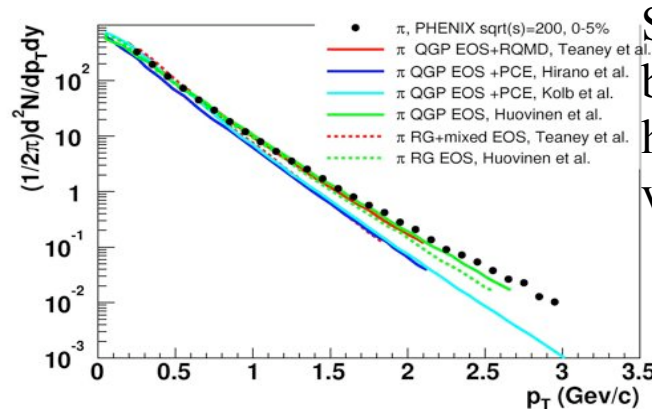
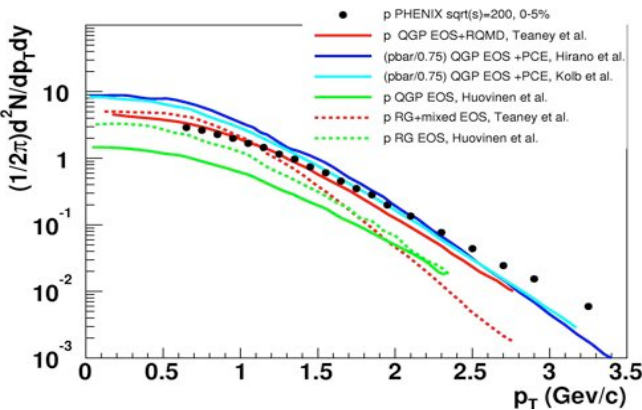
pion



PHENIX,

Nucl-ex/0410003

red lines are for ES +Lauret+Teaney done before RHIC data, never changed or fitted, describes SPS data as well! It does so because of the correct hadronic matter /freezeout via (RQMD)



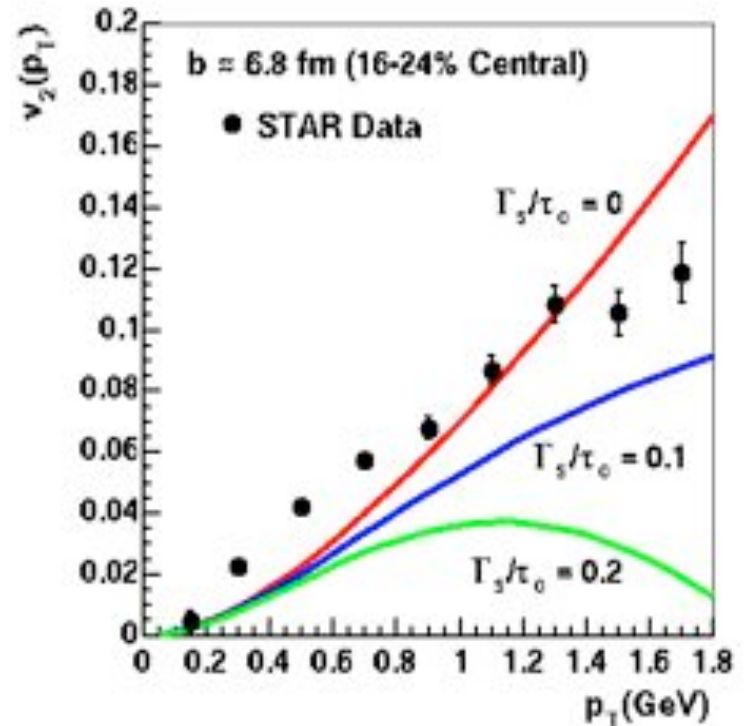
Viscosity reduces v_2 and changes its p_t dependence:

QGP at RHIC seem to be the most ideal fluid known, viscosity/entropy = .1 or so
~~water would not flow if only a drop with 1000 molecules be made~~

Correction $\propto \frac{\eta}{s} p_t^2$

$\Rightarrow \eta/s \approx .1-.3$

($1/4\pi \leq \text{AdS/CFT}$)



Sonic boom from quenched jets

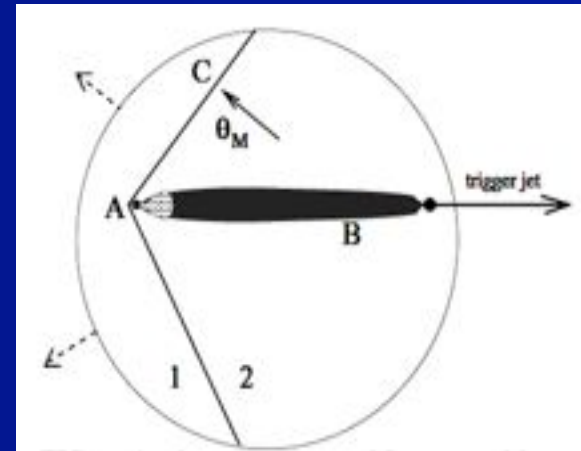
Casalderrey,ES,Teaney,

- the energy deposited by jets into liquid-like strongly coupled QGP must go into **conical shock waves**
- We solved relativistic hydrodynamics and got the flow picture
- If there are start and end points, there are two spheres and a cone tangent to both

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Wake effect or “sonic boom”

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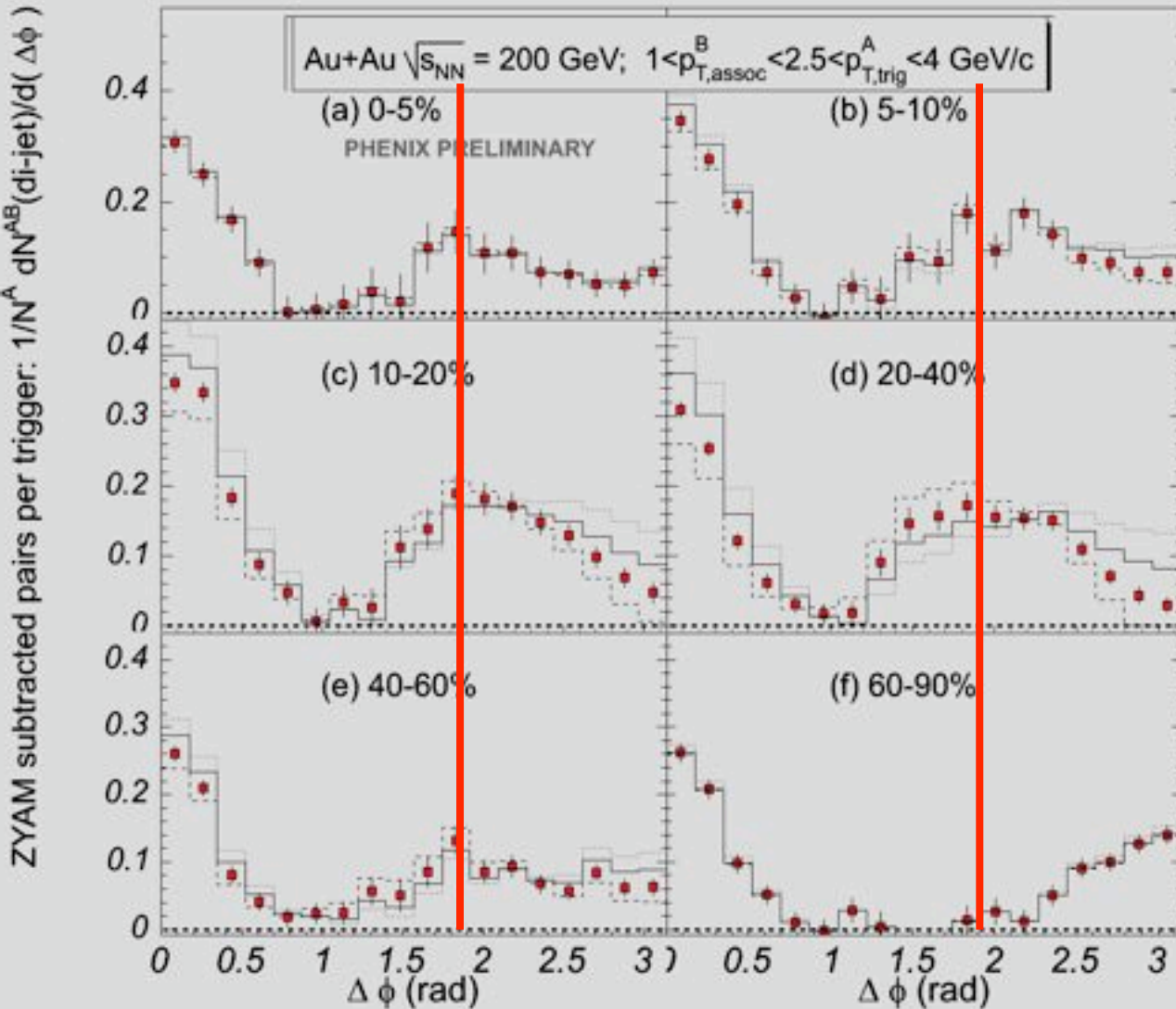


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PHENIX jet pair distribution



Note: it is only projection of a cone on phi

Note 2: more recent data from STAR find also a minimum in

$\langle p_t(\phi) \rangle$ at 180 degr., with a value

Consistent with background

Studies of a charge moving in sQGP at strong coupling (AdS/

- AdS/CFT allows to study a charge moving

With fixed velocity in a system:

A string pending and falling into the black hole

- L.Yaffe talk here, and also D.Teaney and J.Casalderrey found such solution at nonzero T calculating dE/dx (the drag force) , sonic boom etc

**Explaining transport in
sQGP:**

**Classical QGP and its
Molecular Dynamics**

(B.Gelman,ES,I.Zahed,

- For $SU(2)$ charge Q is a unit vector, $\vec{Q} = (Q^1, Q^2, Q^3)$

$$\begin{aligned} dx_i/dt &= p_i/m, \\ dp_i/dt &= (g^2/4\pi) \sum \vec{Q}_i \cdot \vec{Q}_j / r_{ij}^2, \\ d\vec{Q}_i/dt &= (g^2/4\pi) \sum \vec{Q}_i \times \vec{Q}_j / |r_{ij}| \end{aligned}$$

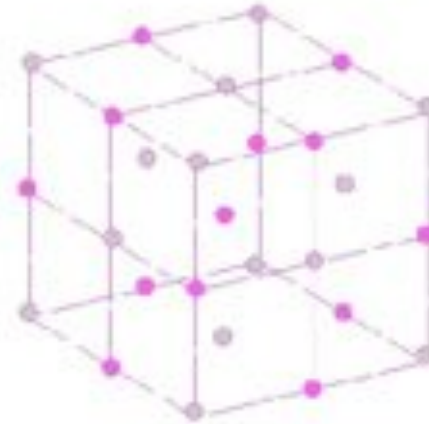
- Note: $d\vec{Q}_i^2/dt = 0$

Wong eqn can be rewritten as
x-p canonical pairs, 1 pair for $SU(2)$, 3 for $SU(3)$,
(as a so called Darboux variables).
We do $su(2) \Rightarrow C$ is a unit vector on a sphere $O(3)$

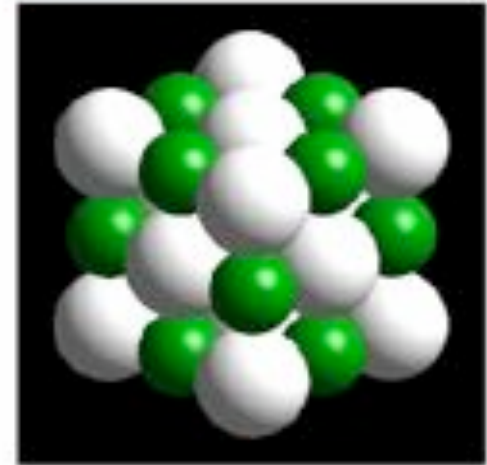
As $\Gamma = \langle |E_{\text{pot}}| \rangle / \langle E_{\text{kin}} \rangle$ grows
gas \Rightarrow liquid \Rightarrow solid

- This is of course for +/- Abelian charges,
- But “green” and “anti-green” quarks do the same!

