

# *Dark Matter Direct Detection in the NMSSM*

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DSU2007

D. Cerdeño, C. Hugonie, D. L-F, C. Muñoz, A. Teixeira, JHEP 0412 (2004) 048.  
D. Cerdeño, E. Gabrielli, D. L-F, C. Muñoz, A. Teixeira, JCAP (2007) (accepted).

## Outline

### Direct Detection of Neutralino Dark Matter in the NMSSM

- The NMSSM
- The Neutralino-Nucleon Cross Section
- Experimental constraints
- Analysis of Neutralino DM in the NMSSM

### Conclusions

## Why the NMSSM?

### The NMSSM

- ★ Solves a problem of naturalness in the MSSM: why the  $\mu$  parameter in  $\mu H_1 H_2$  is of order the electroweak scale.

### Superpotential

$$W = \epsilon_{ij} \left( Y_u H_2^j Q^i u + Y_d H_1^i Q^j d + Y_e H_1^i L^j e \right) - \epsilon_{ij} \lambda S H_1^i H_2^j + \frac{1}{3} \kappa S^3$$

### Higgs soft terms of the NMSSM

$$-\mathcal{L}_{soft}^{Higgs} = m_{H_i}^2 H_i^* H_i + m_S^2 S^* S + \left( -\epsilon_{ij} \lambda A_\lambda S H_1^i H_2^j + \frac{1}{3} \kappa A_\kappa S^3 + \text{H.c.} \right)$$

## NMSSM potential

After EW Symmetry breaking:  $\langle H_1^0 \rangle = v_1$ ,  $\langle H_2^0 \rangle = v_2$ ,  $\langle S \rangle = s$

$$\mu_{\text{eff}} = \lambda s$$

$$\begin{aligned} \langle V_{\text{neutral}}^{\text{Higgs}} \rangle &= \frac{g_1^2 + g_2^2}{8} (|v_1|^2 - |v_2|^2)^2 + |\lambda|^2 (|s|^2 |v_1|^2 + |s|^2 |v_2|^2 + |v_1|^2 |v_2|^2) \\ &+ |\kappa|^2 |s|^4 + m_{H_1}^2 |v_1|^2 + m_{H_2}^2 |v_2|^2 + m_S^2 |s|^2 \\ &+ (-\lambda \kappa^* v_1 v_2 s^{*2} - \lambda A_\lambda s v_1 v_2 + \frac{1}{3} \kappa A_\kappa s^3 + \text{H.c.}) \end{aligned}$$

## Minimization of the scalar potential

Finding a minimum of  $V$  is much harder than in the MSSM ...

From the minimization of the potential with respect to the phases of the VEV's we have

four combinations of signs for  $A_\kappa$ ,  $A_\lambda$ ,  $s$  and  $k$  :

(i)  $\text{sign}(s) = \text{sign}(A_\lambda) = -\text{sign}(A_\kappa),$

(ii)  $\text{sign}(s) = -\text{sign}(A_\lambda) = -\text{sign}(A_\kappa),$

with  $|A_\kappa| > 3\lambda v_1 v_2 |A_\lambda| / (-|sA_\lambda| + \kappa|s^2|).$

(iii)  $\text{sign}(s) = \text{sign}(A_\lambda) = \text{sign}(A_\kappa),$

with  $|A_\kappa| < 3\lambda v_1 v_2 |A_\lambda| / (|sA_\lambda| + \kappa|s^2|).$

(iv)  $\text{sign}(s) = \text{sign}(A_\lambda) = \text{sign}(A_\kappa),$

with  $|A_\kappa| > 3\lambda v_1 v_2 |A_\lambda| / (|sA_\lambda| - \kappa|s^2|).$

$k > 0$

$k < 0$

We must also satisfy the minimization Eqs. for  $|v|$

## NMSSM Particle content

$$\text{NMSSM Spectrum} \equiv \text{MSSM} + \left\{ \begin{array}{l} 2 \text{ Higgs (CP - even, CP - odd)} \\ 1 \text{ Neutralino} \end{array} \right.$$

$$\mathcal{M}_{\tilde{\chi}^0} = \begin{pmatrix} M_1 & 0 & -M_Z \sin \theta_W \cos \beta & M_Z \sin \theta_W \sin \beta & 0 \\ 0 & M_2 & M_Z \cos \theta_W \cos \beta & -M_Z \cos \theta_W \sin \beta & 0 \\ -M_Z \sin \theta_W \cos \beta & M_Z \cos \theta_W \cos \beta & 0 & -\lambda s & -\lambda v_2 \\ M_Z \sin \theta_W \sin \beta & -M_Z \cos \theta_W \sin \beta & -\lambda s & 0 & -\lambda v_1 \\ 0 & 0 & -\lambda v_2 & -\lambda v_1 & 2\kappa s \end{pmatrix}$$

