

# Toward the theory of **strongly coupled Quark-Gluon Plasma** (sQGP)

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# Outreach of the field is exponentially expanding...

- Why do we think we have **strongly coupled quark-gluon plasma (sQGP)** at  $T=(1-2)T_c$ ?  
(4 slides, a summary of main arguments)
- **Flows and near-perfect liquid**
- **classical strongly coupled non-Abelian plasma and its first molecular dynamics (MD)**
- **“New spectroscopy” at  $T > T_c$ : mesons, colored pairs, baryons, electric chains...**
- **Topology and “post-confinement”:** monopoles, instantons  $\Rightarrow N_c$  dyons  $\Rightarrow$  flux tubes  $\Rightarrow$  large potentials at  $T > T_c$ ? (connections to  $N=2$  SUSY YM)
- **Summary**
- (Comment: lessons from AdS/CFT with strongly coupled  $N=4$  theory are spread all over the talk)

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- 1c: **charm diffusion:  $D_c \ll$  pQCD also**  
(from  $R_{AA}, v_2$  of electrons at RHIC, Moore+Teaney, Molnar...)
- 1d: very strong **jet quenching, including charm**, again well beyond pQCD, no Casimir scaling...

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- 2d: **Polymeric “electric” chains of gluons**  $\bar{q} - g - g \dots q$

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- (3e: a **complete gravity dual to RHIC**, with black hole production => ES, Sin+Zahed, sorry no time on that)

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- Above  $T_c$  one gets to a point when **gluons and monopoles have comparable masses and couplings =>**
- **New conjecture: sQGP is a plasma of both electric and magnetic charges (to be studied)**

# Flows and transport properties at RHIC

# Magdeburg hemispheres 1656

(recall here  
pumped out  
Magdeburg  
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- **We cannot pump the QCD vacuum out, but we can pump in something else, namely the Quark-Gluon Plasma**
- **QGP proposed in 1970's was expected to be simple near-ideal gas.**

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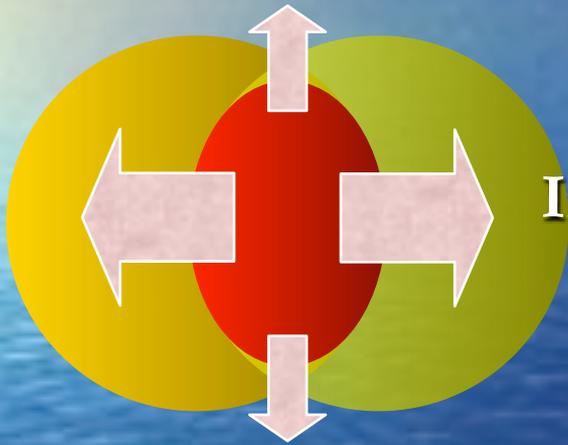
**But something else was on the way...**

**We believed if we increase the energy density, we should eventually get weakly interacting QGP. But something else was found on the way...**

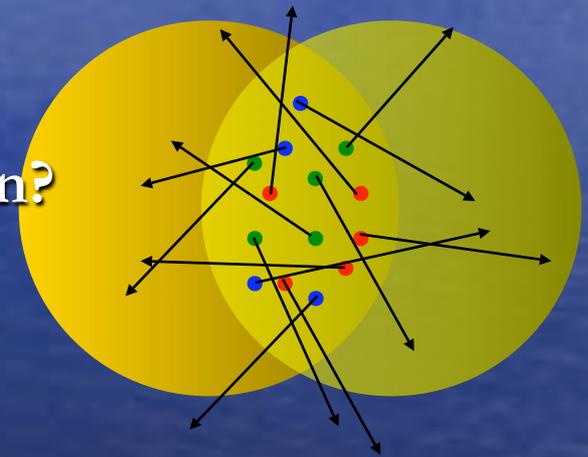
# How Hydrodynamics Works at RHIC

## Elliptic flow

How does the system respond to initial spatial anisotropy?

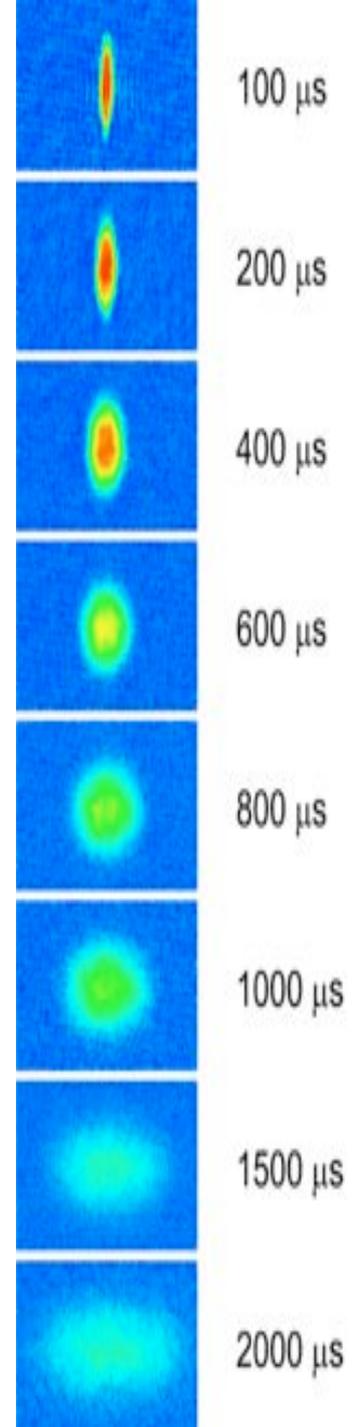


Dense or dilute?  
If dense, thermalization?  
If thermalized, EoS?

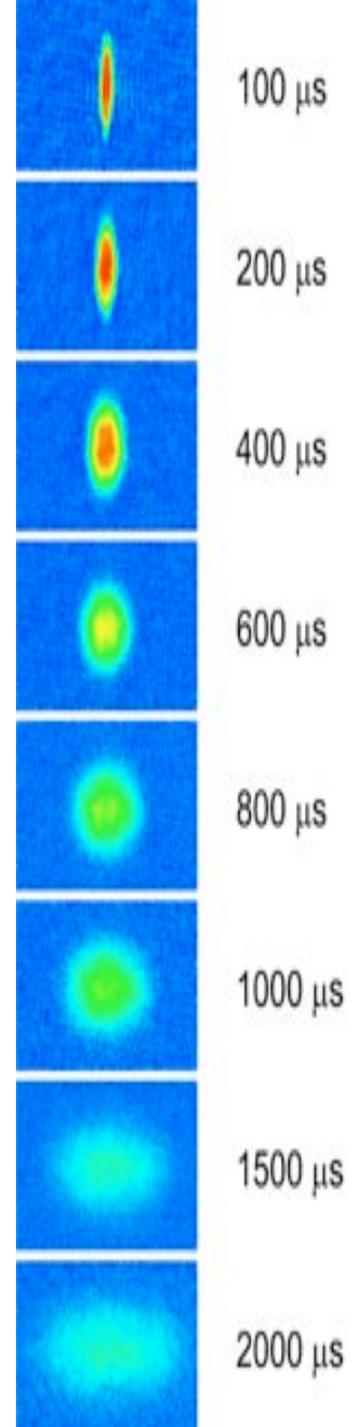


$$\frac{dN}{p_T dp_T dy d\phi} = \frac{1}{2\pi} \frac{dN}{p_T dp_T dy} (1 + 2v_1 \cos(\phi) + 2v_2 \cos(2\phi) + \dots)$$

$$v_2(p_T, y) = \frac{\int d\phi \cos(2\phi) \frac{dN}{p_T dp_T dy d\phi}}{\int d\phi \frac{dN}{p_T dp_T dy d\phi}} = \langle \cos(2\phi) \rangle$$



The coolest thing on Earth,  $T=10$  nK or  $10^{-12}$  eV can actually produce a **Micro-Bang !** (O'Hara et al, Duke )

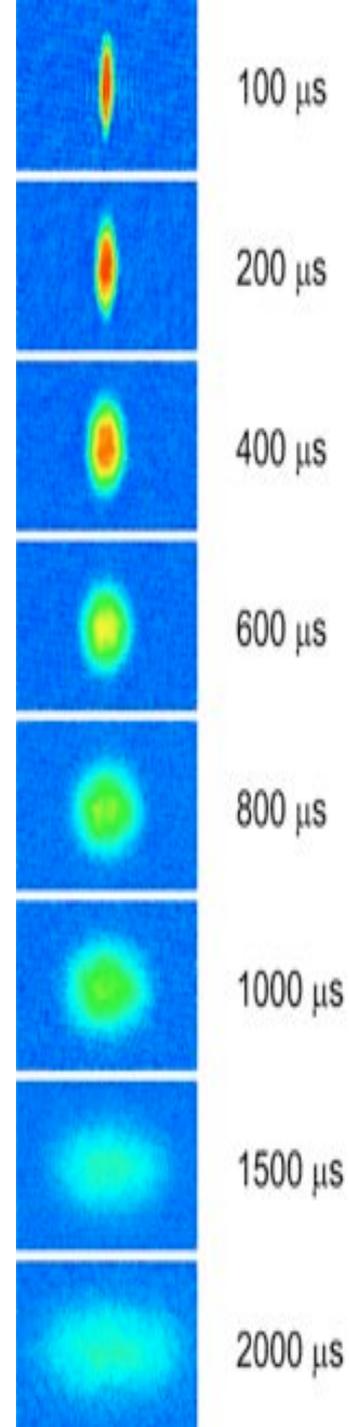


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**Elliptic flow with ultracold trapped Li6 atoms,  $a \Rightarrow$  infinity regime**

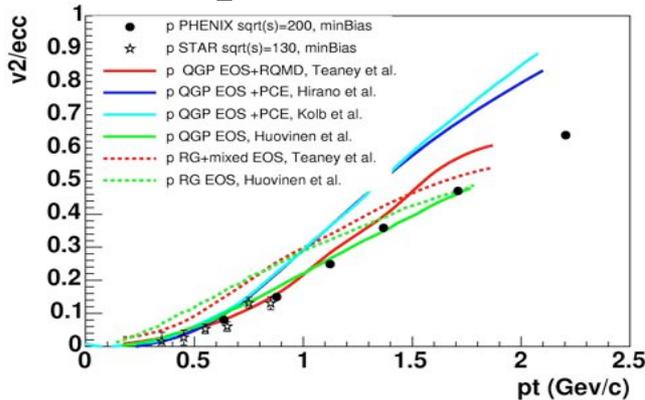
**The system is extremely dilute, but can be put into a hydro regime, with an **elliptic flow**, if it is specially tuned into a strong coupling regime via the so called Feshbach resonance**

**Similar mechanism was proposed (Zahed and myself) for QGP, in which a pair of quasiparticles is in resonance with their bound state at the "zero binding lines"**

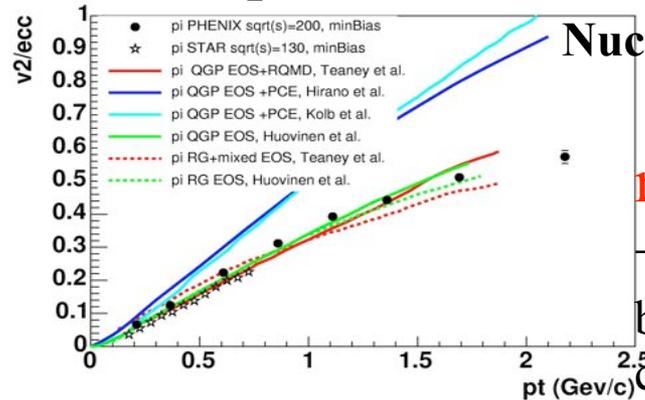


2001-2005: hydro describes radial and elliptic flows for **all secondaries** ,  $p_T < 2 \text{ GeV}$ , centralities, rapidities, A (Cu,Au)...  
 Experimentalists were very sceptical but were

proton



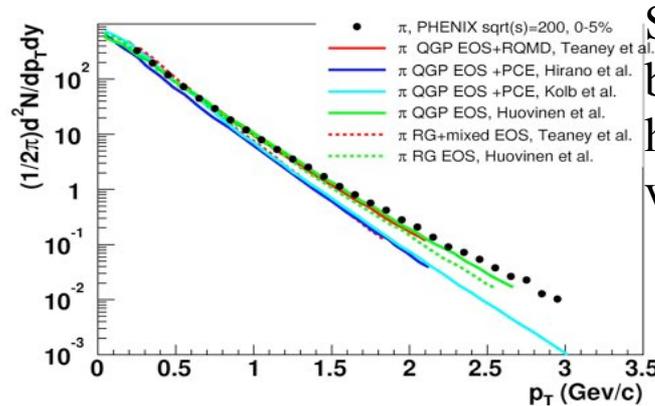
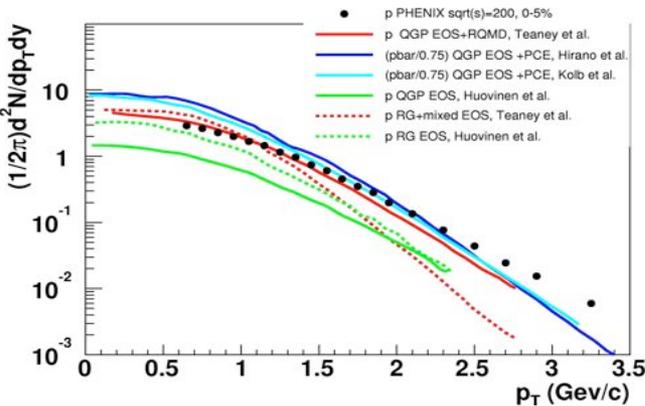
pion