NaCl Structure

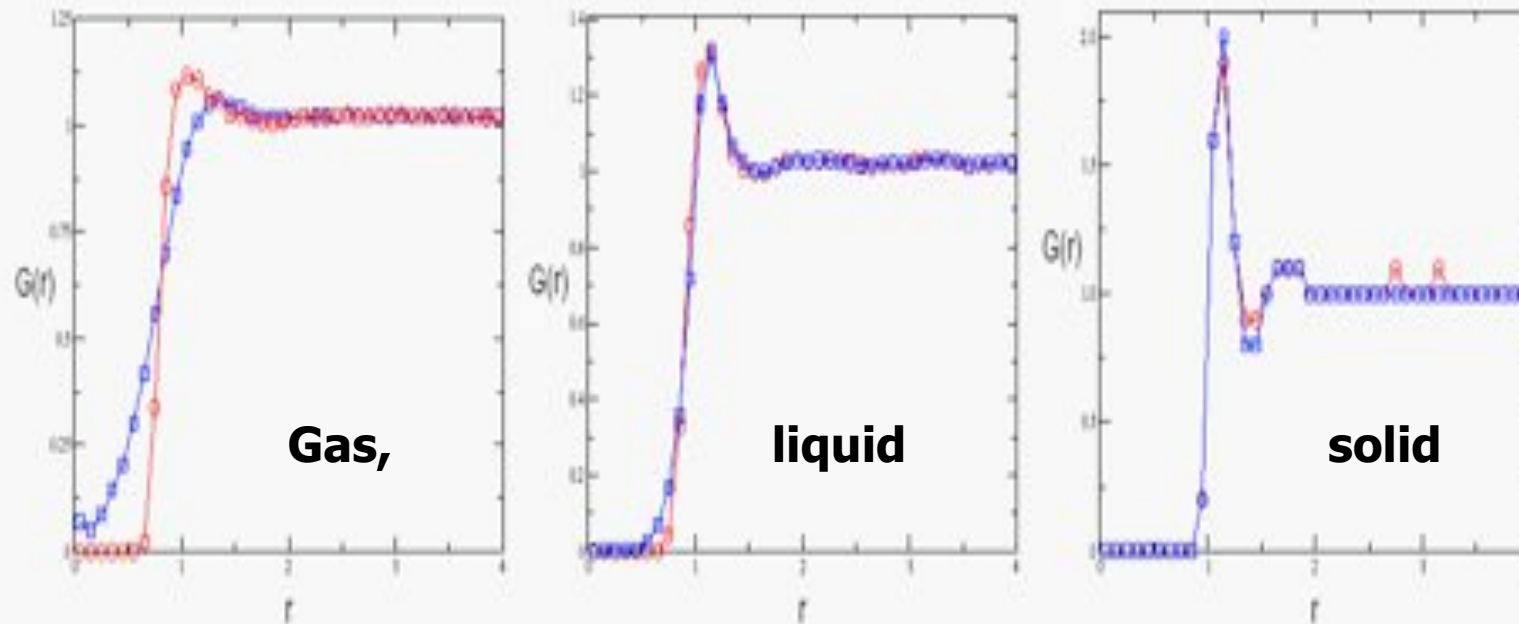


NaCl Structure with
Face Centered Cubic Bravais Lattice



• local order would be preserved in a liquid also,
as it is in molten salts (strongly coupled TCP with
 $\langle \text{pot} \rangle / \langle \text{kin} \rangle = O(60)$, about 3-10 in sQGP)

Structure factor for cQGP



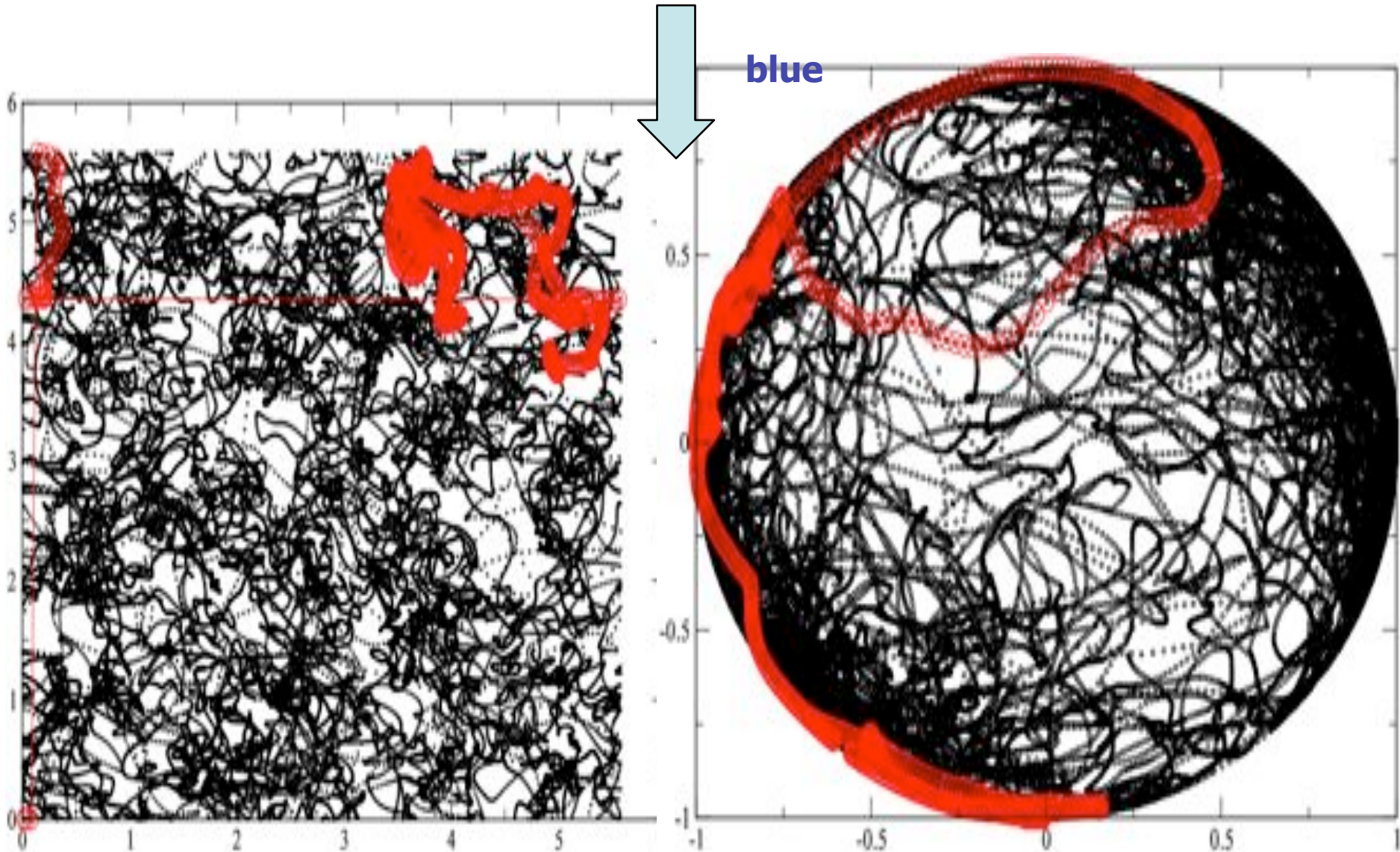
- G_d correlation function for $\Gamma = 0.83, 31.3, 131$, respectively; red circles correspond to $t^* = 0$, and blue squares correspond to $t^* = 6$
- $\Gamma = 0.83$ is a weak correlation between the particles; relaxes rather quickly with time
- The correlation is more robust for $\Gamma = 31.3$ (*liquid*)
- For $\Gamma = 131$ correlation is very stable (*solid*)

**cQGP made of 64 colored particles,
projection of a cube on x-y plane,
red is the path of particle #1.**

**strong coupling,
Gamma is about 100
close to freezing**

Color -> red

blue

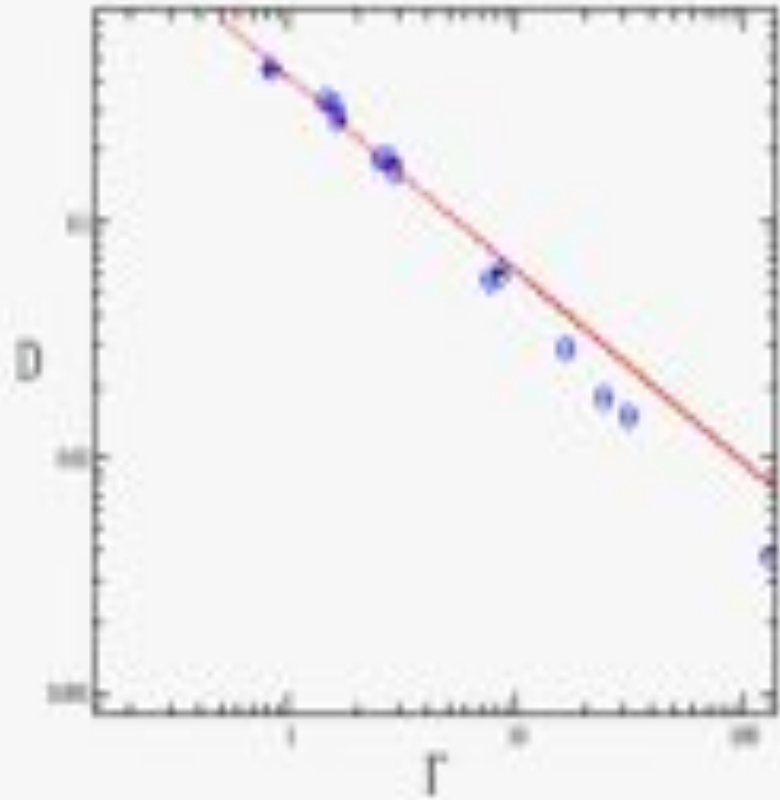


Self-diffusion

$$D(\tau) = \frac{1}{3N} \left\langle \sum_{i=1}^N \vec{v}_i(\tau) \cdot \vec{v}_i(0) \right\rangle$$

$$D = \int_0^{\infty} D(\tau) d\tau$$

$$D \approx \frac{0.4}{\Gamma^{4/5}}$$



Shear viscosity

- Green-Kubo relation for viscosity

$$\eta = \int_0^{\infty} \eta(\tau) d\tau$$

$$\eta(\tau) = \frac{1}{3TV} \left\langle \sum_{x<y} \sigma_{xy}(\tau) \sigma_{xy}(0) \right\rangle$$

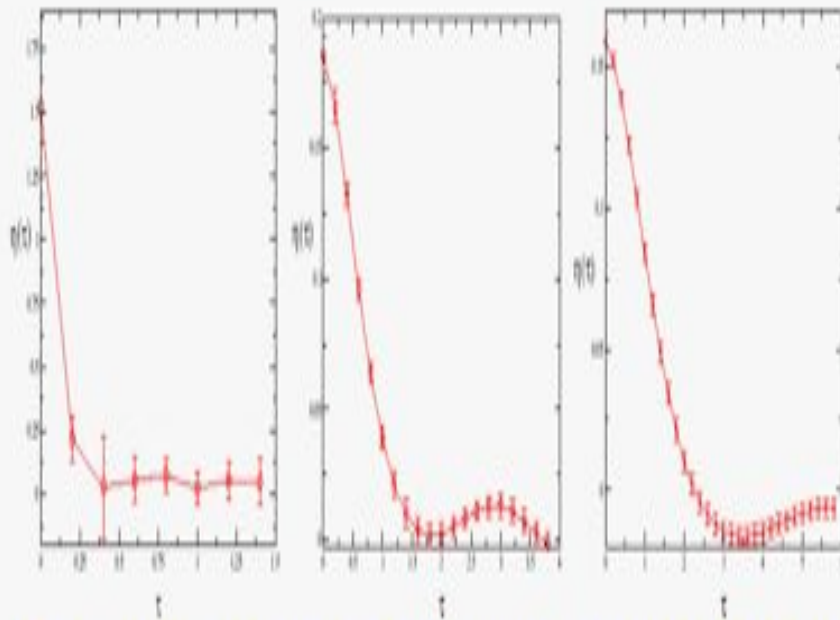
$\sum_{x<y}$ —a sum over the three pairs of distinct tensor components (xy , yz and zx); the stress-energy tensor are given by

$$\sigma_{xy} = \sum_{i=1}^N m_i v_{ix} v_{iy} + \frac{1}{2} \sum_{i \neq j} r_{ij,x} F_{ij,y}$$