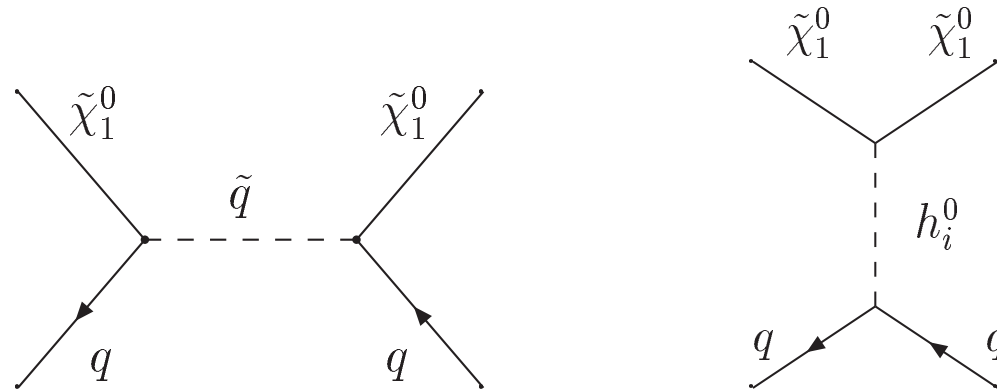
The lightest neutralino:

$$\tilde{\chi}_1^0 = N_{11} \tilde{B}^0 + N_{12} \tilde{W}_3^0 + N_{13} \tilde{H}_1^0 + N_{14} \tilde{H}_2^0 + N_{15} \tilde{S}$$

The lightest CP-even Higgs:

$$h_1^0 = S_{11} H_1^0 + S_{12} H_2^0 + S_{13} S$$

## Dark matter: Direct detection in the NMSSM



$$\mathcal{L}_{\text{eff}} = \alpha_{3i} \tilde{\chi}_1^0 \tilde{\chi}_1^0 \bar{q}_i q_i$$

$$\alpha_{3i}^h = \sum_{a=1}^3 \frac{1}{m_{h_a^0}^2} C_Y^i \text{Re} [C_{HL}^a]$$

$$\alpha_{3i}^{\tilde{q}} = -\sum_{X=1}^2 \frac{1}{4(m_{X_i}^2 - m_{\tilde{\chi}_1^0}^2)} \text{Re} \left[ (C_R^{Xi}) (C_L^{Xi})^* \right]$$

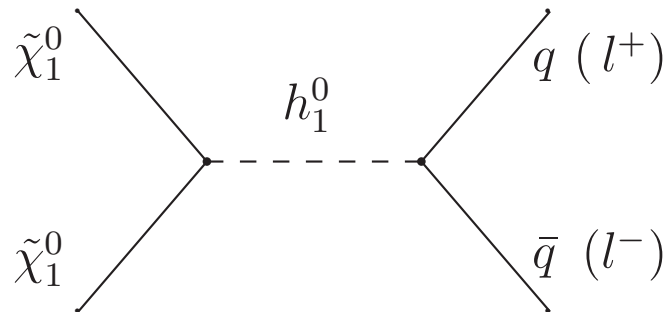
See also V. Barger et al., '07, for an analysis of MSSM singlet extensions.