PHENIX,

Nucl-ex/0410003

red lines are for ES +Lauret+Teaney done before RHIC data, never changed or fitted, describes SPS data as well! It does so because of the correct hadronic matter /freezeout via (RQMD)



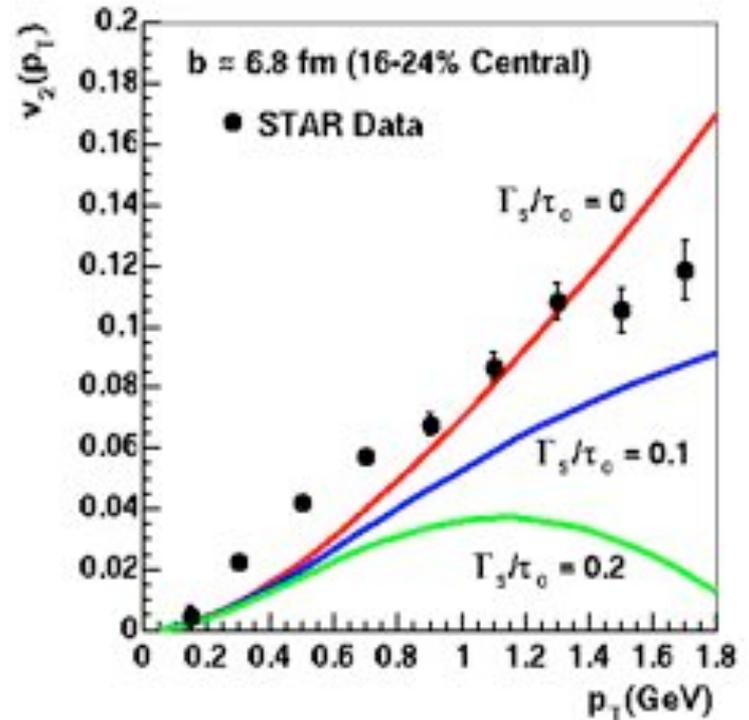
Viscosity reduces  $v_2$  and changes its  $p_t$  dependence:

QGP at RHIC seem to be the most ideal fluid known, viscosity/entropy = .1 or so  
~~water would not flow if only a drop with 1000 molecules be made~~

Correction  $\propto \frac{\eta}{s} p_t^2$

$\Rightarrow \eta/s \approx .1-.3$

( $1/4\pi \leq \text{AdS/CFT}$ )



# Sonic boom from quenched jets

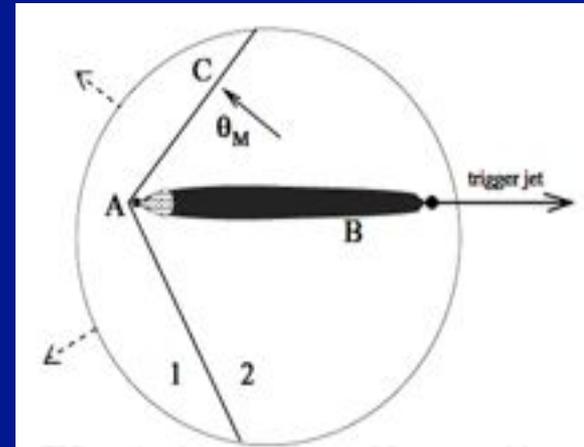
Casalderrey,ES,Teaney,

- the energy deposited by jets into liquid-like strongly coupled QGP must go into **conical shock waves**
- We solved relativistic hydrodynamics and got the flow picture
- If there are start and end points, there are two spheres and a cone tangent to both

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Wake effect or “sonic boom”

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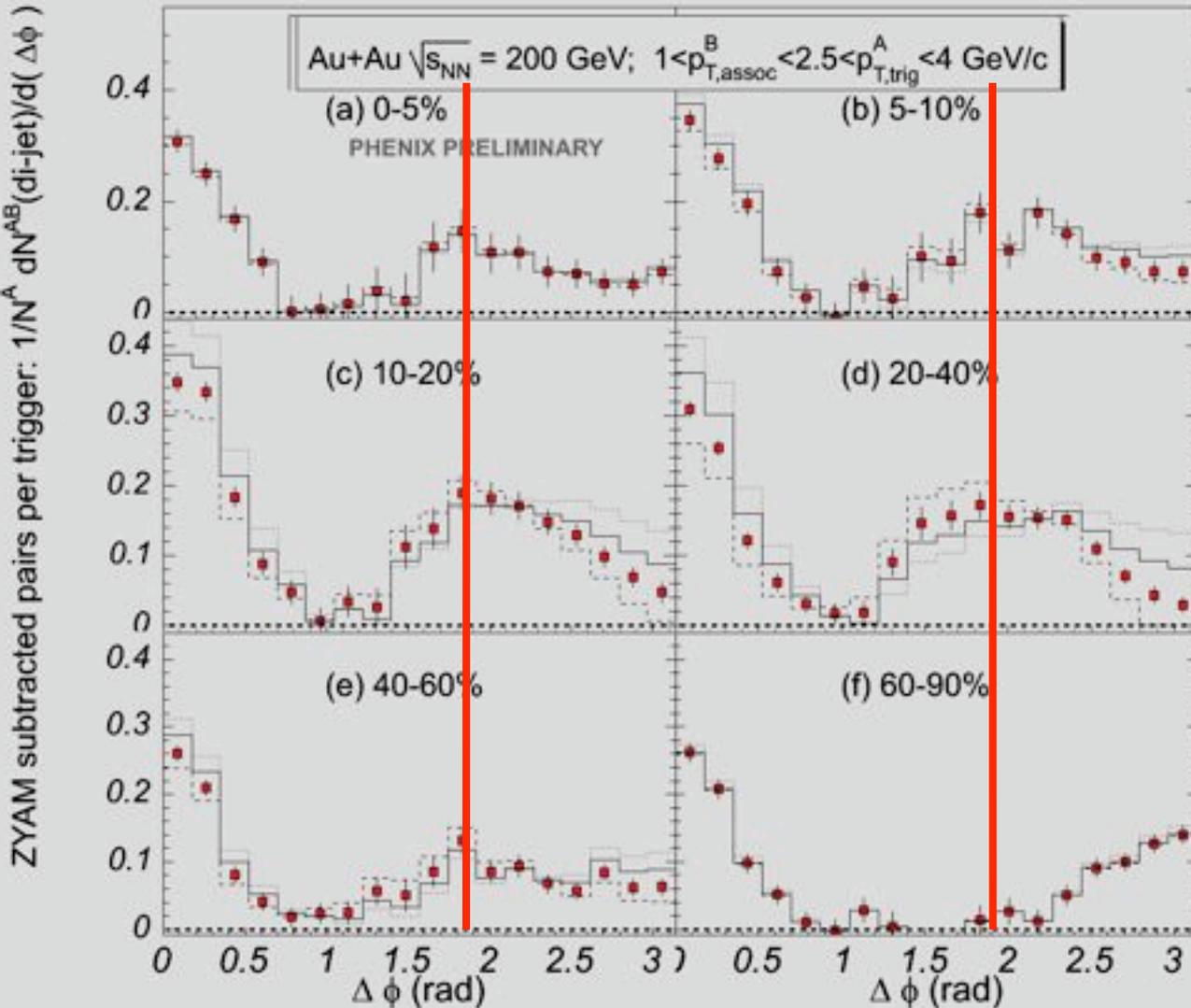


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# PHENIX jet pair distribution



**Note: it is only projection of a cone on phi**

**Note 2: more recent data from STAR find also a minimum in**

**$\langle p_t(\phi) \rangle$  at 180 degr., with a value**

**Consistent with background**

# Studies of a charge moving in sQGP at strong coupling (AdS/

- AdS/CFT allows to study a charge moving

With fixed velocity in a system:

A string pending and falling into the black hole

- L.Yaffe talk here, and also D.Teaney and J.Casalderrey found such solution at nonzero T calculating  $dE/dx$  (the drag force) , sonic boom etc

**Explaining transport in  
sQGP:**

**Classical QGP and its  
Molecular Dynamics**

**(B.Gelman,ES,I.Zahed,**

- For  $SU(2)$  charge  $Q$  is a unit vector,  $\vec{Q} = (Q^1, Q^2, Q^3)$

$$\begin{aligned} dx_i/dt &= p_i/m, \\ dp_i/dt &= (g^2/4\pi) \sum \vec{Q}_i \cdot \vec{Q}_j / r_{ij}^2, \\ d\vec{Q}_i/dt &= (g^2/4\pi) \sum \vec{Q}_i \times \vec{Q}_j / |r_{ij}| \end{aligned}$$

- Note:  $d\vec{Q}_i^2/dt = 0$

**Wong eqn** can be rewritten as

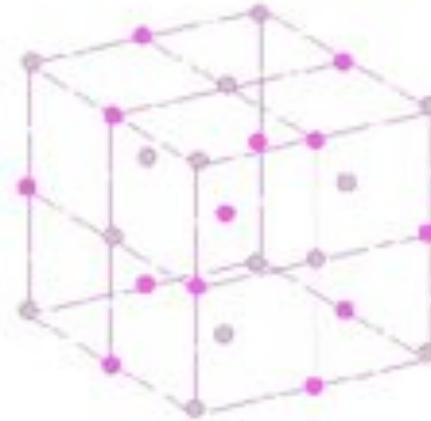
**x-p canonical pairs, 1 pair for  $SU(2)$ , 3 for  $SU(3)$ ,**  
**( as a so called Darboux variables).**

**We do  $su(2) \Rightarrow C$  is a unit vector on a sphere  $O(3)$**

As  $\Gamma = \langle |E_{\text{pot}}| \rangle / \langle E_{\text{kin}} \rangle$  grows  
gas  $\Rightarrow$  liquid  $\Rightarrow$  solid

- This is of course for +/- Abelian charges,
- But “green” and “anti-green” quarks do the same!

NaCl Structure

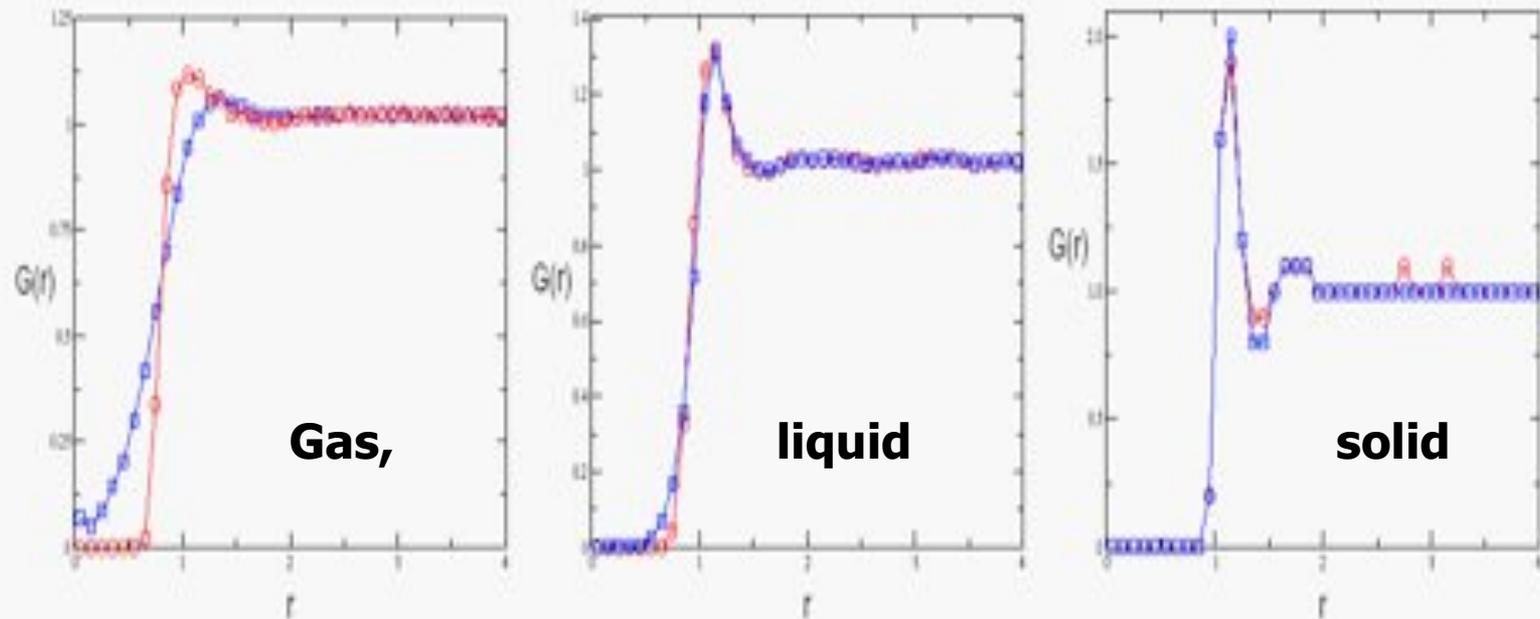


NaCl Structure with  
Face Centered Cubic Bravais Lattice



• local order would be preserved in a liquid also,  
as it is in molten salts (strongly coupled TCP with  
 $\langle \text{pot} \rangle / \langle \text{kin} \rangle = O(60)$ , about 3-10 in sQGP)