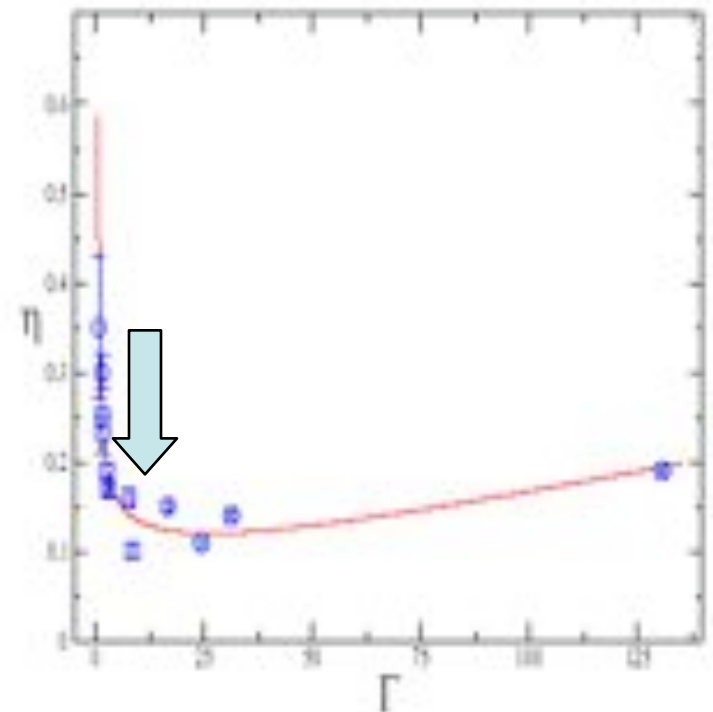
\vec{F}_{ij} is the force on particle i due to particle j

First results on viscosity:

QGP (blue arrow) is about the best liquid one can possibly make



• Stress-tensor autocorrelation correlation function $\eta(t)$ for $\Gamma \equiv$
0.83, 31.3, 131



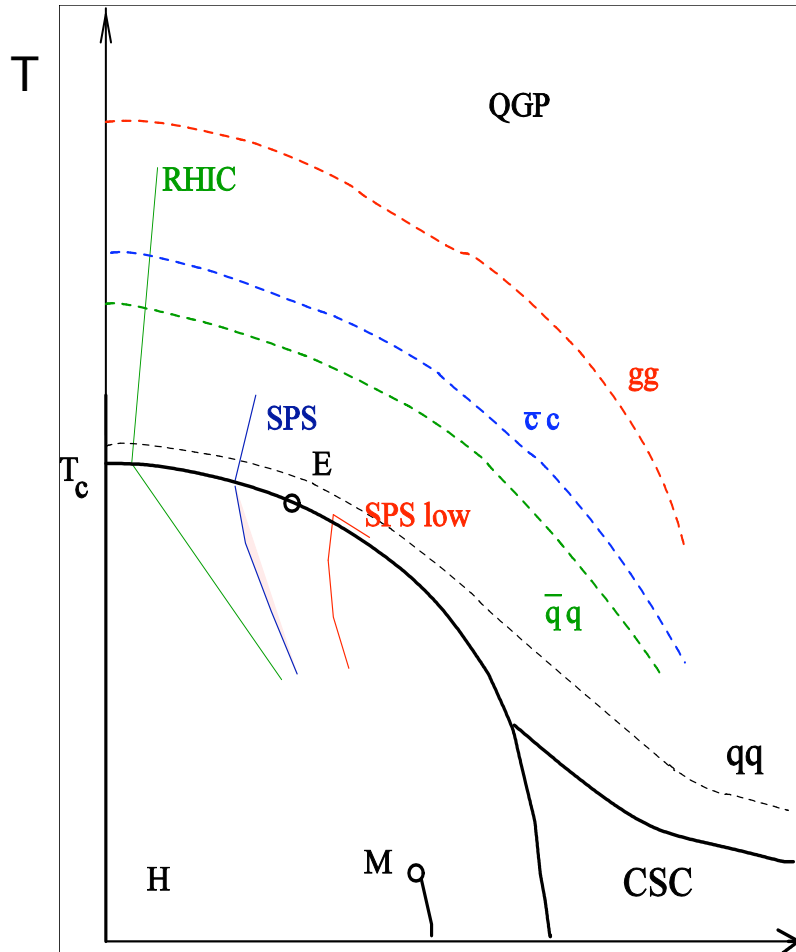
$$\eta \approx 0.001 \Gamma + \frac{0.242}{\Gamma^{0.3}} + \frac{0.072}{\Gamma^2}$$

“New spectroscopy” in sQGP

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2003: Can mesons survive deconfinement?

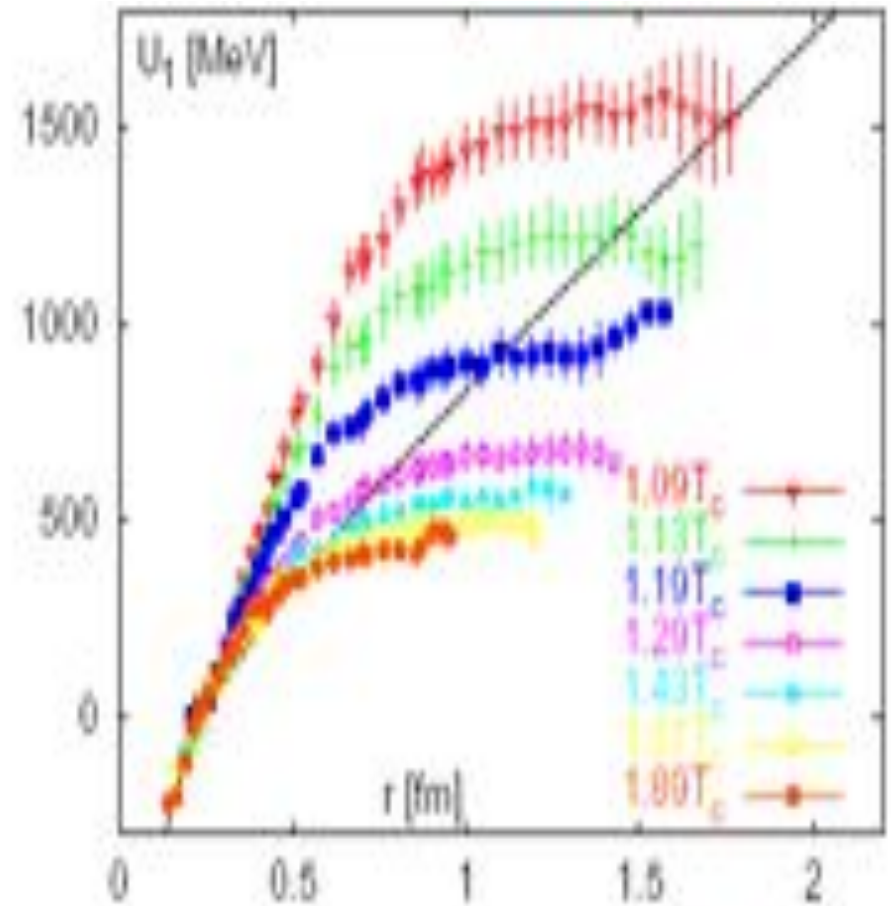
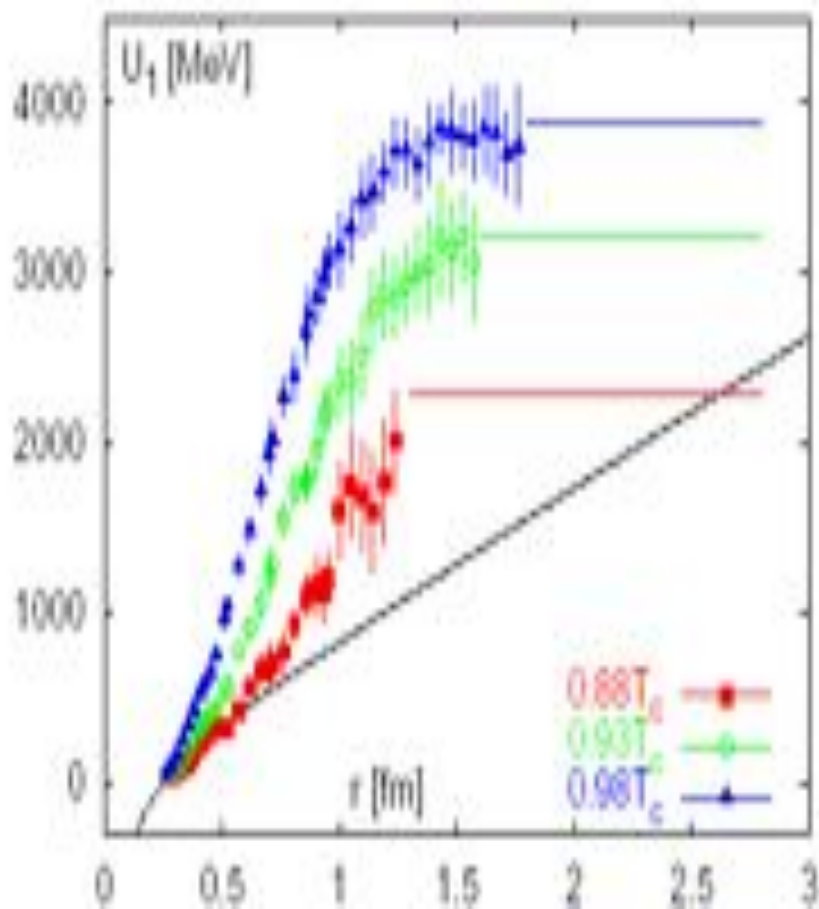


Chemical potential
 μ

Can resonance scattering help explain small m.f.p.? (It does for atoms)

Are regions of **meson binding** the divider between wQGP and sQGP? (ES+I.Zahed, "rethinking" paper PRC 2003, the beginning of sQGP...):

“Postconfinement”
potential energy of a static dipole
at $T=(1-2)T_c$ and $r=.5-1$ fm is even larger



Solving for the bound states

ES+I.Zahed, hep-ph/0403127

- **Charmonium remains bound till $2T_c \Rightarrow$ confirmed by lattice correlators and now by direct RHIC J/Psi data**
- **In QGP there is no confinement \Rightarrow Hundreds of colored channels SHOULD have bound states as well**

channel	rep.	charge factor	no. of states
gg	1	9/4	9_s
gg	8	9/8	$9_s * 16$
$qg + \bar{q}g$	3	9/8	$3_c * 6_s * 2 * N_f$
$qg + \bar{q}g$	6	3/8	$6_c * 6_s * 2 * N_f$
$\bar{q}q$	1	1	$8_s * N_f^2$
$qq + \bar{q}\bar{q}$	3	1/2	$4_s * 3_c * 2 * N_f^2$

the strongest

The usual

weak

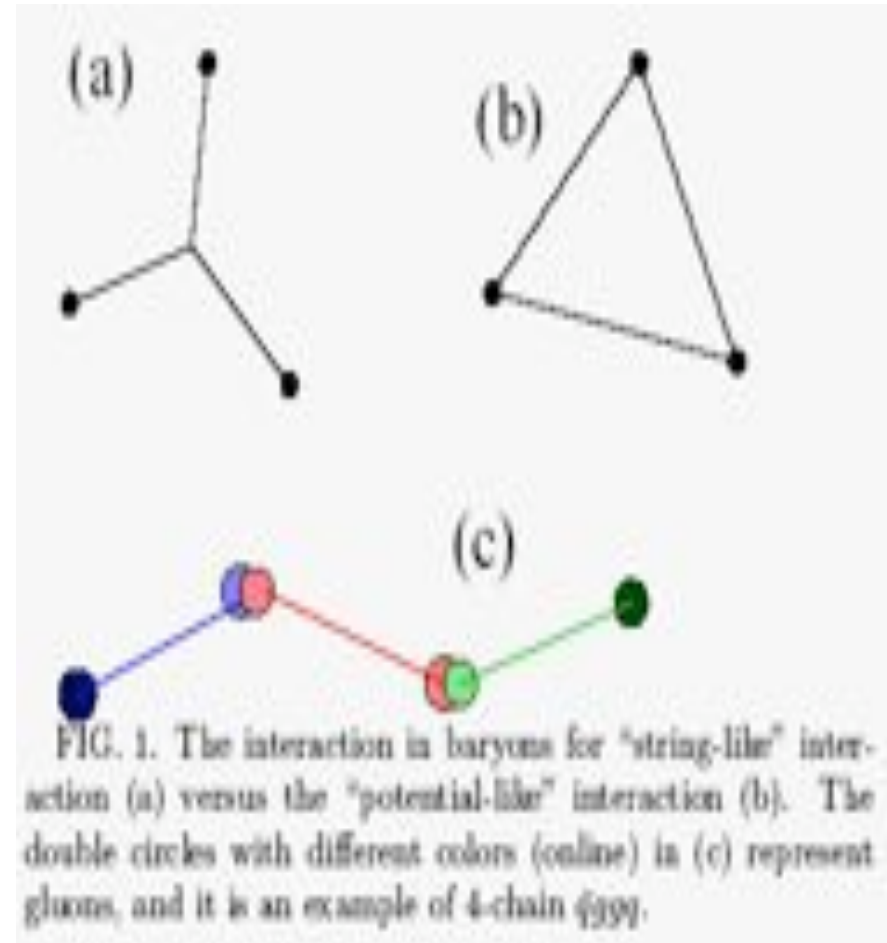
• gg color $8*8=64=27+2*10+2*8+1$: only the 2 color octets $(gg)_8$ have $(16*3_s * 3_s = 144)$ states.