## Relic density

Enough  $\tilde{\chi}_1^0$  can survive annihilation (and coannihilation) in order to account for observed  $\Omega$

$$\text{For example: } \tilde{\chi}_1^0 \tilde{\chi}_1^0 \Rightarrow \begin{cases} W^\pm W^\pm, Z Z \\ h^0 h^0, a^0 a^0, h^0 Z \\ \bar{q} q, l^+ l^- \end{cases}$$

NMSSM similar to MSSM, but **additional "fingerprint"-type processes** like



where  $\tilde{\chi}_1^0 \leftrightarrow$  singlino;  $h_1^0 \leftrightarrow$  singlet

**BUT! Generating large  $\sigma$  may lead to excessive  $\tilde{\chi}_1^0$ -annihilation (low  $\Omega$ )**



## Constraints on the NMSSM parameter space and computation

Relevant parameters at low scale  $\lambda, \kappa, \tan\beta, \mu, A_\lambda, A_\kappa, M_1, M_2, M_3$  ( $M_0, A_0$ )

- **Minimization** of the potential
  - Absence of **Landau Pole** for  $\lambda, \kappa, Y_t$ , and  $Y_b$  below  $M_{GUT}$
  - Computation of the **NMSSM spectrum**
  - **Experimental** constraints from **LEP**
    - Neutralino**
    - Higgs**
    - Squark**
- } **NMHDECAY 2.0**  
(Ellwanger, Hugonie)
- $b \rightarrow s \gamma$  ( $g_\mu - 2$ ), rare  $B$  and  $K$  decays Our code
  - **Dark Matter Relic density** New MicrOMEGAs
  - **Neutralino Nucleon Cross Section** Our code

## Muon anomalous magnetic moment ( $a_\mu$ )

Experimental data:  $a_\mu = 11659208(6) \times 10^{-10}$   
Theoretical for SM:  $a_\mu = 11659180.4(5.1) \times 10^{-10}$

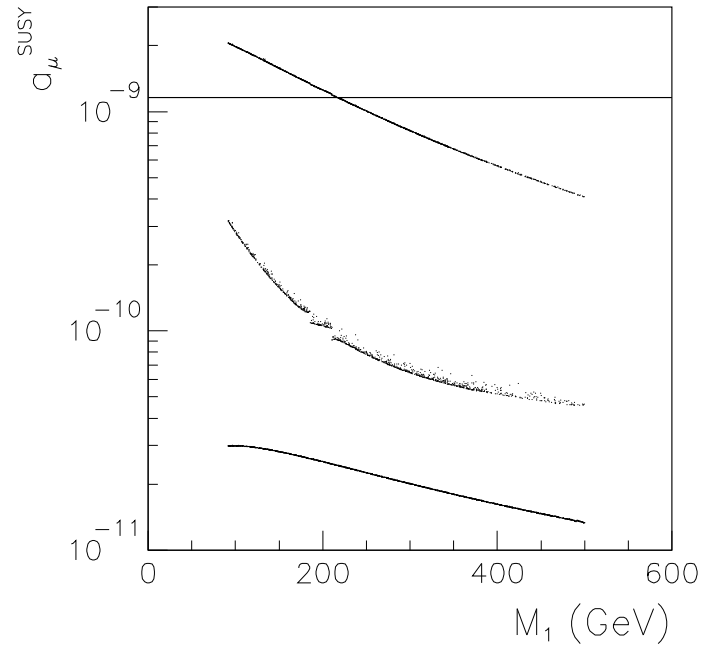
$$\Delta a_\mu = (27.6 \pm 8) \times 10^{-10}$$

At to  $2\sigma$  level the SUSY contribution must be:

$$11.6 \times 10^{-10} \lesssim a_\mu^{\text{SUSY}} \lesssim 43.6 \times 10^{-10}$$

SUSY contributions at 1 loop-level:

- Dominant: **Sneutrino and Chargino**
- **Charged Sleptons and Neutralino**



$\mathbf{a_{\mu}^{SUSY}}$  as a function of  $\mathbf{M_1}$

The horizontal solid line indicates the lower bound of the allowed  $2\sigma$  interval.

Choosing typical NMSSM values  $\mu = 150$  GeV,  $-800 \lesssim A_\lambda \lesssim 800$  GeV,  $-300 \lesssim A_\kappa \lesssim 300$  GeV, and low  $\tan \beta$ ,  $\tan \beta = 5$ , in order to analyze departures from the MSSM.