## Structure factor for cQGP



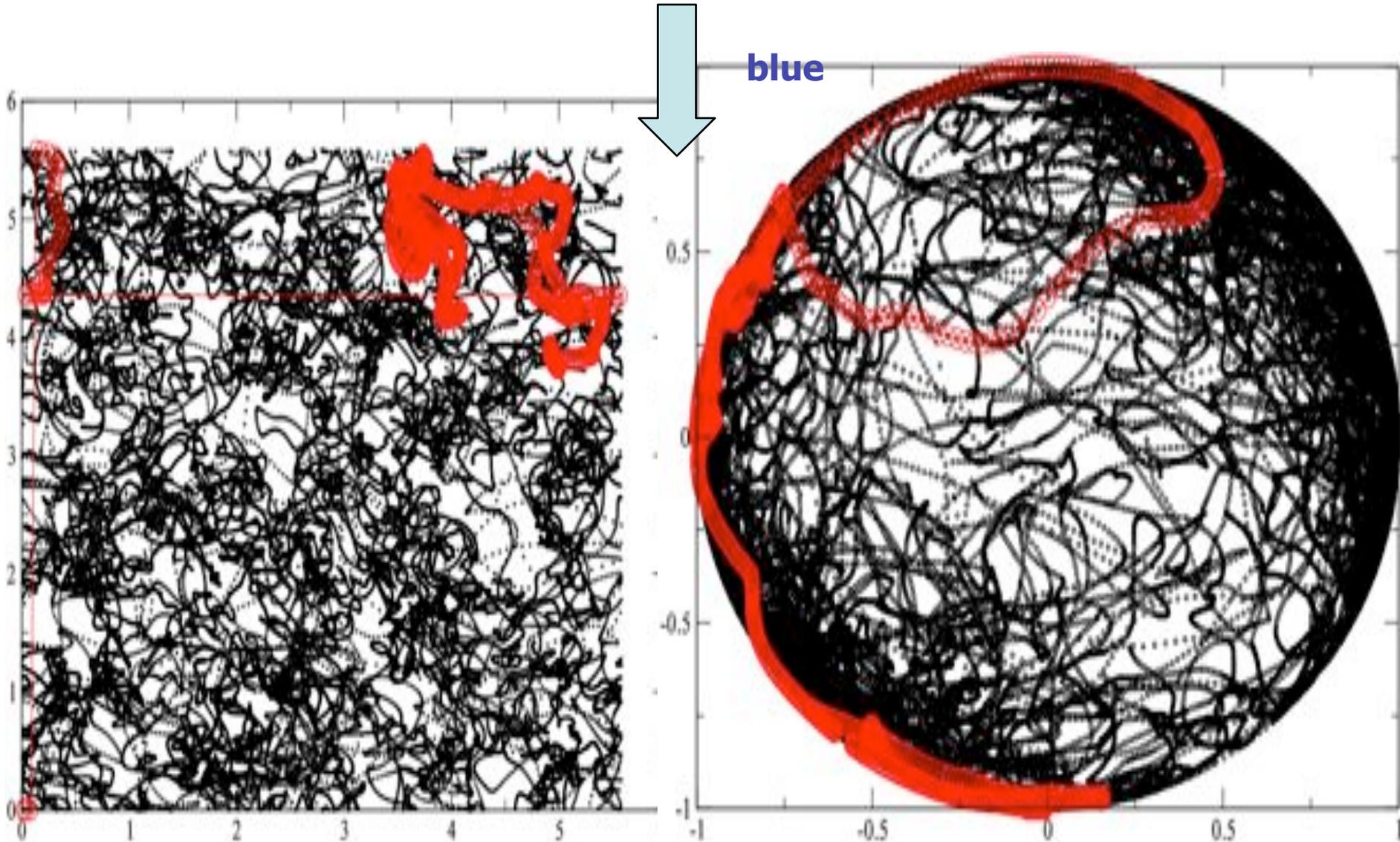
- $G_d$  correlation function for  $\Gamma = 0.83, 31.3, 131$ , respectively; red circles correspond to  $t^* = 0$ , and blue squares correspond to  $t^* = 6$
- $\Gamma = 0.83$  is a weak correlation between the particles; relaxes rather quickly with time
- The correlation is more robust for  $\Gamma = 31.3$  (*liquid*)
- For  $\Gamma = 131$  correlation is very stable (*solid*)

**cQGP made of 64 colored particles,  
projection of a cube on x-y plane,  
red is the path of particle #1.**

**strong coupling,  
Gamma is about 100  
close to freezing**

**Color -> red**

**blue**

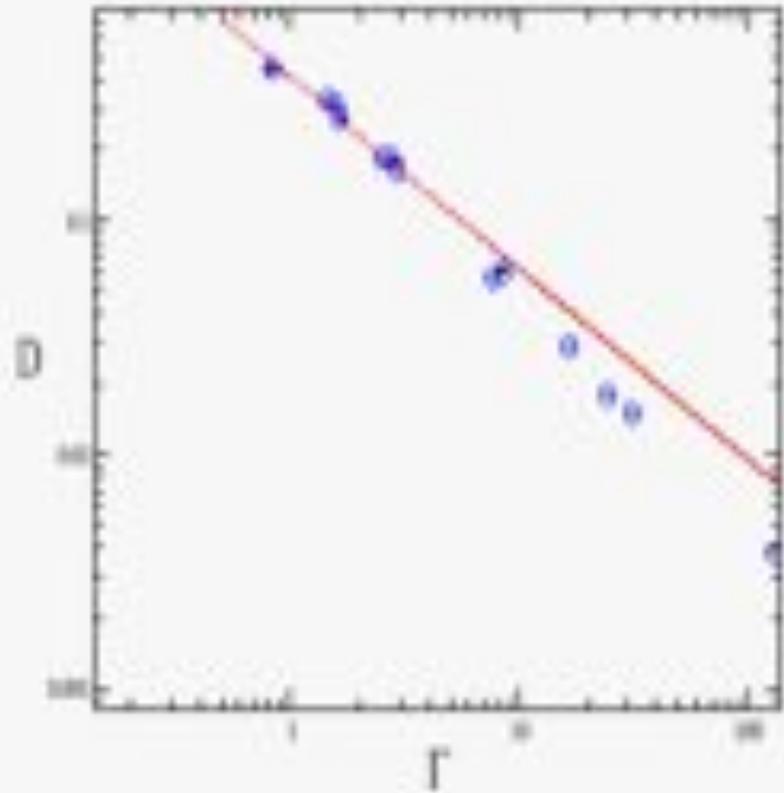


# Self-diffusion

$$D(\tau) = \frac{1}{3N} \left\langle \sum_{i=1}^N \vec{v}_i(\tau) \cdot \vec{v}_i(0) \right\rangle$$

$$D = \int_0^{\infty} D(\tau) d\tau$$

$$D \approx \frac{0.4}{\Gamma^{4/5}}$$



# Shear viscosity

- Green-Kubo relation for viscosity

$$\eta = \int_0^{\infty} \eta(\tau) d\tau$$

$$\eta(\tau) = \frac{1}{3TV} \left\langle \sum_{x < y} \sigma_{xy}(\tau) \sigma_{xy}(0) \right\rangle$$

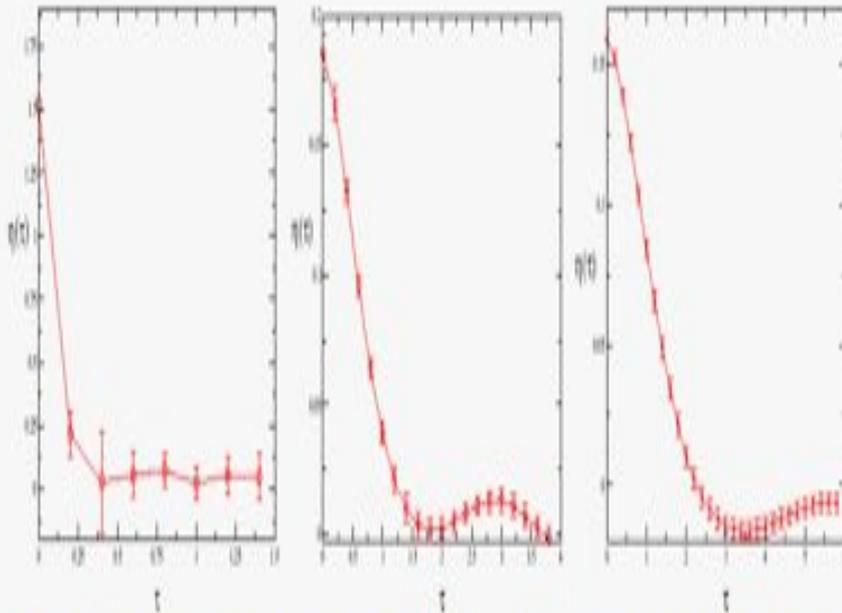
$\sum_{x < y}$ —a sum over the three pairs of distinct tensor components ( $xy$ ,  $yz$  and  $zx$ ); the stress-energy tensor are given by

$$\sigma_{xy} = \sum_{i=1}^N m_i v_{ix} v_{iy} + \frac{1}{2} \sum_{i \neq j} r_{ij,x} F_{ij,y}$$

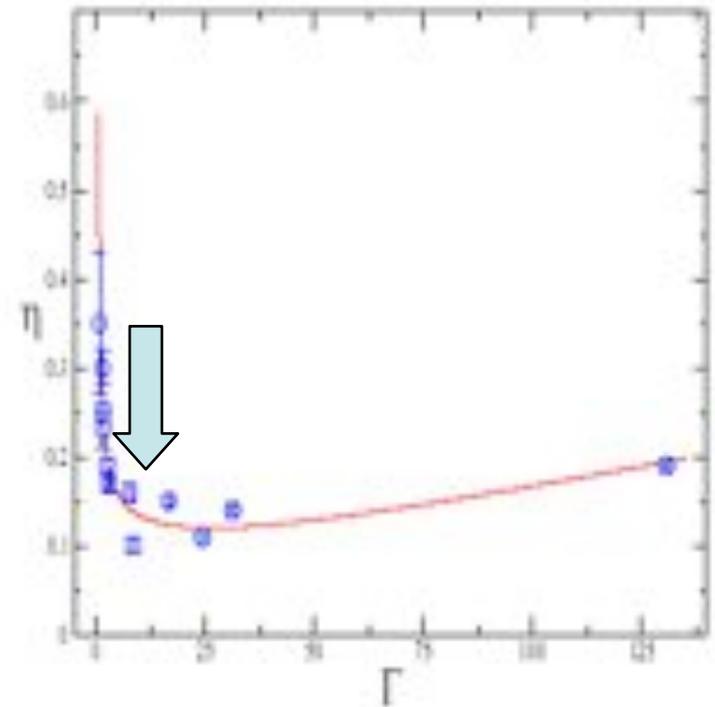
$\vec{F}_{ij}$  is the force on particle  $i$  due to particle  $j$

# First results on viscosity:

QGP (blue arrow) is about the best liquid one can possibly make



• Stress-tensor autocorrelation correlation function  $\eta(t)$  for  $\Gamma \equiv$   
0.83, 31.3, 131



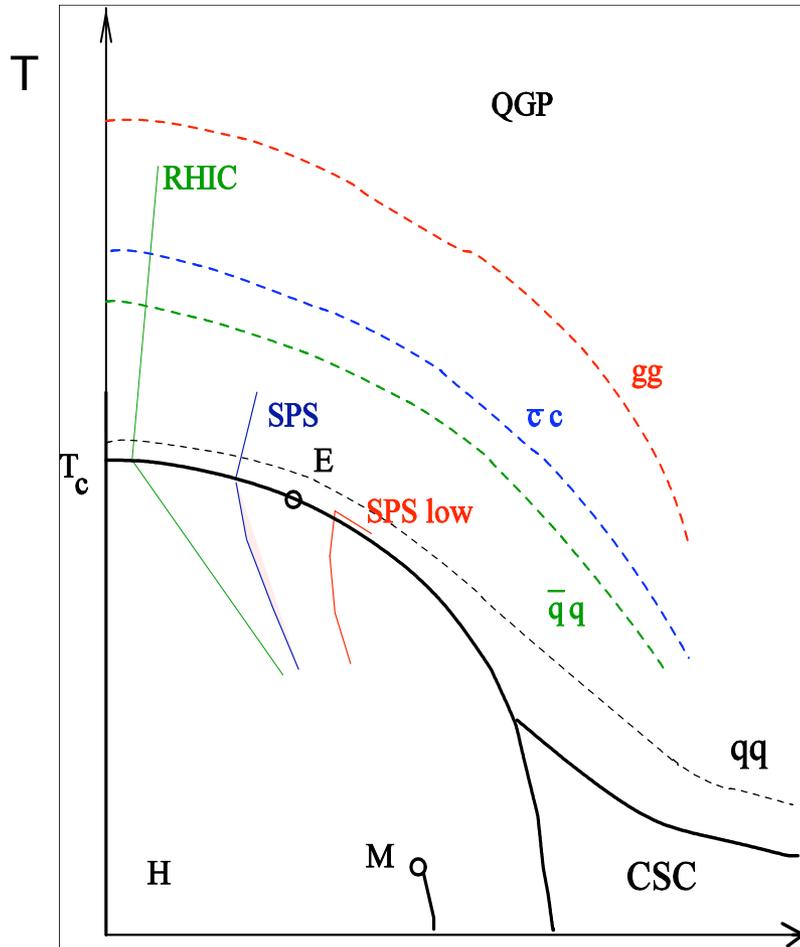
$$\eta \approx 0.001 \Gamma + \frac{0.242}{\Gamma^{0.3}} + \frac{0.072}{\Gamma^2}$$

# “New spectroscopy” in sQGP

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# 2003: Can mesons survive deconfinement?