Baryons at $T > T_c$? Polymer chains?

J.Liao+ES,05

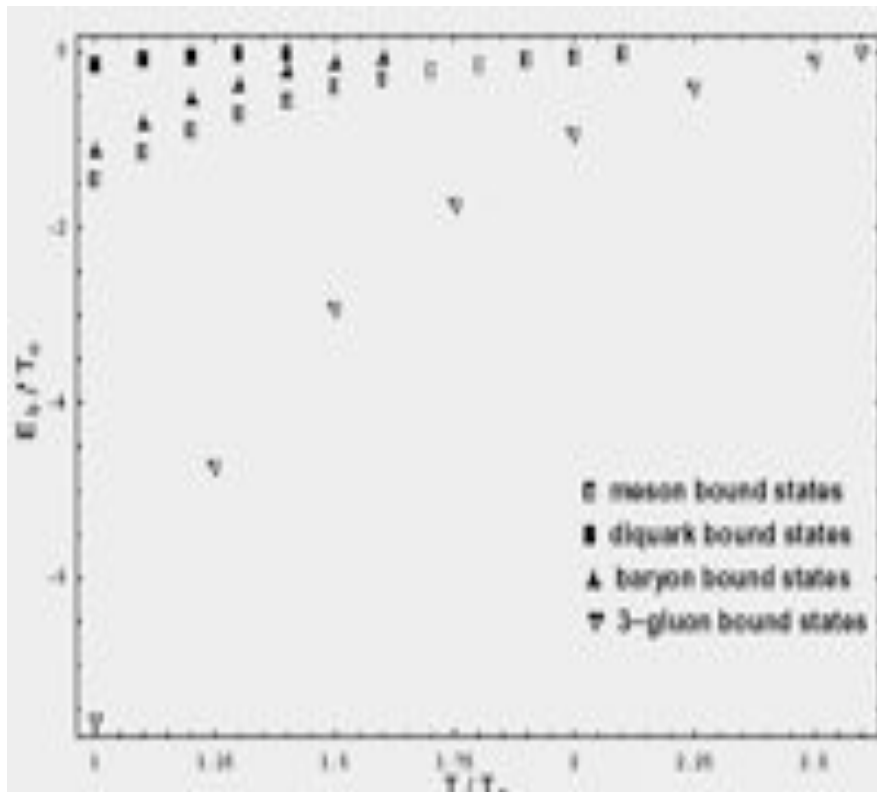
- Lattice favors “potential-like” (b) behavior of the potentials for baryons.
- $(a) = V(1j) + V(2j) + V(3j)$
(j=junction)
- $(b) = (V(12) + V(13) + V(23))(1/2)$
Casimir
- Fortunately $\langle V \rangle(a)$ and $\langle V \rangle(b)$ do not differ by more than 15%!

- **polymeric chains**
 $\bar{q} g \dots g q$, with color indices convoluted as writte



Bindings from variational calculation for baryons and ggg chain (J.Liao+ES, 05)

electric chains have the same binding as mesons per link



structure	-body	G	E_b at T_c	T_m
$\bar{q}q$	2	1	-1.45	2.1
$\bar{q}g \cdots gq$ (polymer chain)	N	1	$-1.45 \cdot (N-1)$	2.1
ggg (closed chain)	3	1	-7.64	2.6
qq	2	1/2	-0.13	1.4
qqq (close chain)	3	1/2	-1.10	1.6

Polymeric chains in strongly coupled Higgsed $N=4$ (J.Minahan 98)

N_c branes are put not at the same point, but say 2 lumps $N_c/2$ + $N_c/2 \Rightarrow$

Massive gluons

String solutions with a string oscillating between the lumps

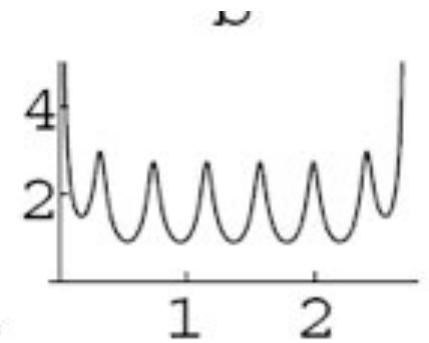
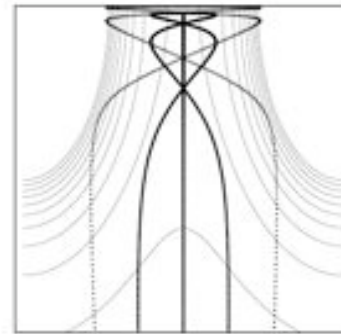


Fig. 2: Geodesics with six half oscillations. As L is increased, the geodesic approaches the concatenation of the BPS geodesics of two quarks and a five W s.

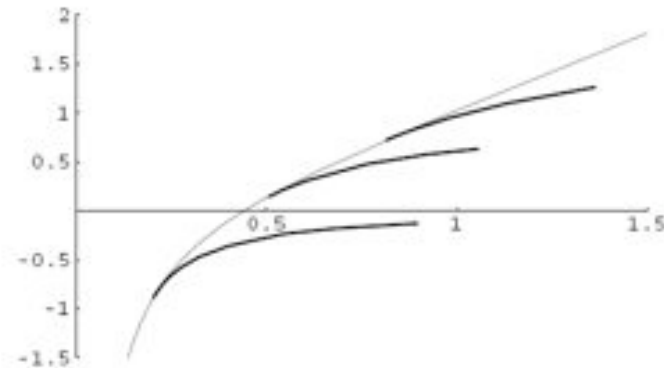
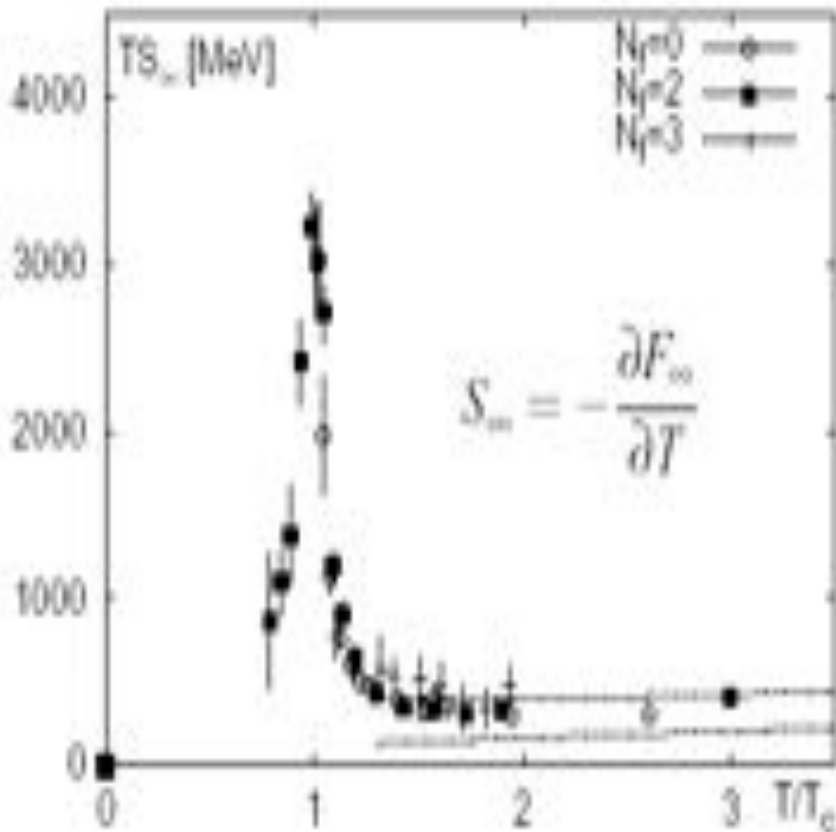


Fig. 3: Plot of E vs. L for the saddle branch and the first three coulomb branches. E is plotted in units of the W mass, m_W , and L is in units of R^2/m_W . The first and third branches are doubly degenerate. The second branch is a \mathbb{Z}_2 symmetric branch.

Entropy associated with a static dipole gets huge! (shown at large r vs T/T_c)



- **S/charge = 0(10)**
- **#(states) = exp(10)**
- **What those states may be?**
- **string picture**
(Polyakov 78 => Klebanov, Maldacena, Thorn et al hep-th/0602255)
- **electric polymers (Liao, ES 05 ... Ads/CFT Minahan 98)**
- **trapped monopoles?**

Postconfinement and monopoles at $T > T_c$

monopoles in QGP

monopoles in QGP

- Dual superconductivity as a confinement mechanism ('tHooft, Mandelstam 1980's) require monopole condensation (nonzero VEV)

monopoles in QGP

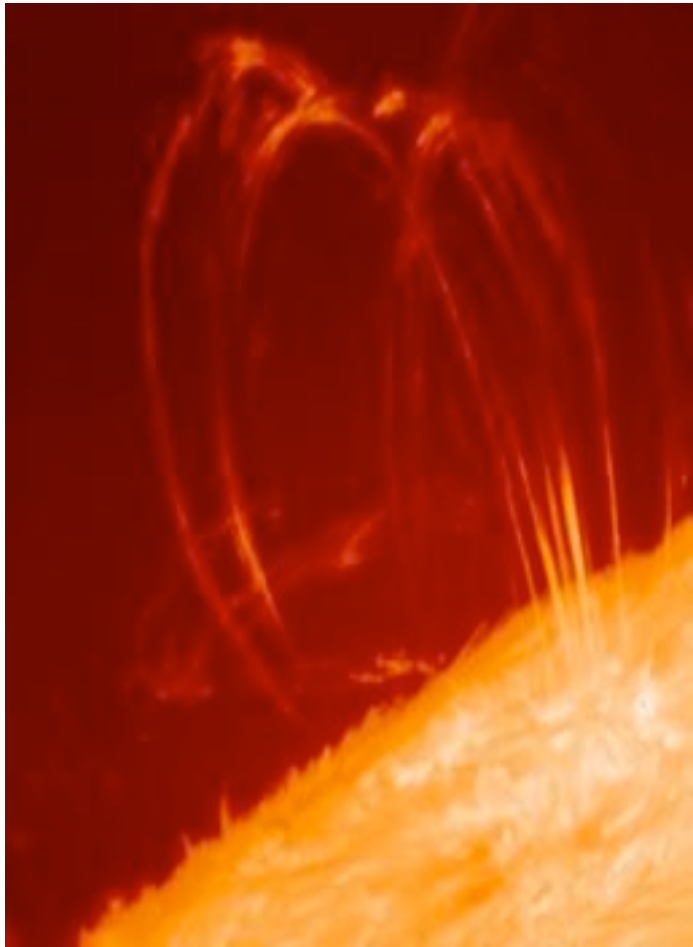
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monopoles in QGP

- Dual superconductivity as a confinement mechanism ('tHooft, Mandelstam 1980's) require monopole condensation (nonzero VEV)
- But maybe we better look at $T > T_c$ and study dyon dynamics **without condensation when they are heavy/classical enough?**
- Lorentz force on monopoles makes them reflect from a region with E, or even rotate around the E flux => compresses E into flux tubes even in classical plasma!