From bottom to top,  $m_{L,E} = 1$  TeV with  $A_E = 1$  TeV,

$m_{L,E} = 150$  GeV with  $A_E = 1$  TeV,  $m_{L,E} = 150$  GeV with  $A_E = -2.5$  TeV.

$$b \rightarrow s \gamma$$

Experimental data [HFAG '06]:  $\text{BR}(b \rightarrow s \gamma) = (3.55 \pm 0.27) \times 10^{-4}$

Theoretical calculation for the SM [Gambino '05]:  $\text{BR}(b \rightarrow s \gamma) = (3.73 \pm 0.30) \times 10^{-4}$

### SUSY contributions at 1 loop-level

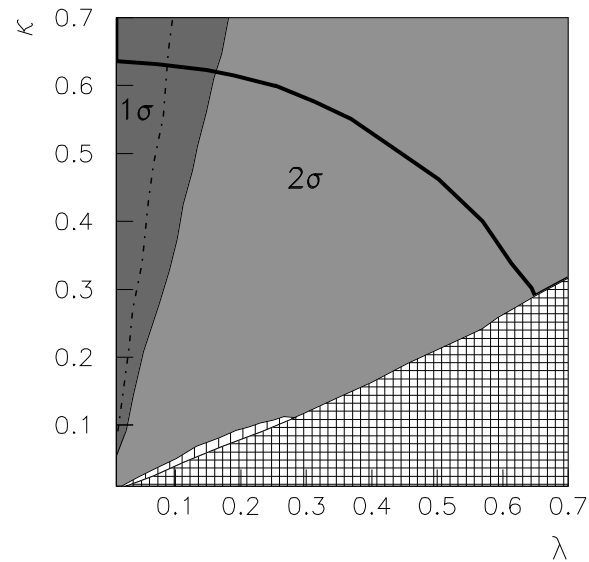
- Charged Higgs  $H^\pm$  and up quarks  $u, c, t$
- Chargino  $\tilde{\chi}^\pm$  and up squarks  $\tilde{u}, \tilde{c}, \tilde{t}$
- Neutralino  $\tilde{\chi}^0$  and down squarks  $\tilde{d}, \tilde{s}, \tilde{b}$
- gluino  $\tilde{g}$  and down squarks  $\tilde{d}, \tilde{s}, \tilde{b}$

In our analysis: dominant  $H^\pm$ -mediated contribution! [No flavour mixing other than the  $V_{\text{CKM}}$ ]

$$\Rightarrow \text{BR}(b \rightarrow s \gamma) \propto 1/m_{H^\pm}^4 \quad \text{with } m_{H^\pm}^2 = \frac{2\mu^2}{\sin(2\beta)} \frac{\kappa}{\lambda} - v^2 \lambda^2 + \frac{2\mu A_\lambda}{\sin(2\beta)} + m_W^2$$

## BR( $b \rightarrow s\gamma$ ) in the NMSSM: Results

$M_1 = 160 \text{ GeV}$ ,  $M_2 = 320 \text{ GeV}$ ,  $A_\lambda = 400 \text{ GeV}$ ,  $A_\kappa = -200 \text{ GeV}$ ,  $\mu = 130 \text{ GeV}$ ,  
 $\tan \beta = 5$



$b \rightarrow s\gamma$  isocurves "mimic"  $m_{H^\pm}$  isocurves

$b \rightarrow s\gamma$  typically maximal close to tachyon "border"

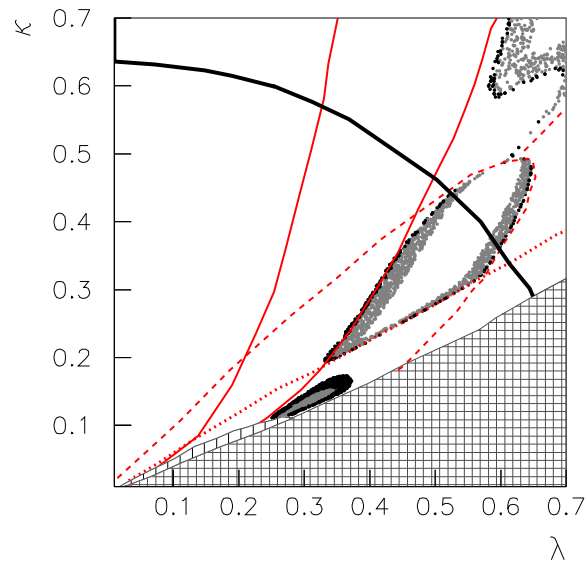
Improve  $b \rightarrow s\gamma$ : larger  $(A_\lambda, \mu, \tan \beta) \longleftrightarrow$  Worsens exclusion by LEP constraints