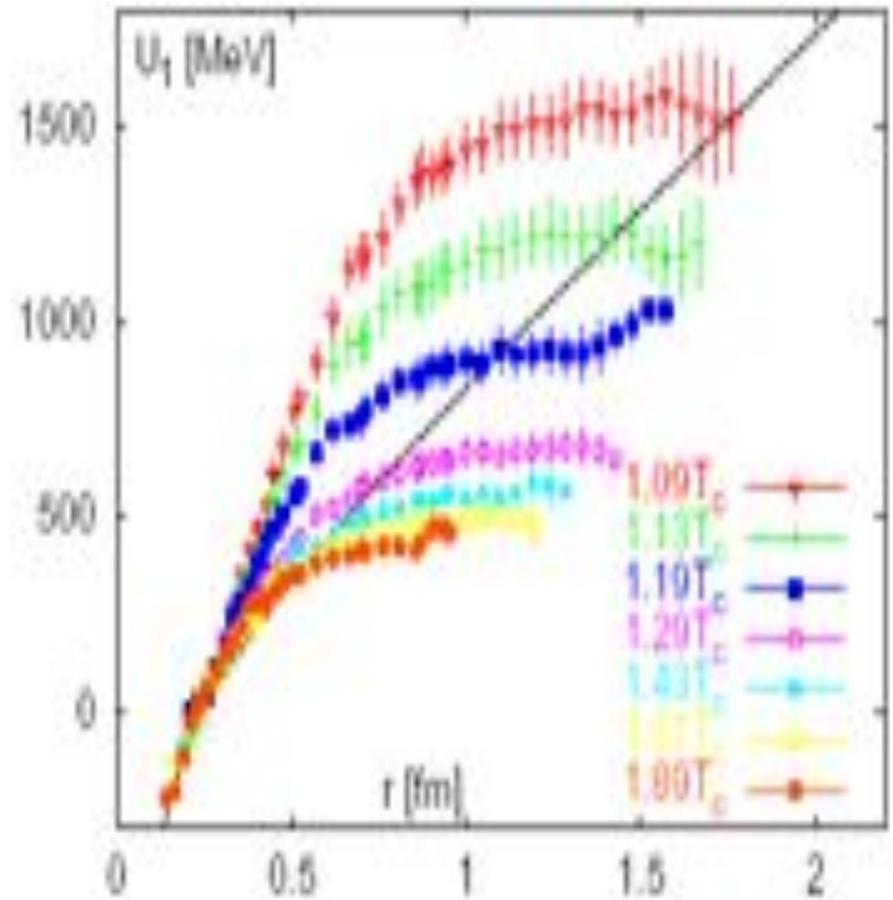
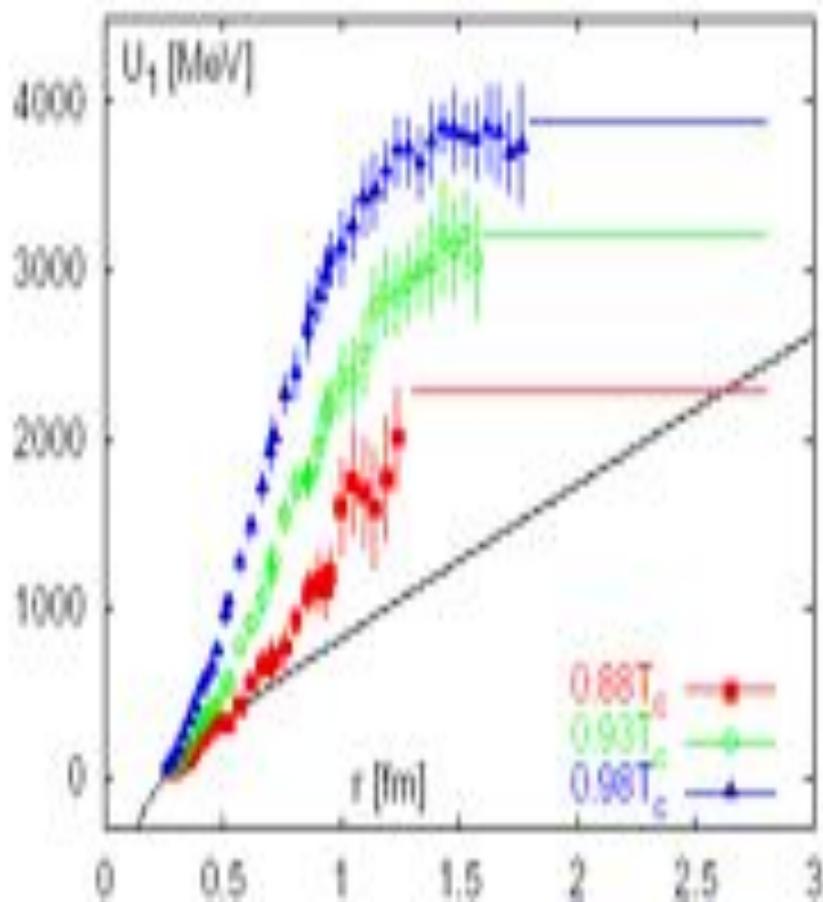


Chemical potential  
 $\mu$

Can resonance scattering help explain small m.f.p.? (It does for atoms)

Are regions of **meson binding** the divider between wQGP and sQGP? (ES+I.Zahed, "rethinking" paper PRC 2003, the beginning of sQGP...):

“Postconfinement”  
potential energy of a static dipole  
at  $T=(1-2)T_c$  and  $r=.5-1$  fm is even larger



# Solving for the bound states

## ES+I.Zahed, hep-ph/0403127

- **Charmonium remains bound till  $2T_c \Rightarrow$  confirmed by lattice correlators and now by direct RHIC J/Psi data**
- **In QGP there is no confinement  $\Rightarrow$  Hundreds of colored channels SHOULD have bound states as well**

channel	rep.	charge factor	no. of states
$gg$	1	9/4	$9_s$
$gg$	8	9/8	$9_s * 16$
$qg + \bar{q}g$	3	9/8	$3_c * 6_s * 2 * N_f$
$qg + \bar{q}g$	6	3/8	$6_c * 6_s * 2 * N_f$
$\bar{q}q$	1	1	$8_s * N_f^2$
$qq + \bar{q}\bar{q}$	3	1/2	$4_s * 3_c * 2 * N_f^2$

the strongest

The usual

weak

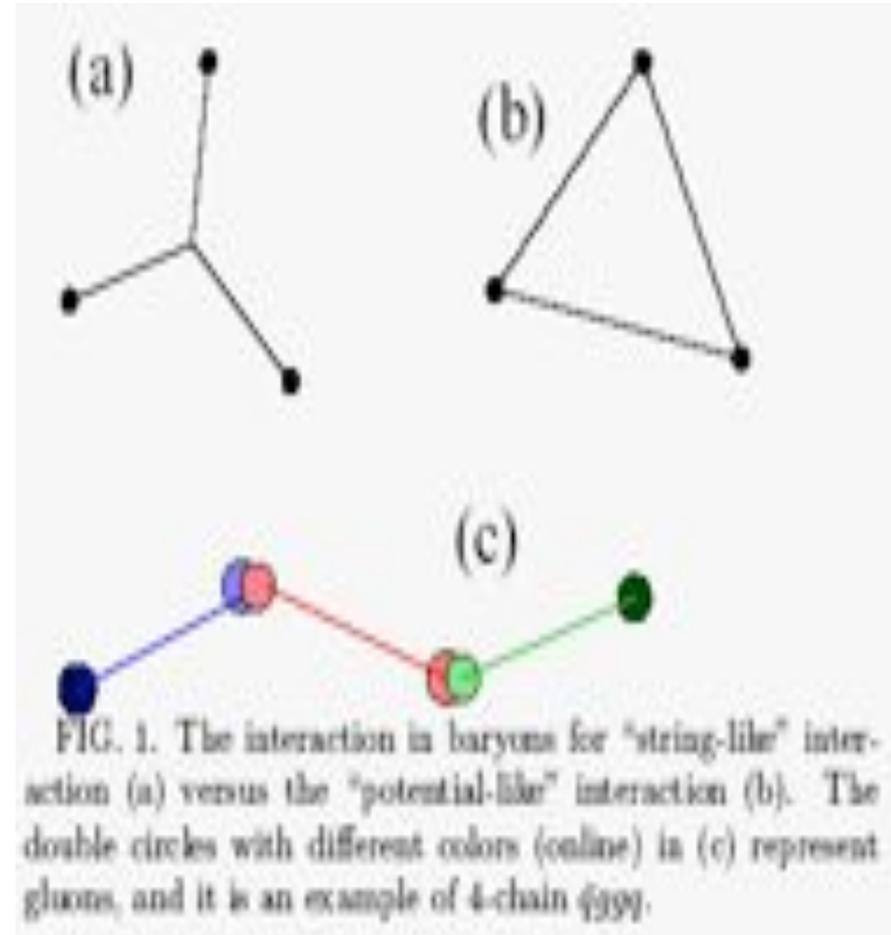
•  $gg$  color  $8*8=64=27+2*10+2*8+1$ : only the 2 color octets  $(gg)_8$  have  $(16*3_s * 3_s = 144)$  states.

# Baryons at $T > T_c$ ? Polymer chains?

J.Liao+ES,05

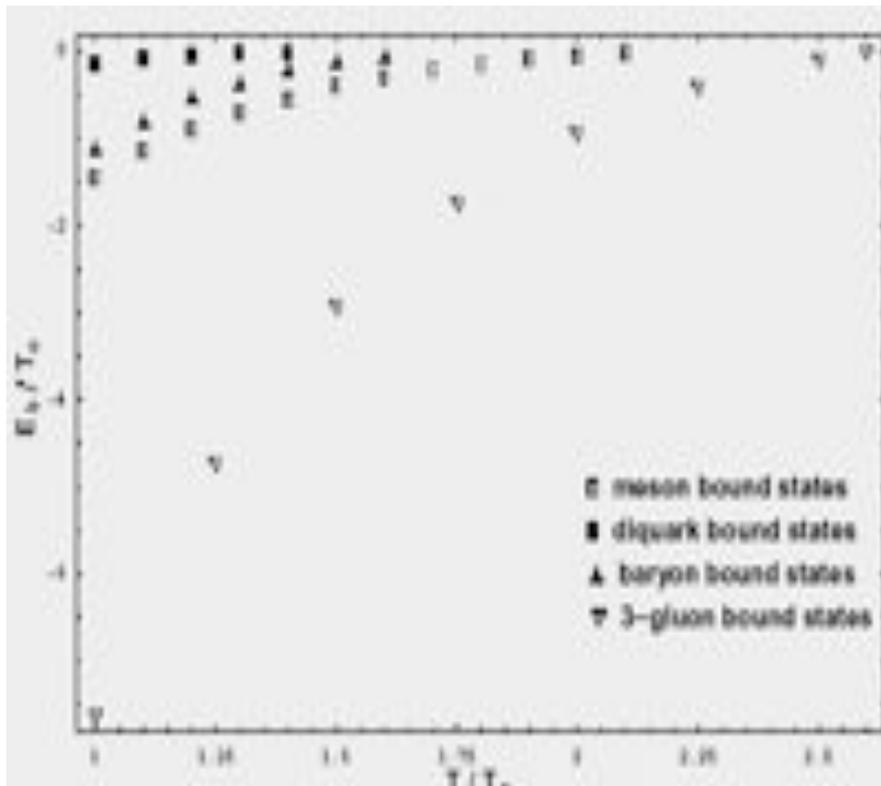
- Lattice favors “potential-like” (b) behavior of the potentials for baryons.
- $(a) = V(1j) + V(2j) + V(3j)$   
(j=junction)
- $(b) = (V(12) + V(13) + V(23))(1/2)$   
Casimir
- Fortunately  $\langle V \rangle(a)$  and  $\langle V \rangle(b)$  do not differ by more than 15%!

- **polymeric chains**  
 $\bar{q} g \dots g q$ , with color indices convoluted as writte



# Bindings from variational calculation for baryons and ggg chain (J.Liao+ES, 05)

electric chains have the same binding as mesons per link



structure	-body	$G$	$E_b$ at $T_c$	$T_m$
$\bar{q}q$	2	1	-1.45	2.1
$\bar{q}g \cdots gq$ (polymer chain)	$N$	1	$-1.45 \cdot (N-1)$	2.1
$ggg$ (closed chain)	3	1	-7.64	2.6
$qq$	2	1/2	-0.13	1.4
$qqq$ (close chain)	3	1/2	-1.10	1.6

# Polymeric chains in strongly coupled Higgsed $N=4$ (J.Minahan 98)

$N_c$  branes are put not at the same point, but say 2 lumps  $N_c/2$  +  $N_c/2 \Rightarrow$

Massive gluons

String solutions with a string oscillating between the lumps

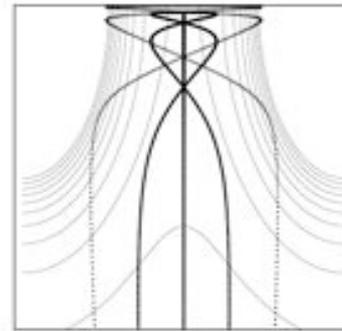


Fig. 2: Geodesics with six half oscillations. As  $L$  is increased, the geodesic approaches the concatenation of the BPS geodesics of two quarks and a five  $W$ s.