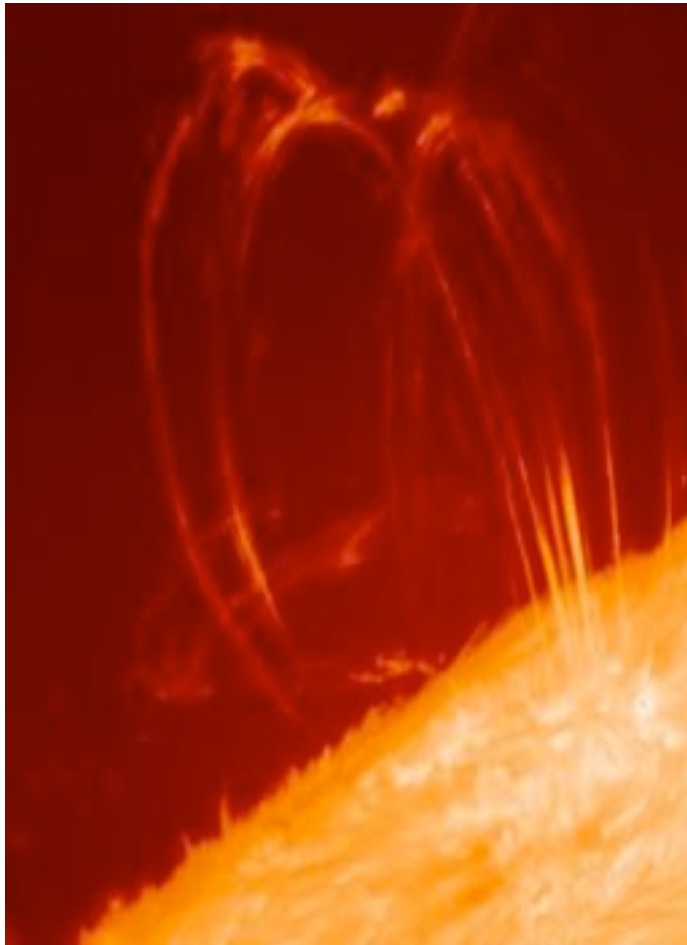
Can a flux tube exist **without**
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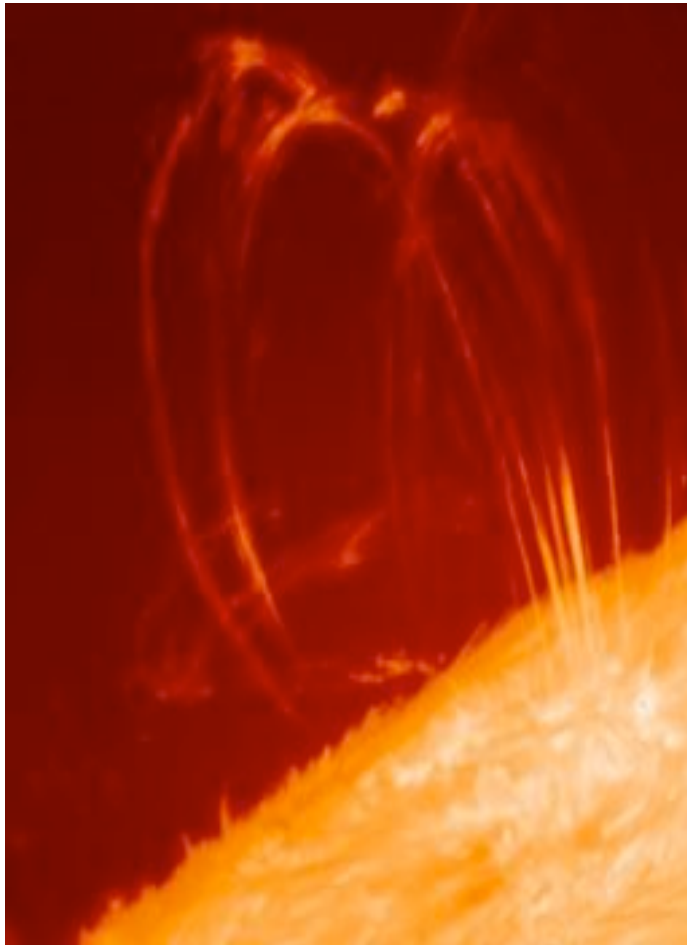
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- Here are magnetic **flux tubes at the Sun,**



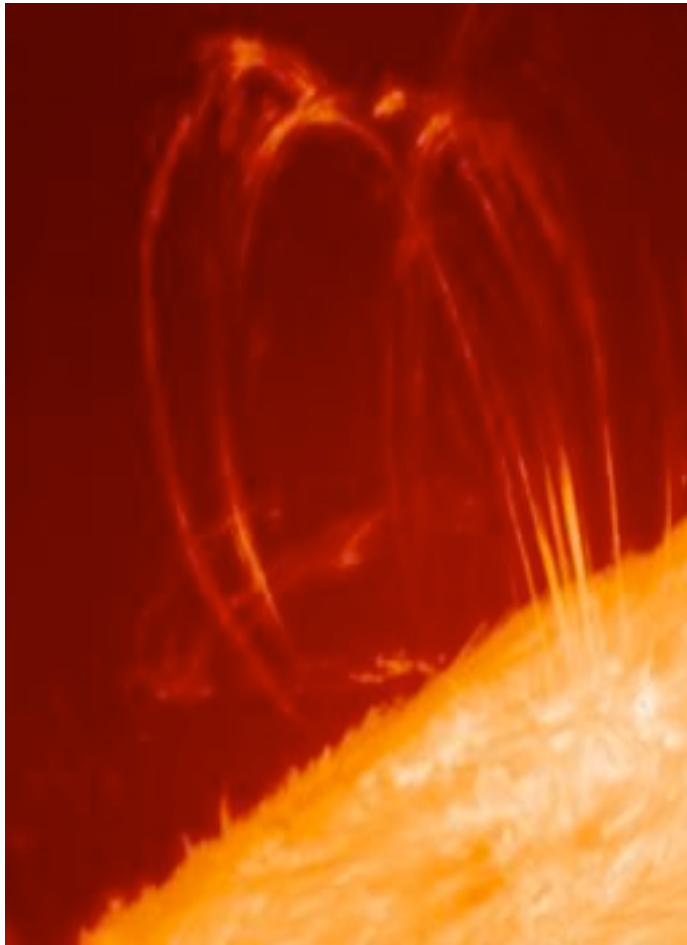
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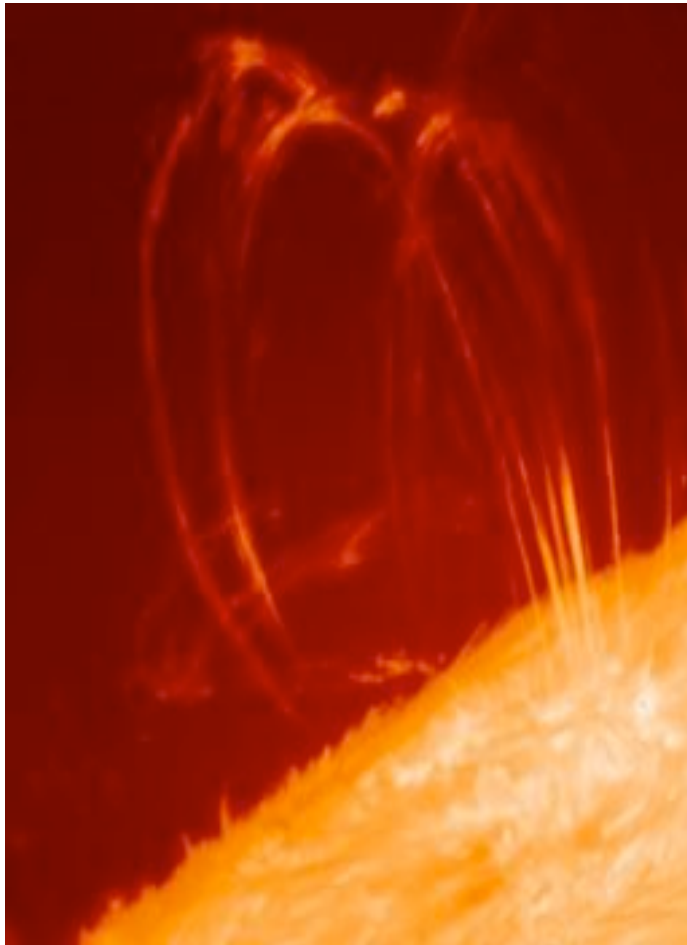


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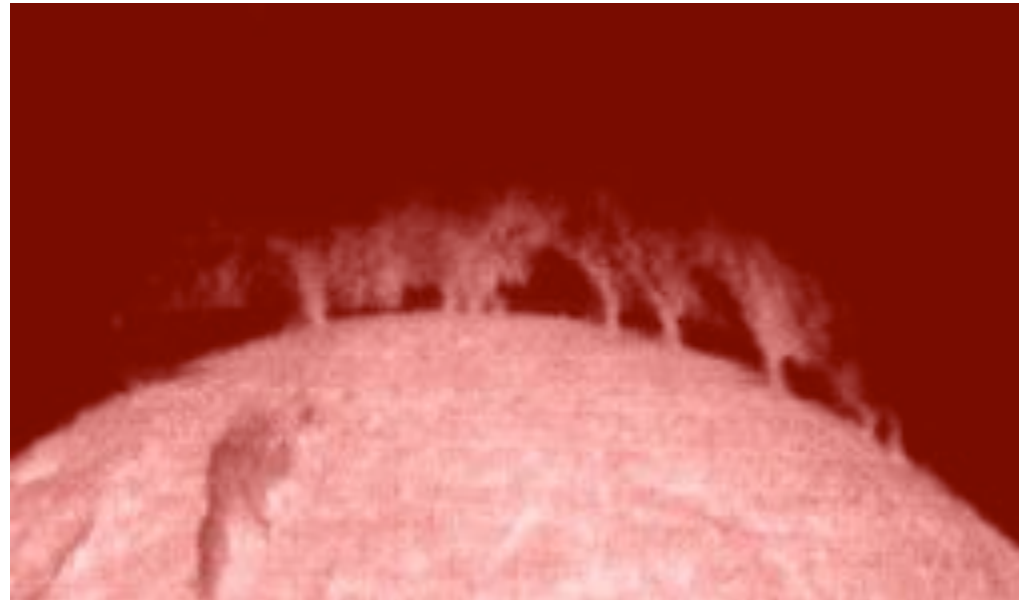
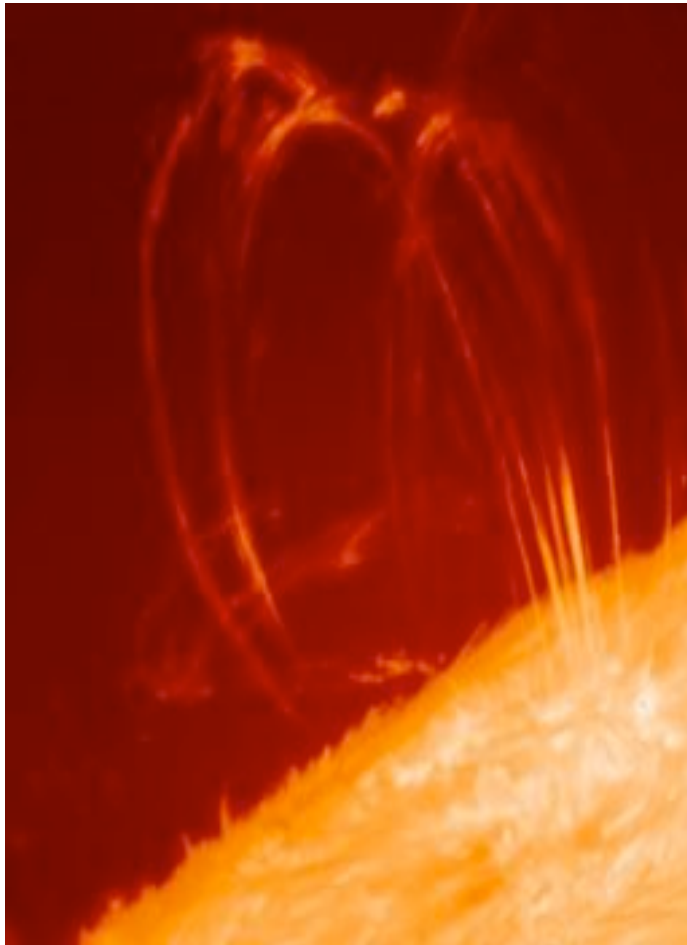