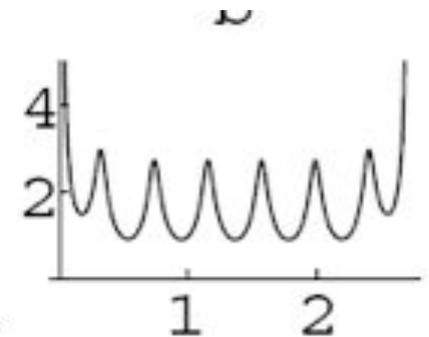
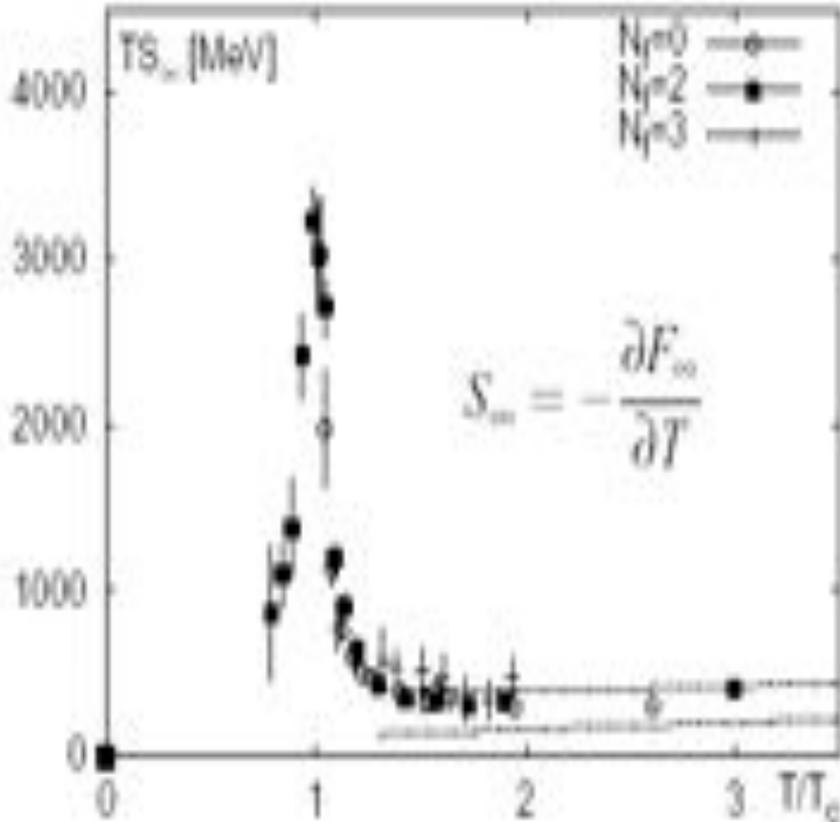


Fig. 3: Plot of  $E$  vs.  $L$  for the saddle branch and the first three coulomb branches.  $E$  is plotted in units of the  $W$  mass,  $m_W$ , and  $L$  is in units of  $R^2/m_W$ . The first and third branches are doubly degenerate. The second branch is a  $\mathbb{Z}_2$  symmetric branch.

# Entropy associated with a static dipole gets huge! (shown at large $r$ vs $T/T_c$ )



- **S/charge = 0(10)**
- **#(states) = exp(10)**
- **What those states may be?**
- **string picture**  
(Polyakov 78 =>  
Klebanov, Maldacena, Thorn et al hep-th/0602255)
- **electric polymers (Liao, ES 05 ... Ads/CFT Minahan 98)**
- **trapped monopoles?**

# Postconfinement and monopoles at $T > T_c$

# monopoles in QGP

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- Dual superconductivity as a confinement mechanism ('tHooft, Mandelstam 1980's) require monopole condensation (nonzero VEV)

# monopoles in QGP

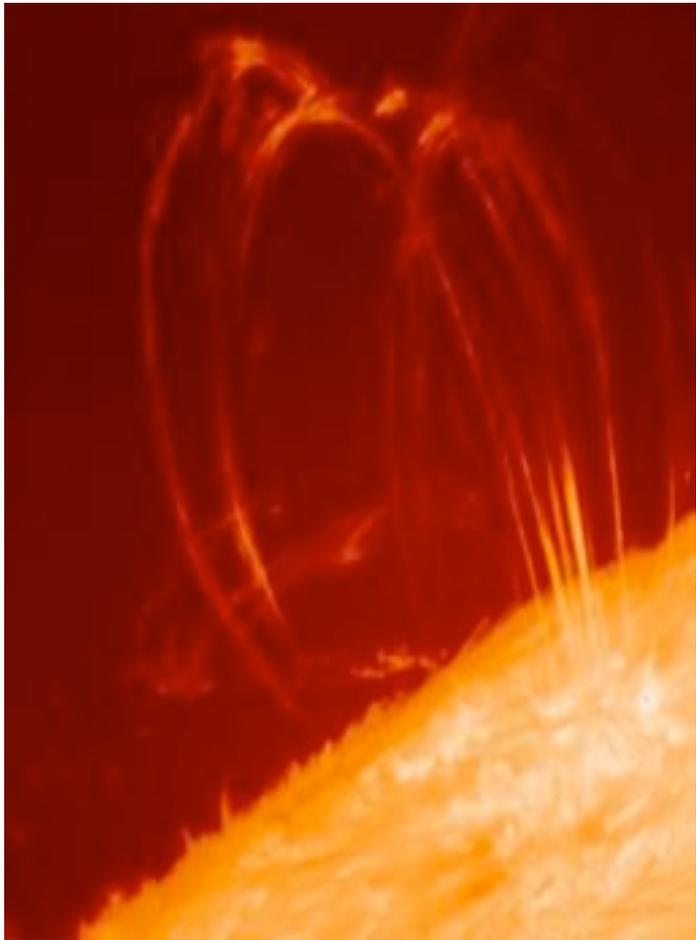
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# monopoles in QGP

- Dual superconductivity as a confinement mechanism ('tHooft, Mandelstam 1980's) require monopole condensation (nonzero VEV)
- But maybe we better look at  $T > T_c$  and study dyon dynamics **without condensation when they are heavy/classical enough?**
- Lorentz force on monopoles makes them reflect from a region with  $E$ , or even rotate around the  $E$  flux => compresses  $E$  into flux tubes even in classical plasma!

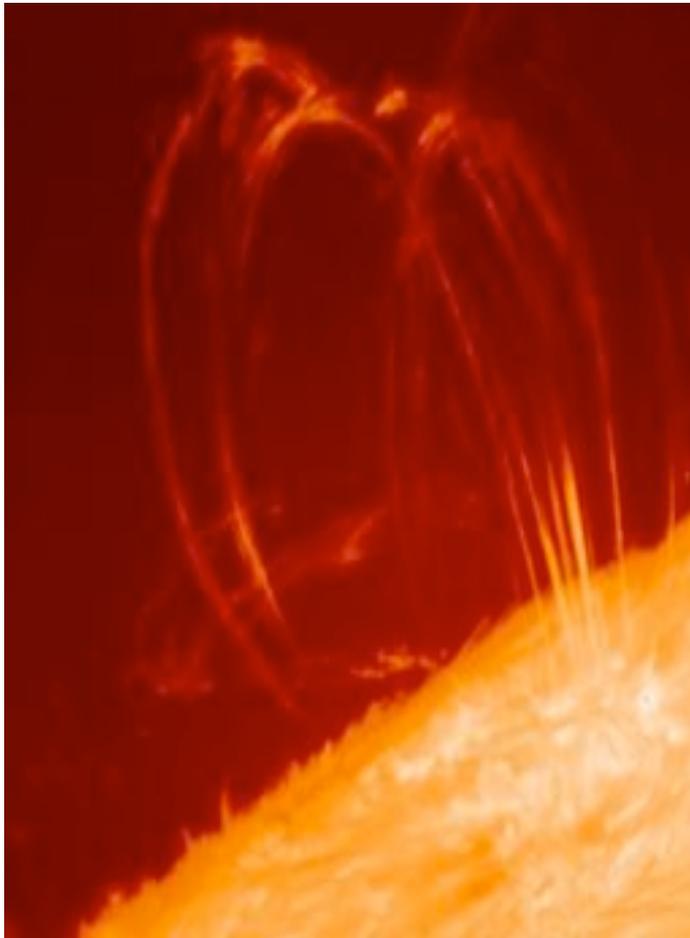
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a dual superconductor?

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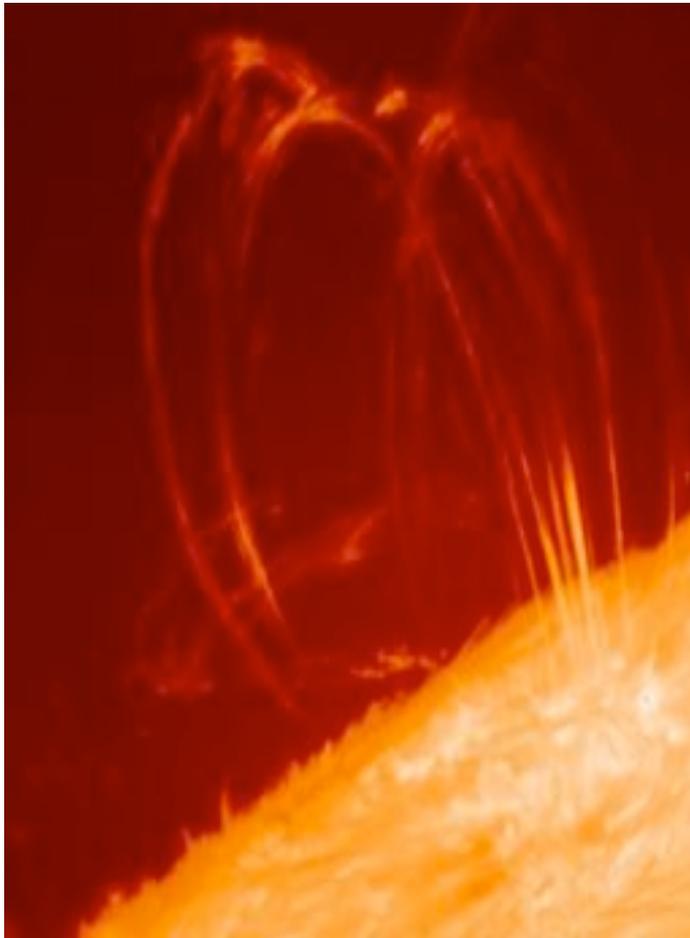
# Can a flux tube exist **without** a dual superconductor?

- Here are magnetic **flux tubes at the Sun,**



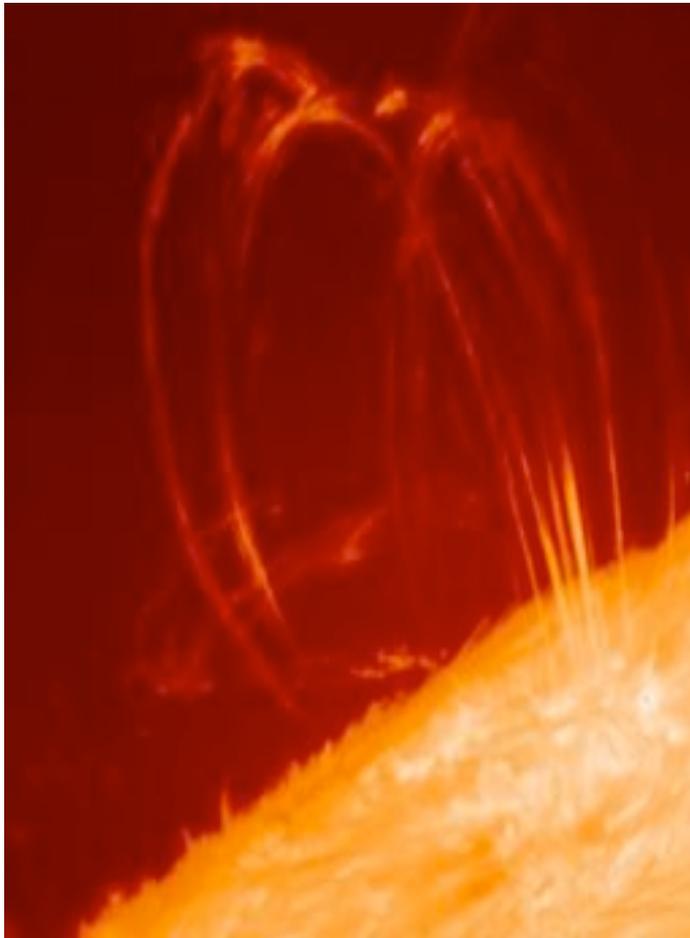
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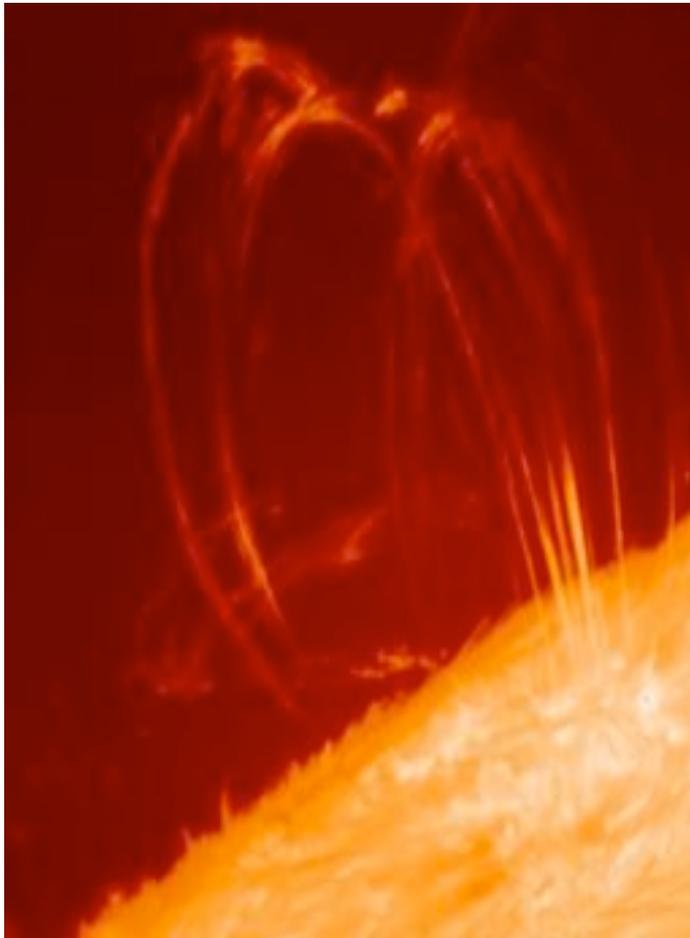


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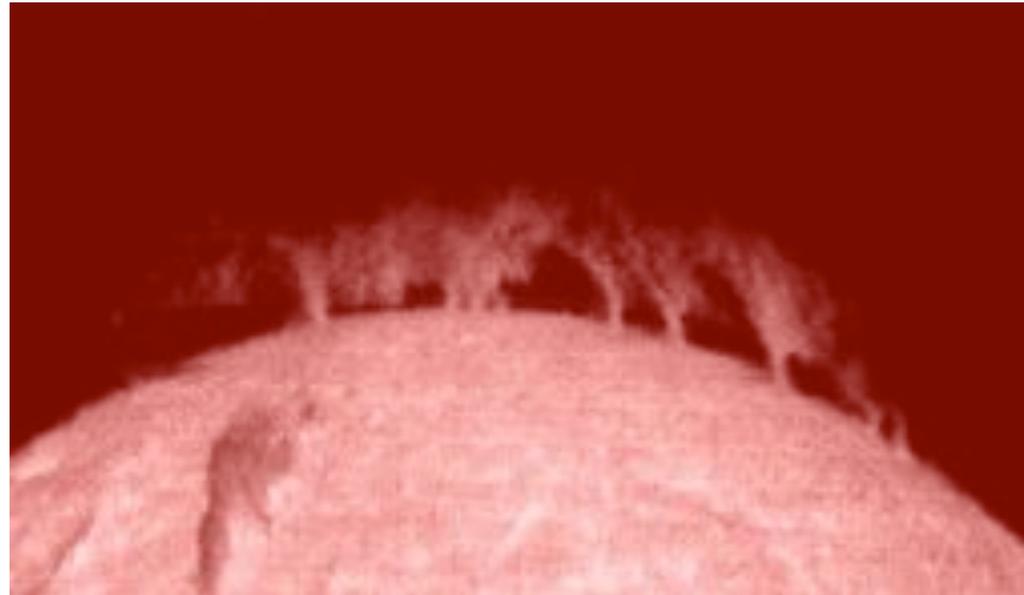
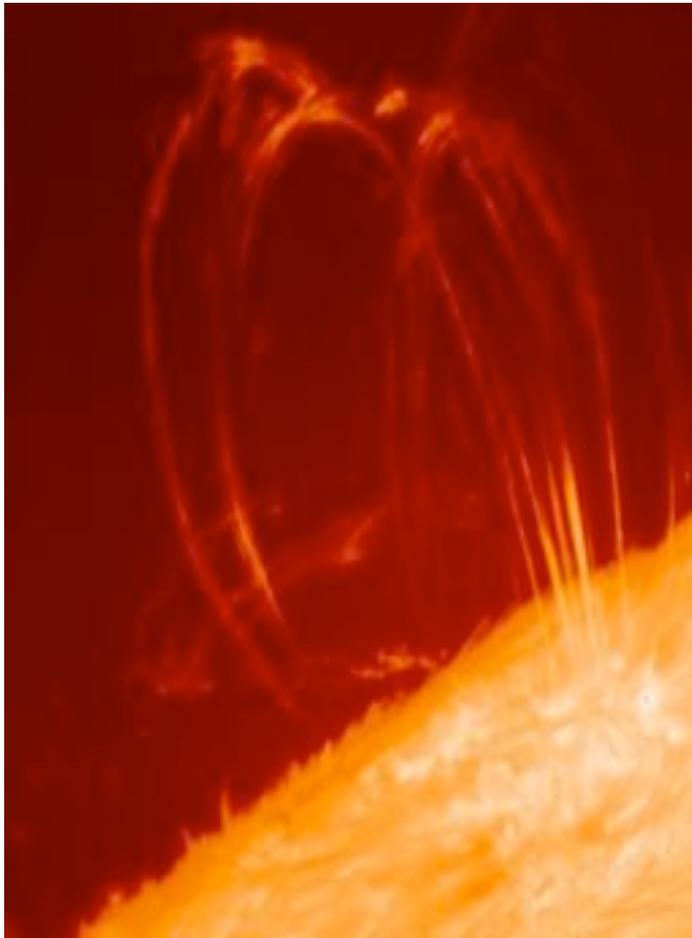


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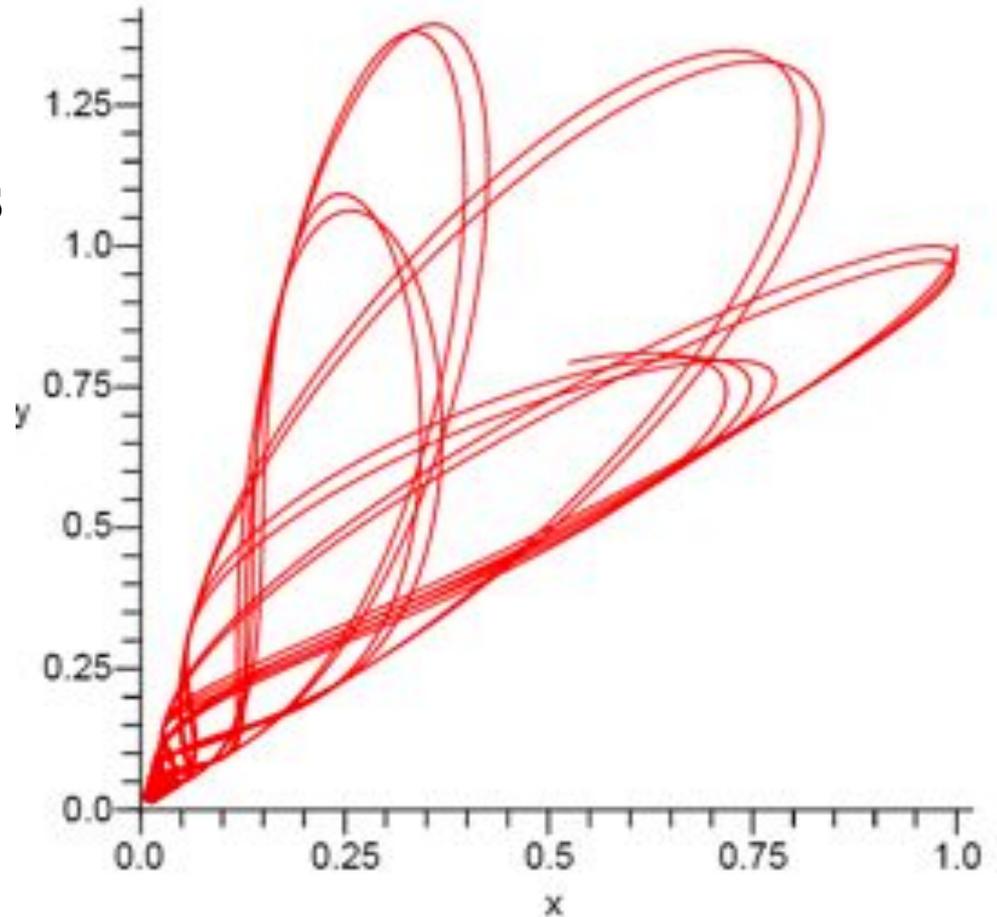


# Let us however start with one monopole (dyon)+ one charge

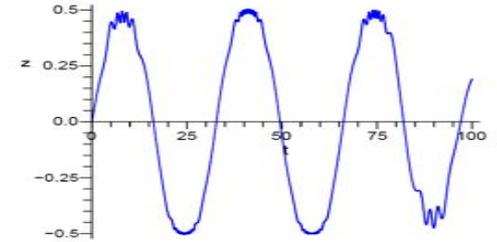
**A. Poincaré 110 years ago had explained that there is angular momentum of the field  $\mathbf{J} \parallel \mathbf{r}$  and that the motion is restricted to a cone**

**Monopole repels from a charge**

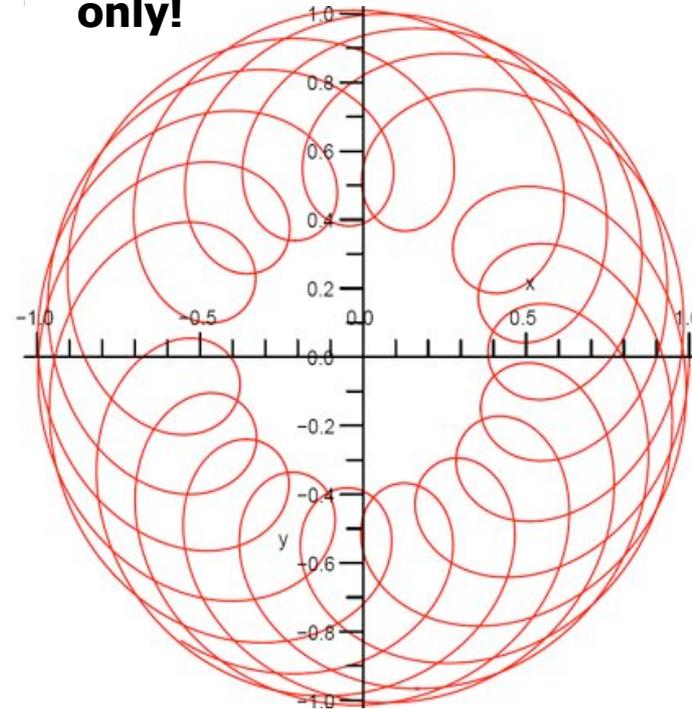
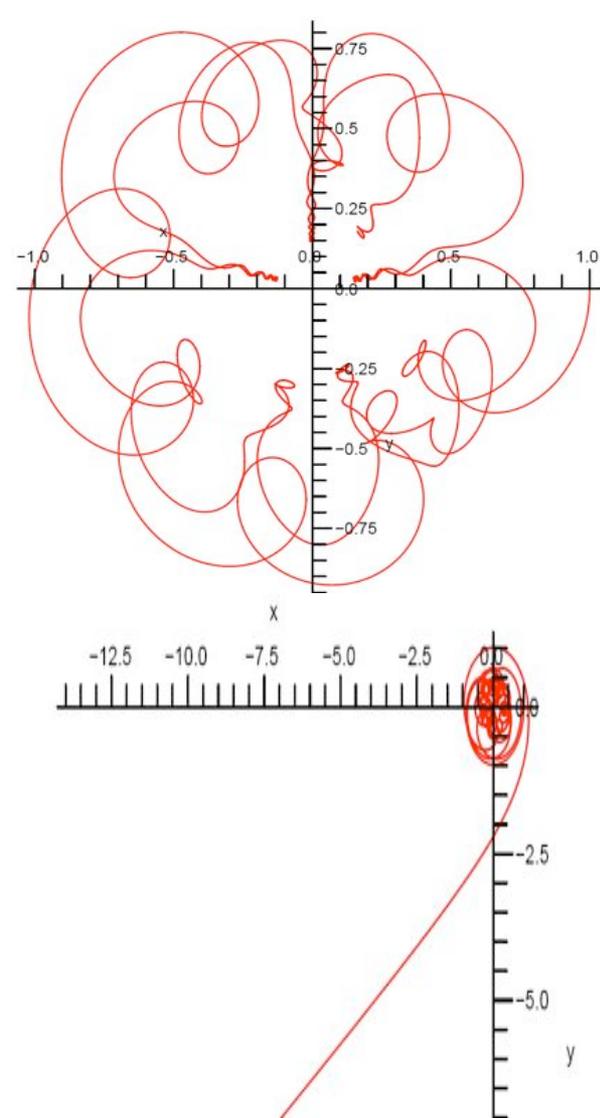
**Here is my solution for a dyon with Attractive charge, preventing the escape to large  $r$**   
Quantum system is like H atom...



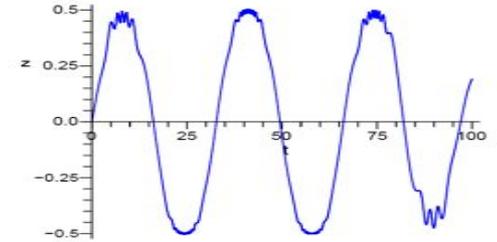
I found that **two charges** play ping-pong by a **monopole** without even moving!