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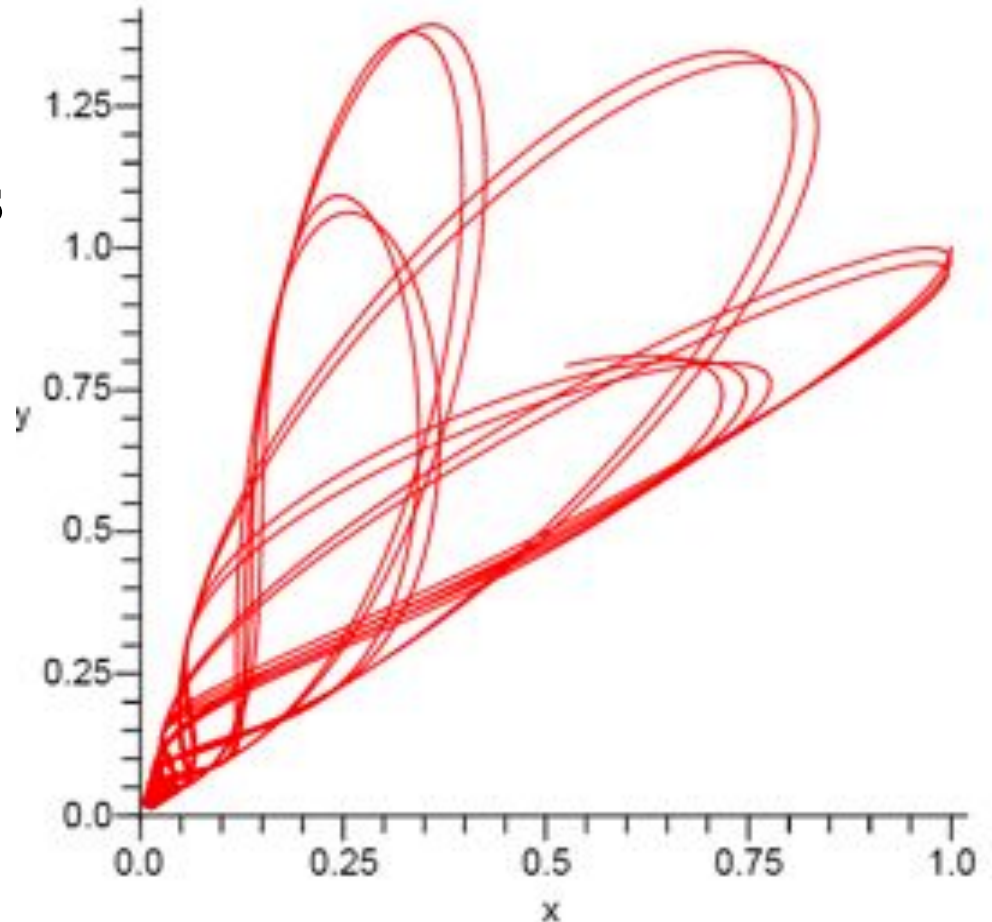


Let us however start with one monopole (dyon)+ one charge

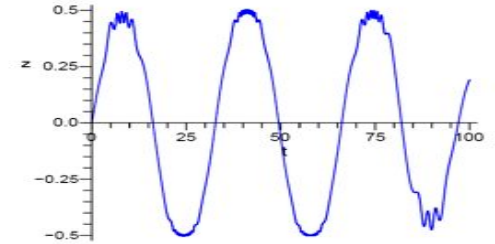
A.Poincare 110 years ago had explained that there is angular momentum of the field $\mathbf{J} \parallel \mathbf{r}$ and that the motion is restricted to a cone

Monopole repels from a charge

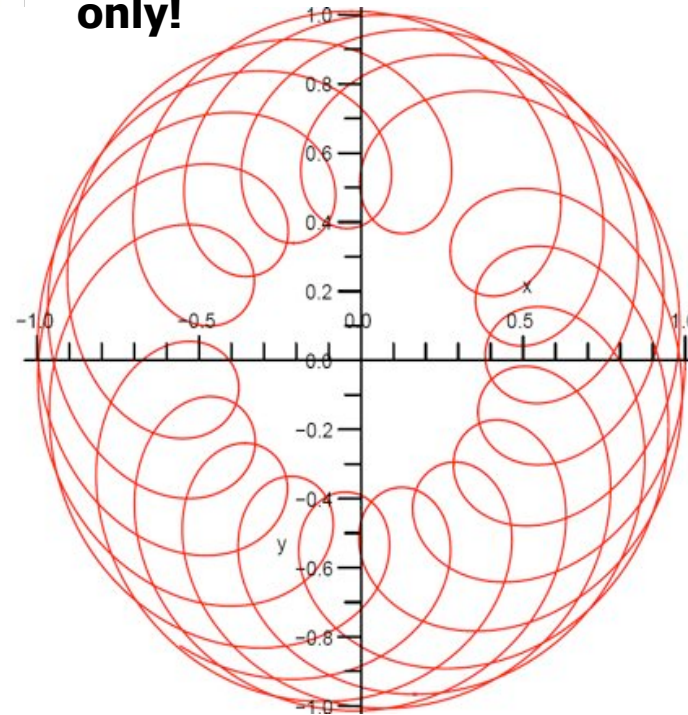
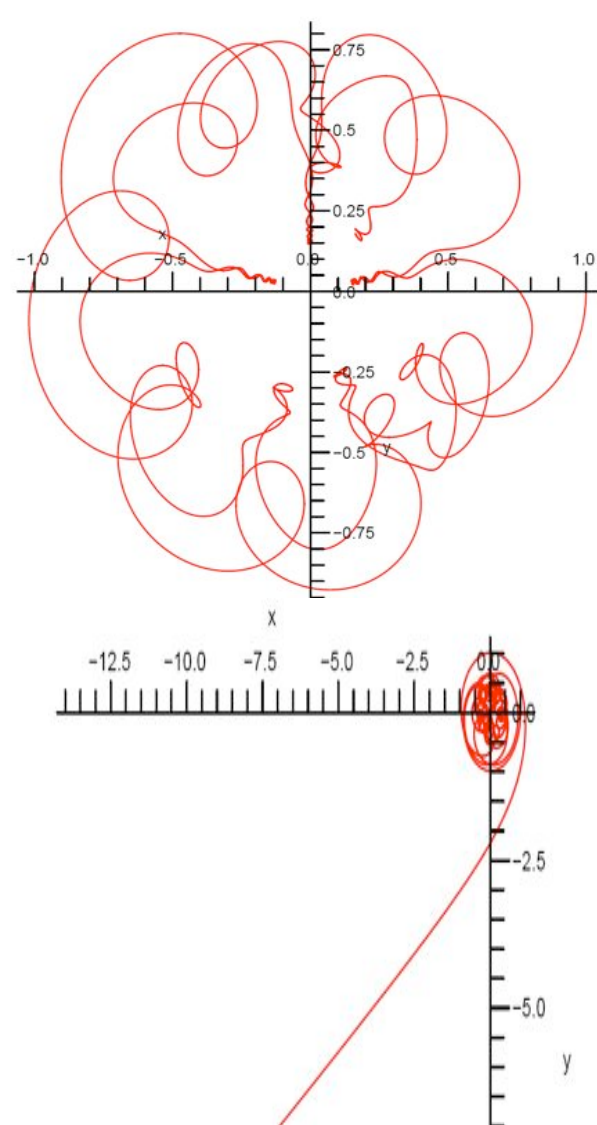
Here is my solution for a dyon with Attractive charge, preventing the escape to large r
Quantum system is like H atom...



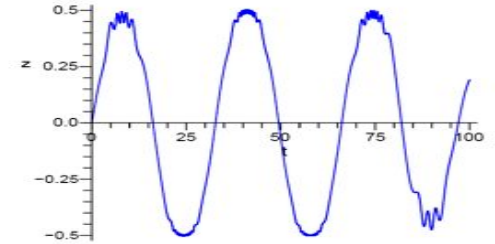
I found that **two charges** play ping-pong
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**Chaotic, regular
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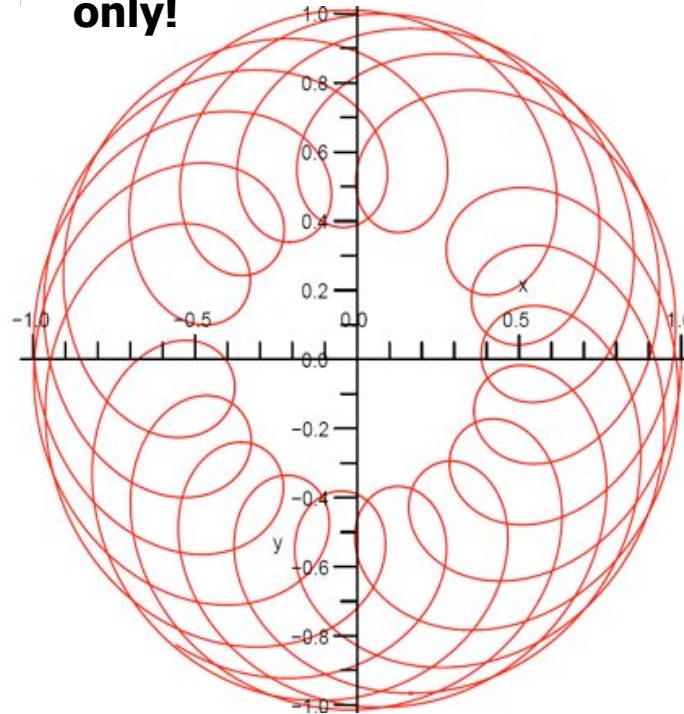
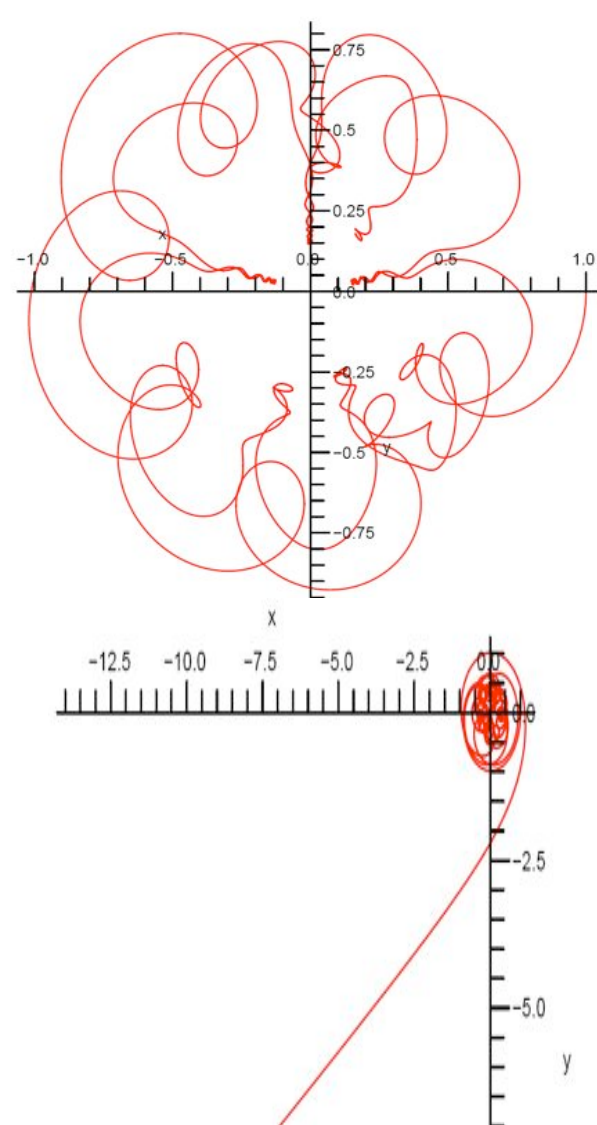