**Chaotic, regular and escape trajectories for a monopole, all different in initial condition by 1/1000 only!**

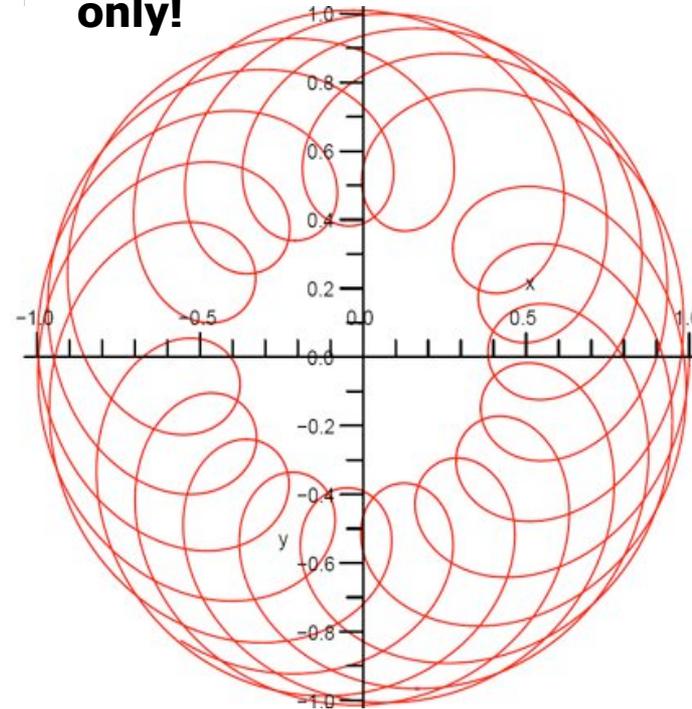
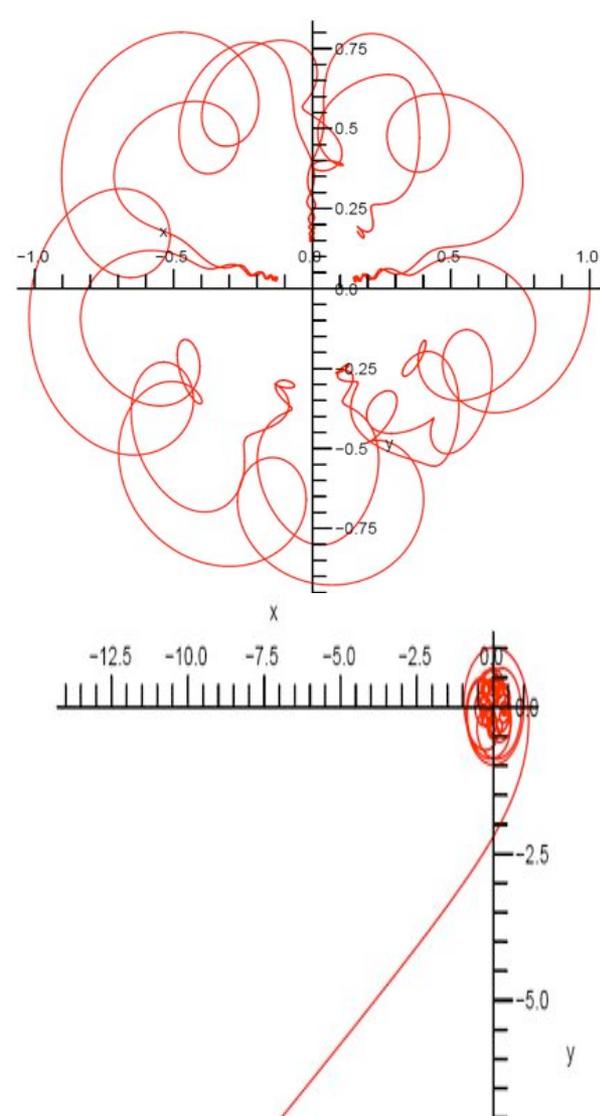


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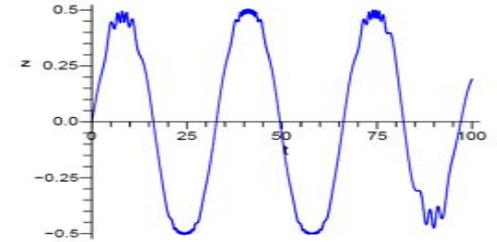


Dual to Budker's

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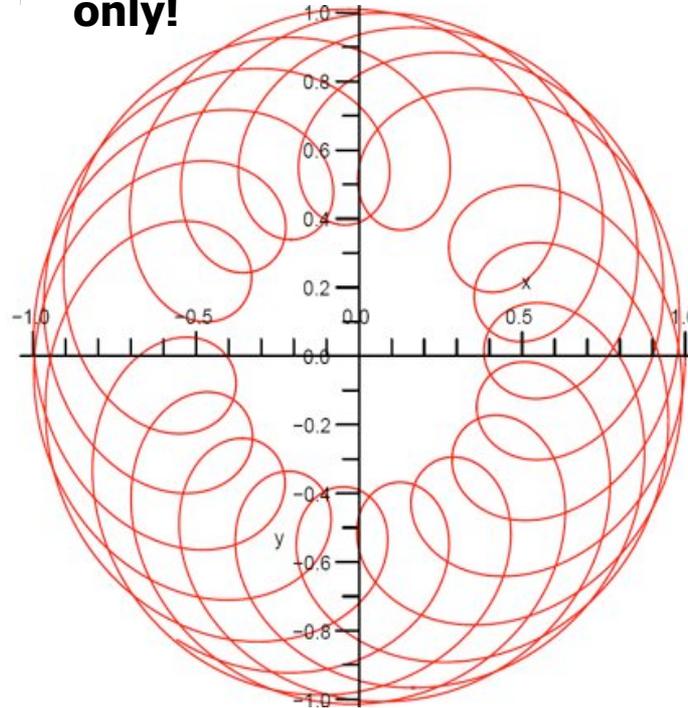
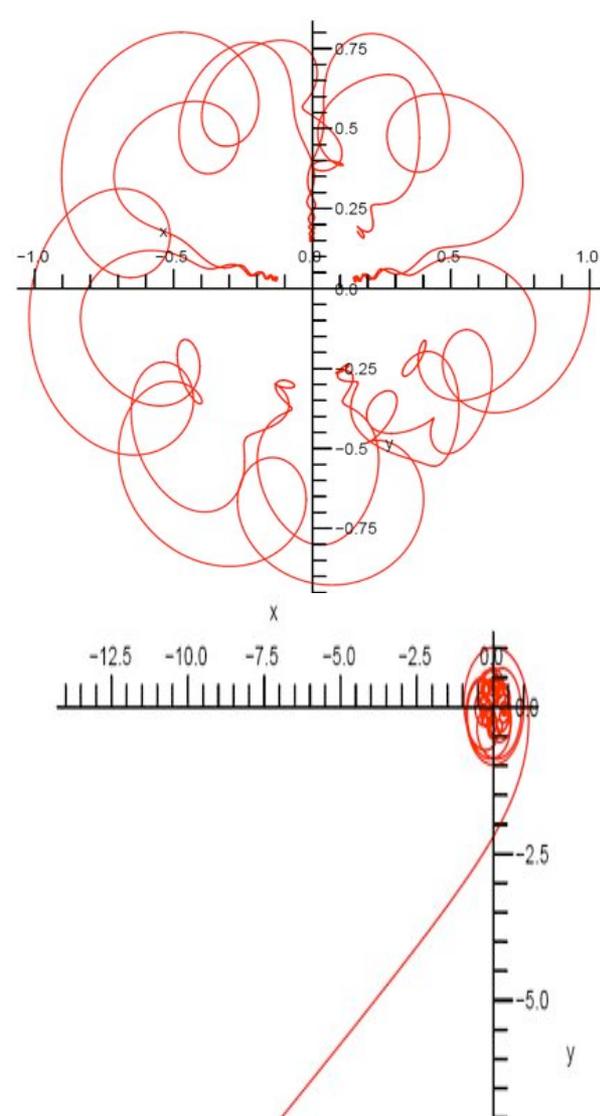


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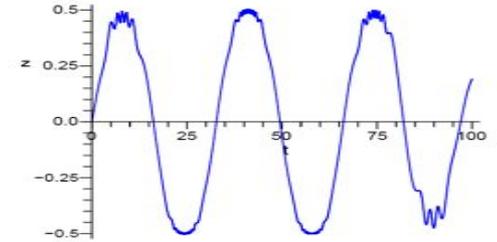
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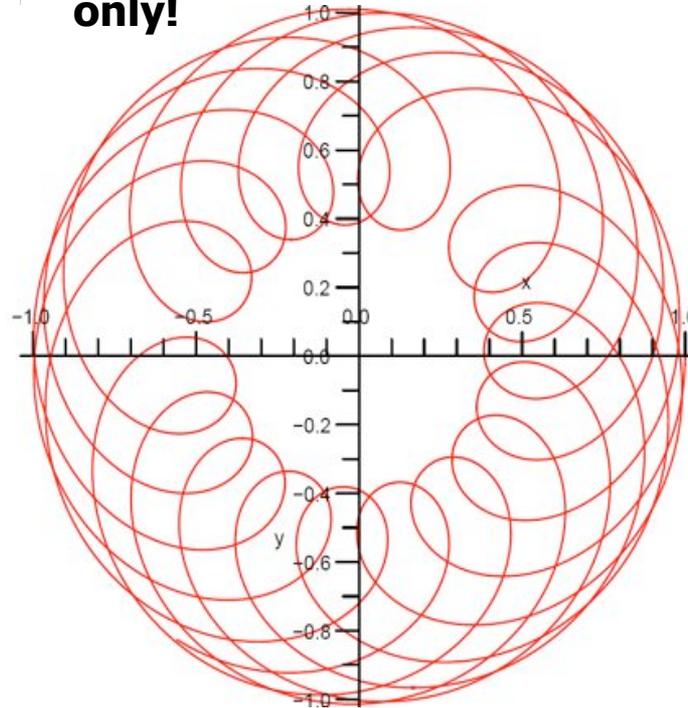
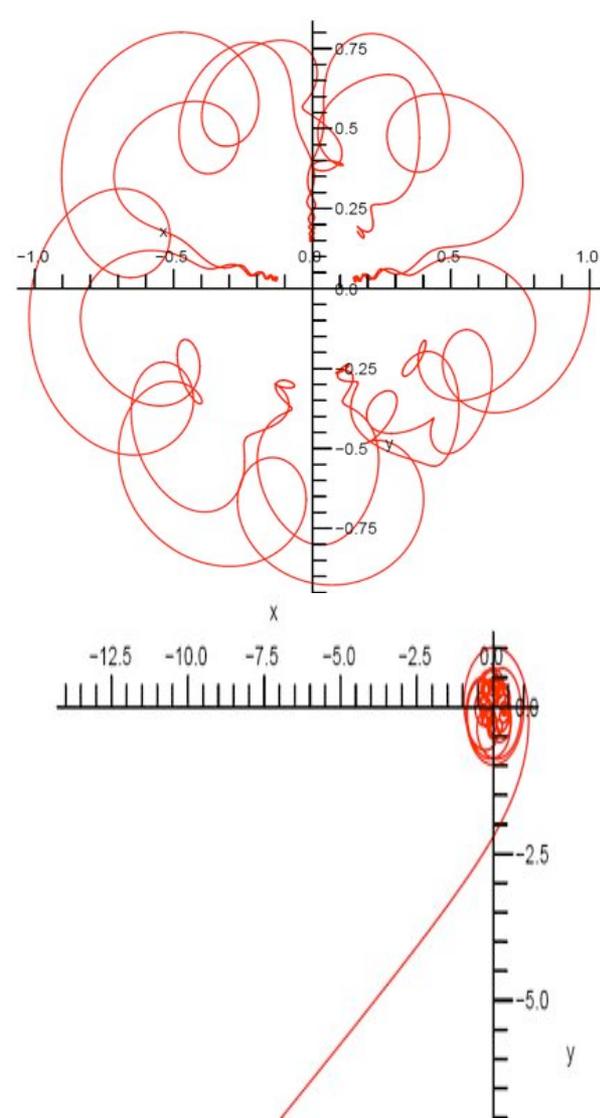
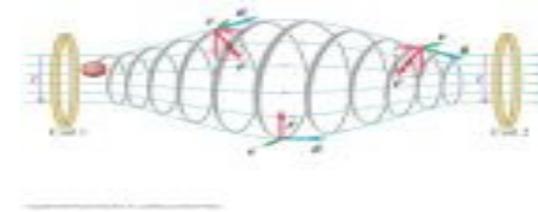


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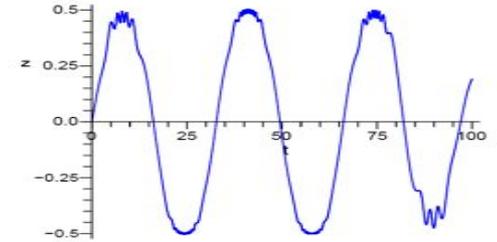