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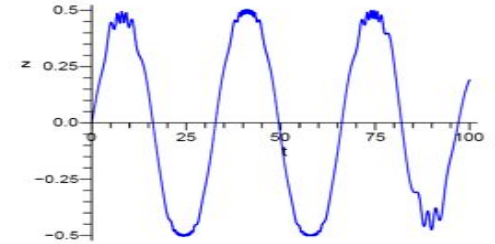


Dual to Budker's

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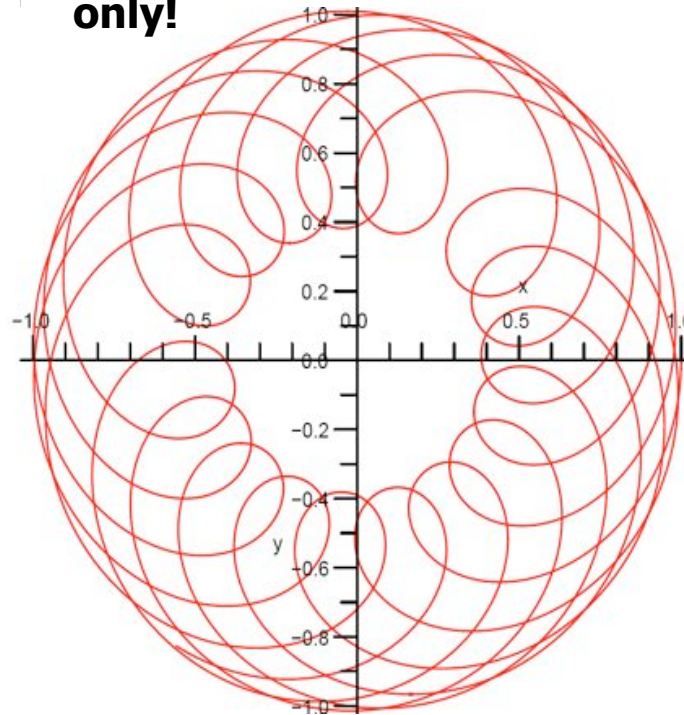
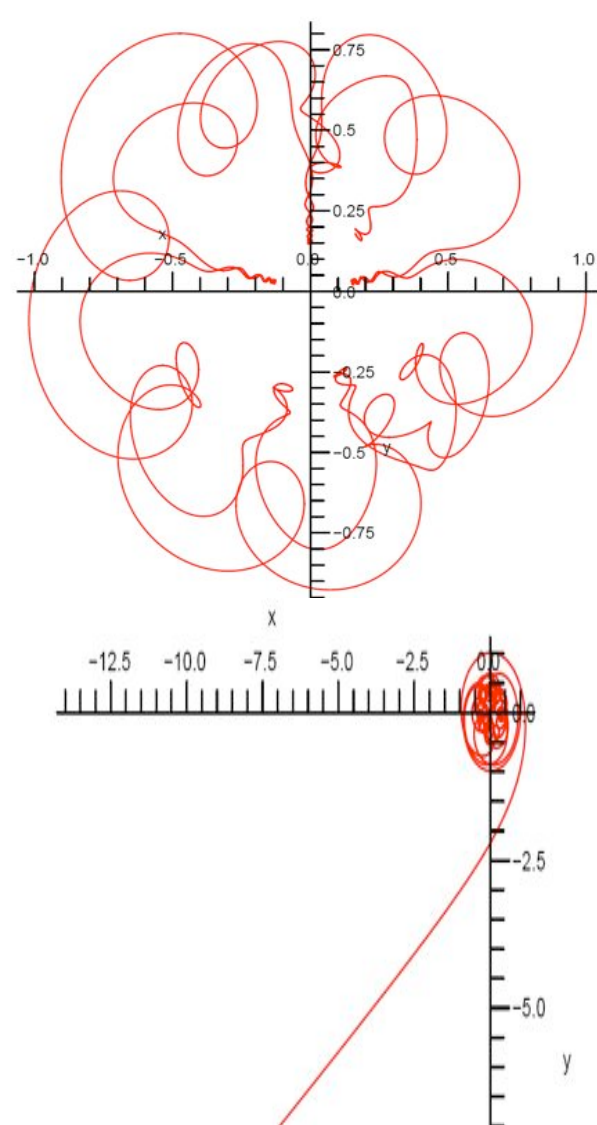


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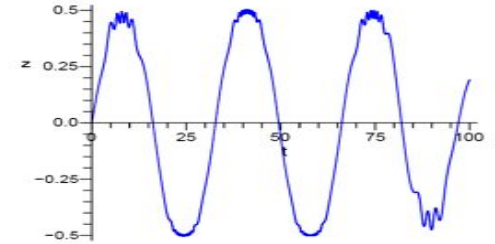
Dual to Budker's magnetic bottle

Chaotic, regular and escape trajectories for a monopole, all different in initial condition by 1/1000 only!

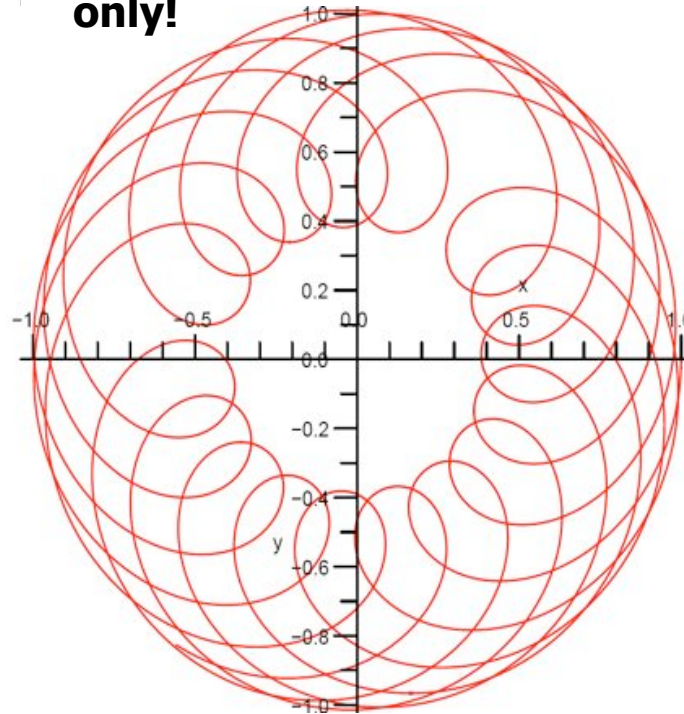
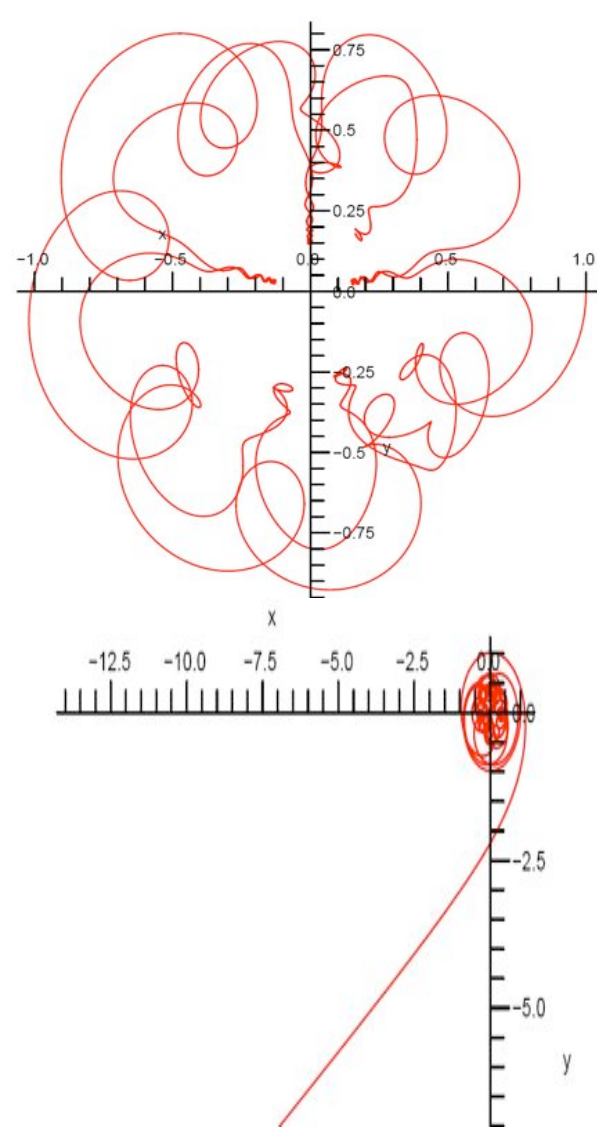
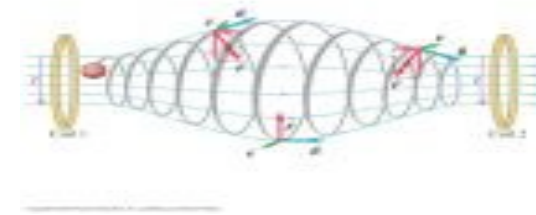


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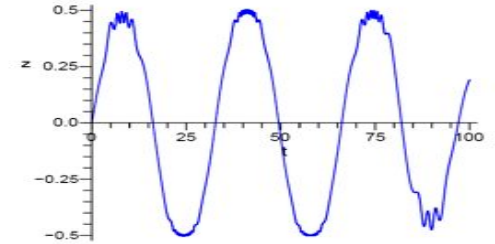


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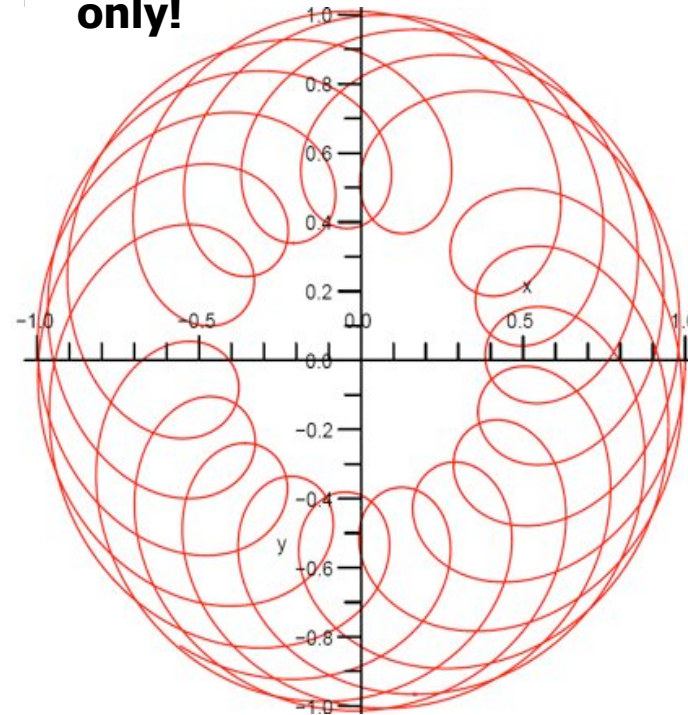
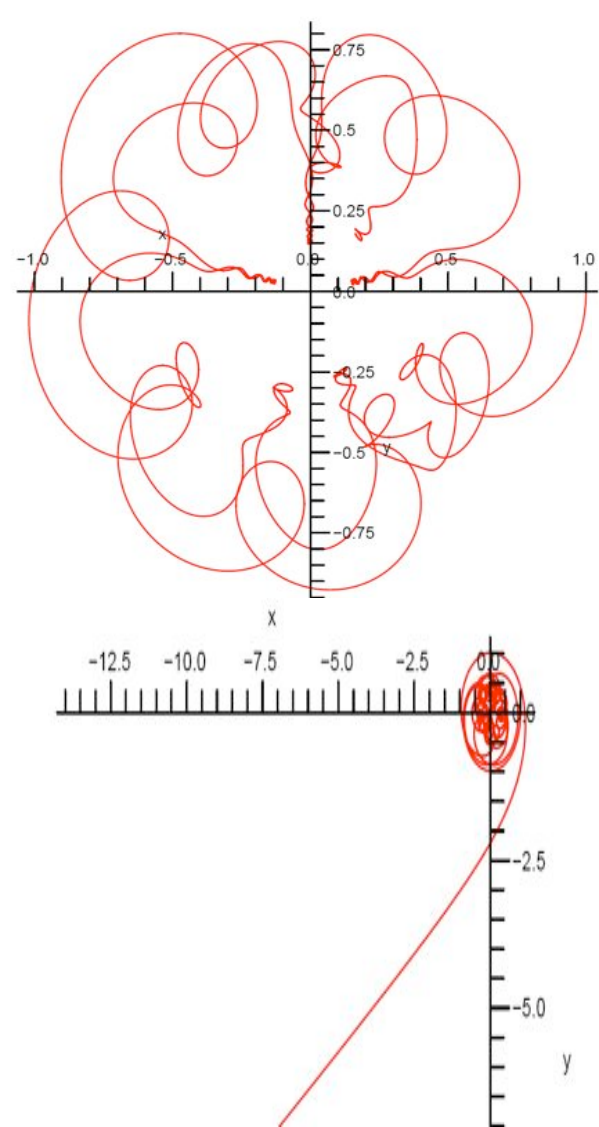
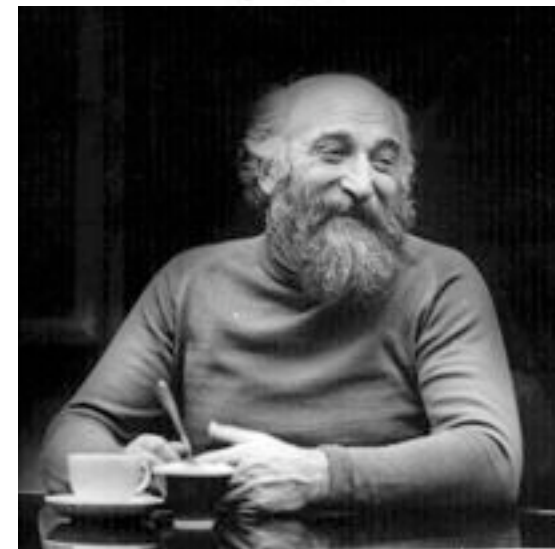
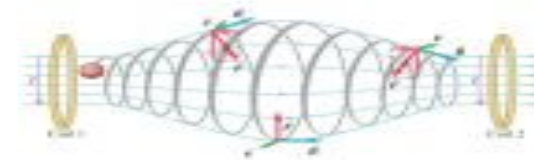


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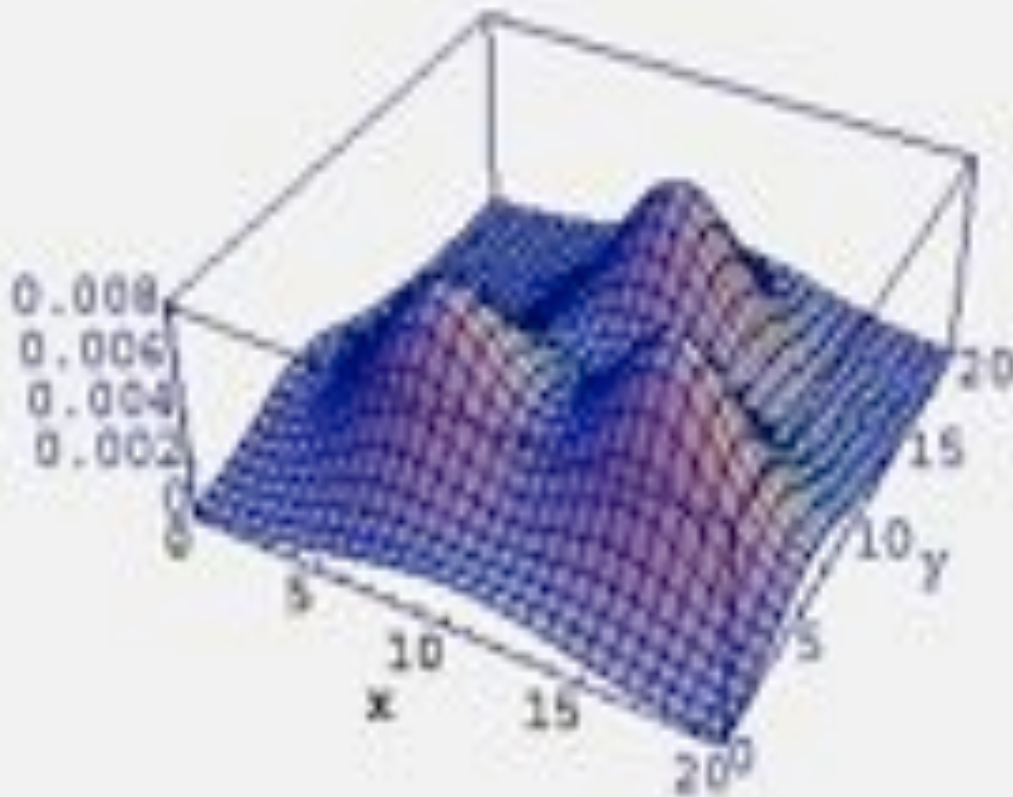
Can we see monopoles? How many are there at $T > T_c$?

Topology and fermionic zero modes helps

Caloron = baryon made of N_c dyons, can be seen in energy directly:

KvBLL solutions:

T. C. Kraan and P. van Baal, K. Lee and C. Lu [1998]



**Classical solutions
with the top. charge
 $Q=1$ and **nonzero
holonomy $\langle P \rangle$**
(A_0 or Higgs VeV)**

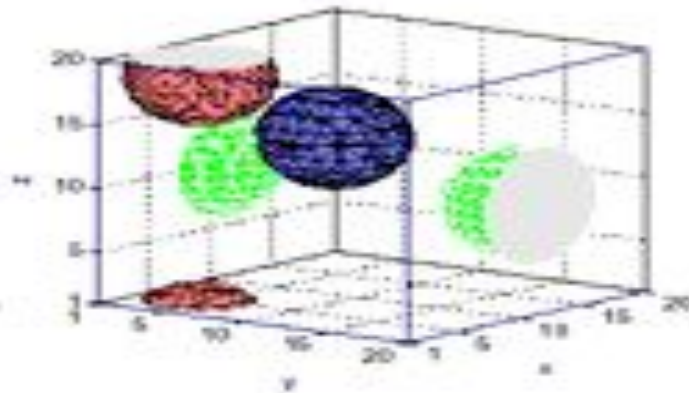
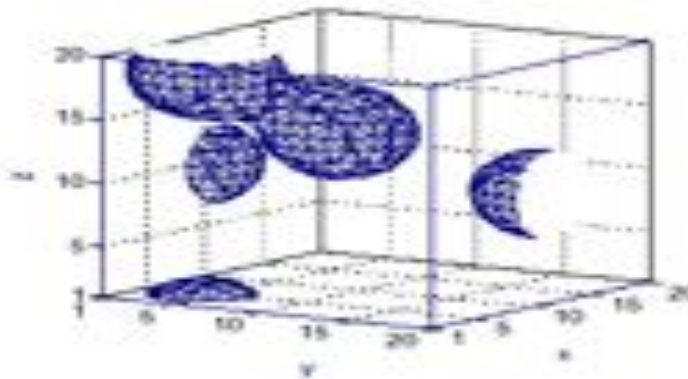
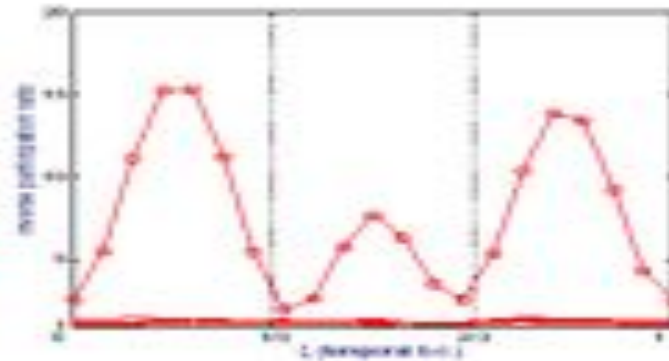
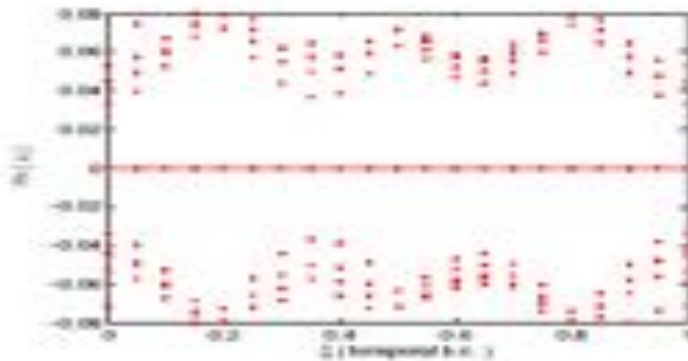
\Rightarrow

**(long suspected because there
are 4 N_c collective coordinates
and monopoles have 4)**

**Now it has nice Ads/CFT
brane derivation**

Such semiclassical self-dual dyons are even better seen in lattice configurations via fermionic zero modes

(From Ilgenfritz et al)



Non-trivial $Q = 1$ caloron : Spectral flow (upper left), IPR of zero-mode (breathing, upper right), action density (bottom left) and zero-mode density (bottom right), for three z 's corresponding to maximal localization.

A $SU(2)$ multicaloron ring with $Q = 3$ containing 6 dyons

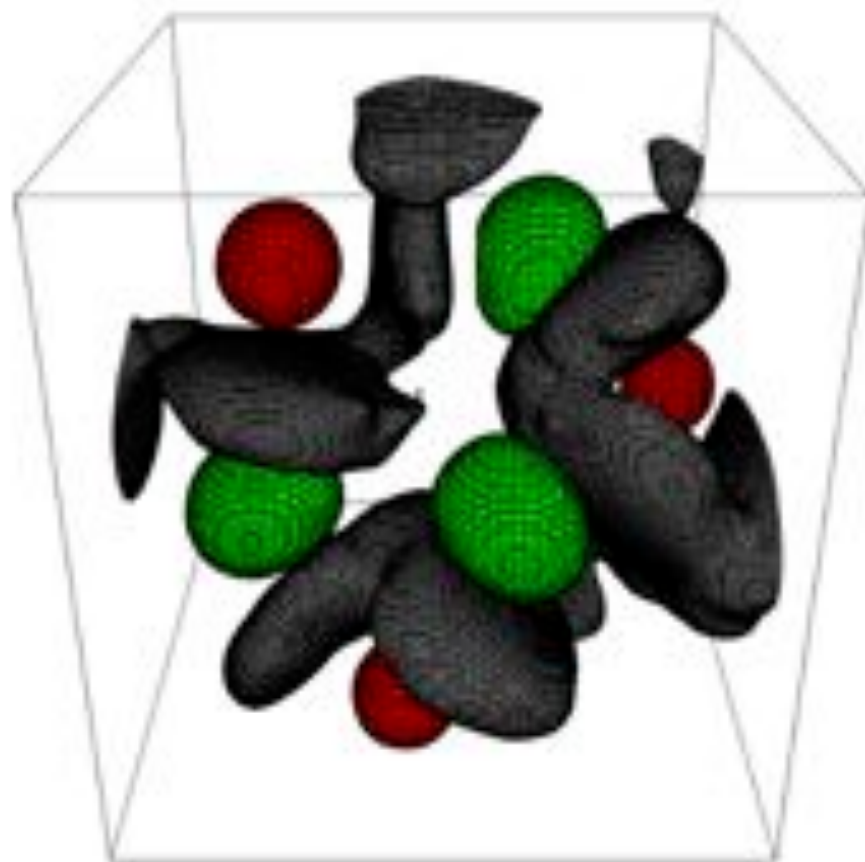


Figure 13: A $Q = 3$ caloron with non-trivial holonomy in $SU(2)$: Iso-surfaces of the Polyakov loop at positive (L dyons, red) and negative values (M dyons, green). Regions of non-staticity (in dark) are separating the L and M dyons (alternating along a multicaloron ring) from each other.

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 - **a strongly coupled liquid with local color and crystalline order can be studied in real time**

Additional slides