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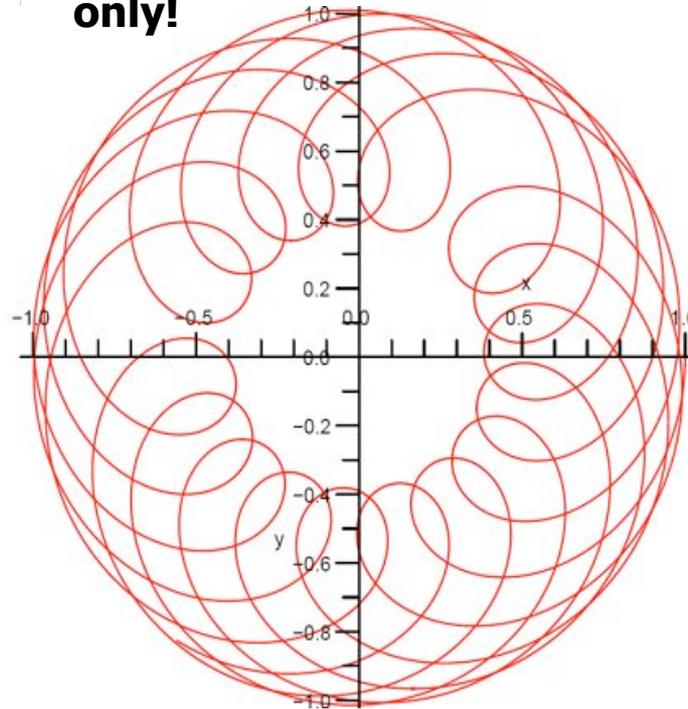
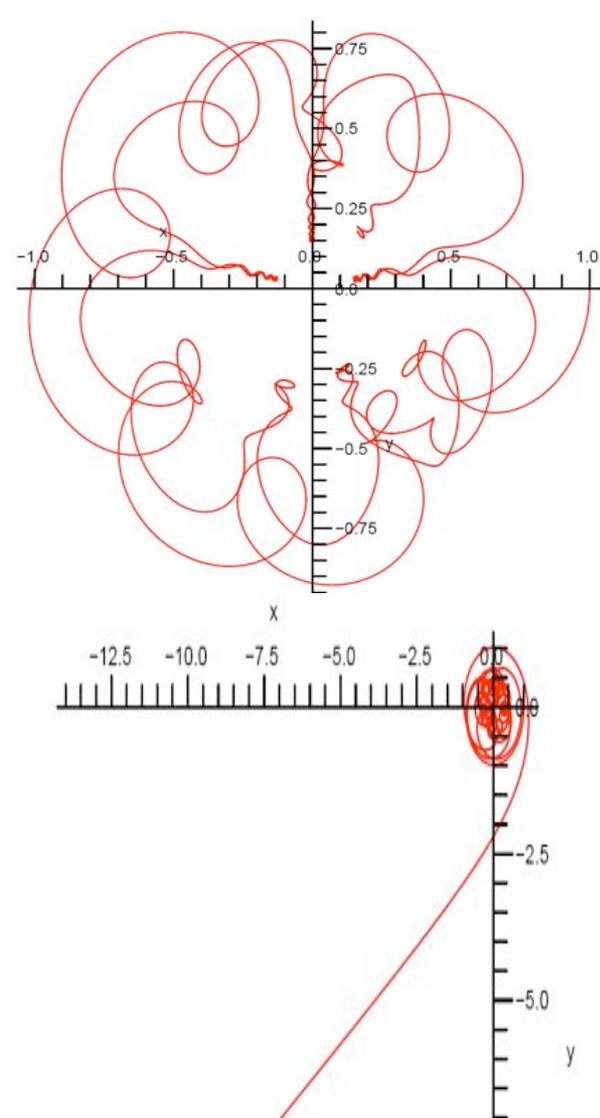
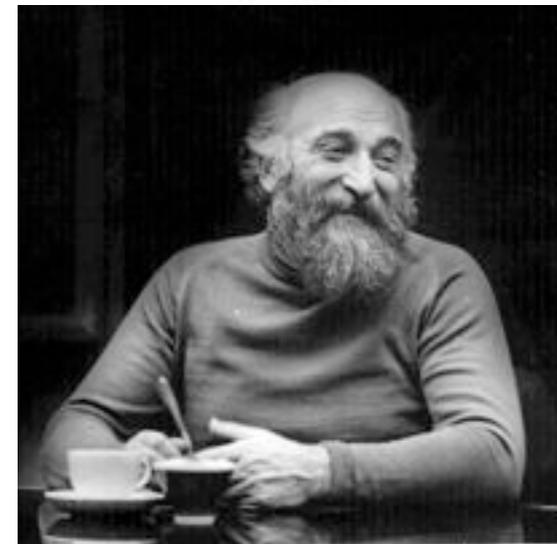


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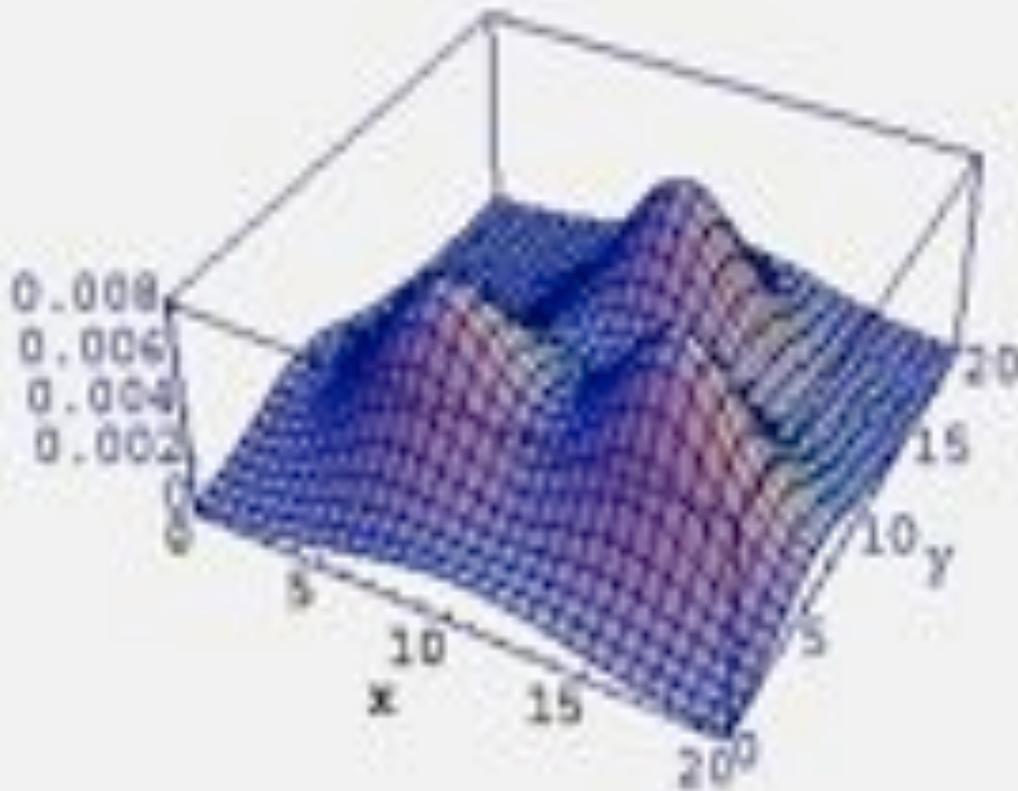
Can we see monopoles? How many are there at  $T > T_c$ ?

Topology and fermionic zero modes helps

# Caloron = baryon made of $N_c$ dyons, can be seen in energy directly:

KvBLL solutions:

T. C. Kraan and P. van Baal, K. Lee and C. Lu [1998]



**Classical solutions  
with the top. charge  
 $Q=1$  and **nonzero  
holonomy  $\langle P \rangle$**   
( $A_0$  or Higgs  $\text{VeV}$ )**

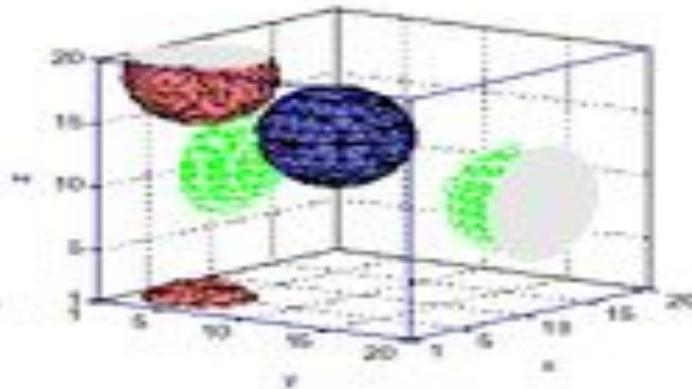
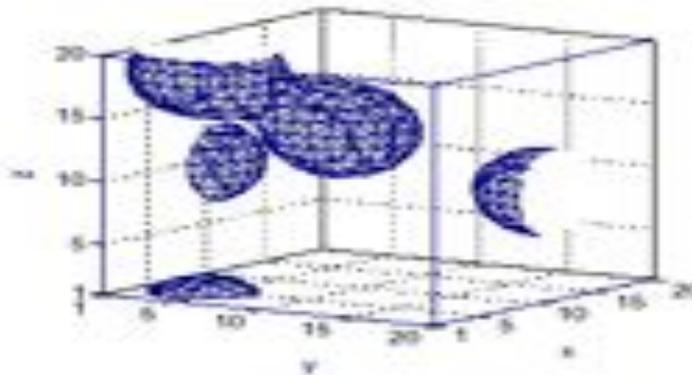
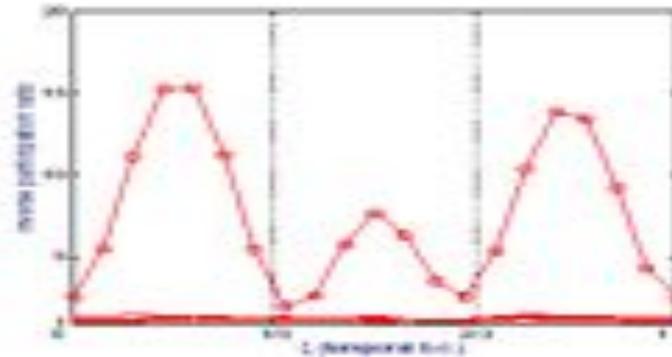
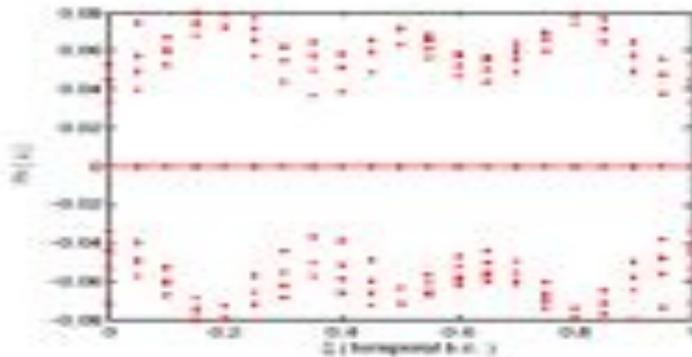
**$\Rightarrow$**

**(long suspected because there  
are 4  $N_c$  collective coordinates  
and monopoles have 4)**

**Now it has nice Ads/CFT  
brane derivation**

# Such semiclassical self-dual dyons are even better seen in lattice configurations via fermionic zero modes

(From Ilgenfritz et al)



Non-trivial  $Q = 1$  caloron : Spectral flow (upper left), IPR of zero-mode (breathing, upper right), action density (bottom left) and zero-mode density (bottom right), for three  $z$ 's corresponding to maximal localization.

A  $SU(2)$  multicaloron ring with  $Q = 3$  containing 6 dyons

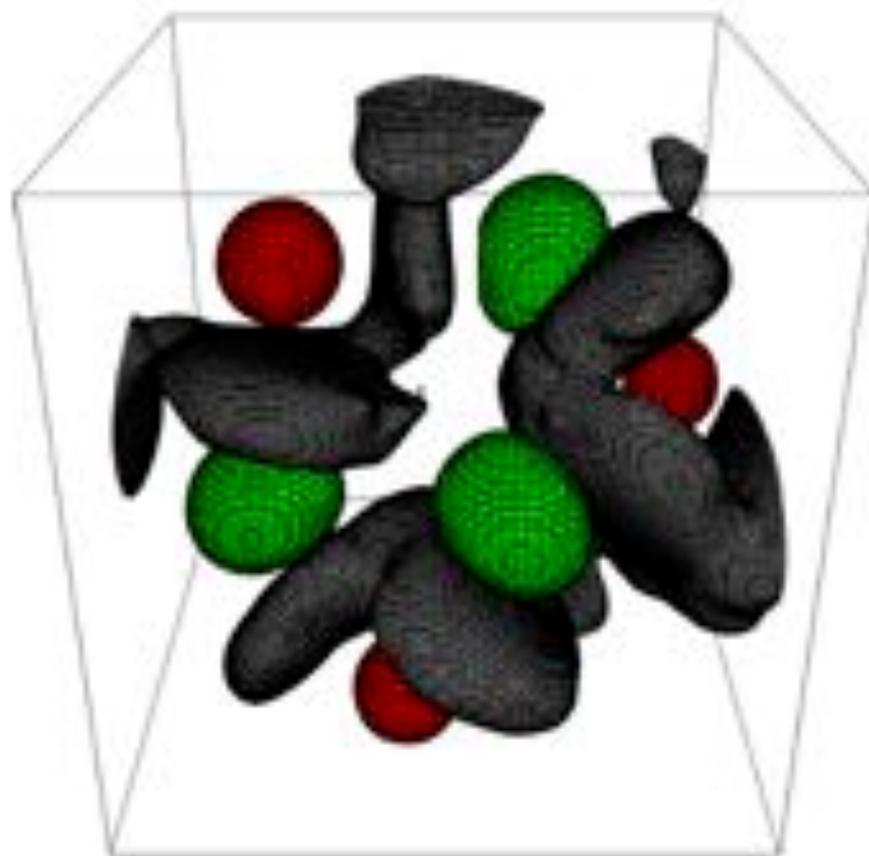


Figure 13: A  $Q = 3$  caloron with non-trivial holonomy in  $SU(2)$ : Iso-surfaces of the Polyakov loop at positive ( $L$  dyons, red) and negative values ( $M$  dyons, green). Regions of non-staticity (in dark) are separating the  $L$  and  $M$  dyons (alternating along a multicaloron ring) from each other.

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- **Classical QGP and its MD:**
  - **a strongly coupled liquid with local color and crystalline order can be studied in real time**

# Additional slides