## Relic density in the $\lambda$ - $\kappa$ plane

For the same parameters as the previous study

$$M_1 = 160 \text{ GeV}, M_2 = 320 \text{ GeV}, A_\lambda = 400 \text{ GeV}, A_\kappa = -200 \text{ GeV}, \mu = 130 \text{ GeV},$$

$$\tan \beta = 5$$



red dots  $\leftrightarrow m_{\chi_1^0} = m_{h_1^0}$ ; black full  $\leftrightarrow m_{\chi_1^0} = m_Z, m_W$ ; red dashed  $\leftrightarrow 2m_{\chi_1^0} = m_{h_2^0}$ ;

Very **light** neutral Higgs:  $m_{h_1^0} \gtrsim 20 \text{ GeV}$ ; **singlet** component:  $S_{13}^2 \sim 0.99$ ;

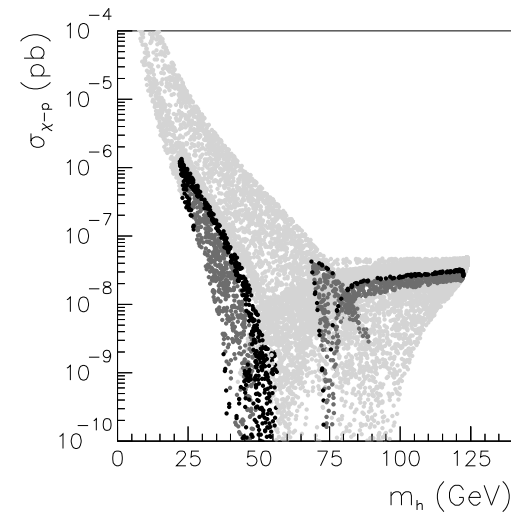
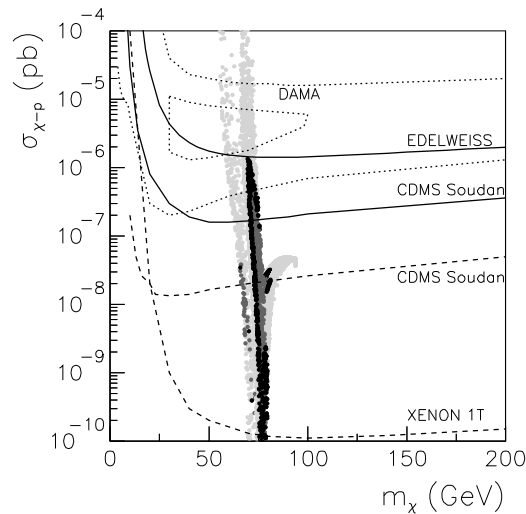
Higgsino-Bino LSP; moving to small  $\kappa$  with respect to  $\lambda \Rightarrow$  small  $m_{\chi_1^0}$  and more singlino  
( $N_{15}^2 \lesssim 0.35$ )

## Dark Matter: $\Omega$ and direct detection

For the same parameters as the previous study

$$M_1 = 160 \text{ GeV}, M_2 = 320 \text{ GeV}, A_\lambda = 400 \text{ GeV}, A_\kappa = -200 \text{ GeV}, \mu = 130 \text{ GeV},$$

$$\tan \beta = 5$$



Gray  $\rightarrow$  Experimentally accepted (accelerators)

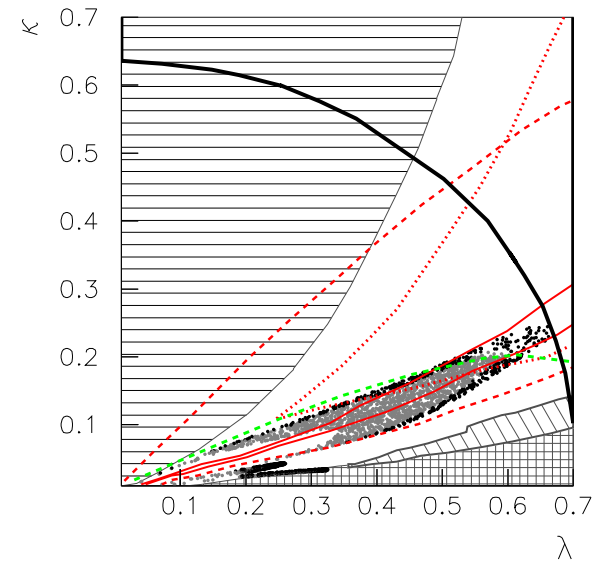
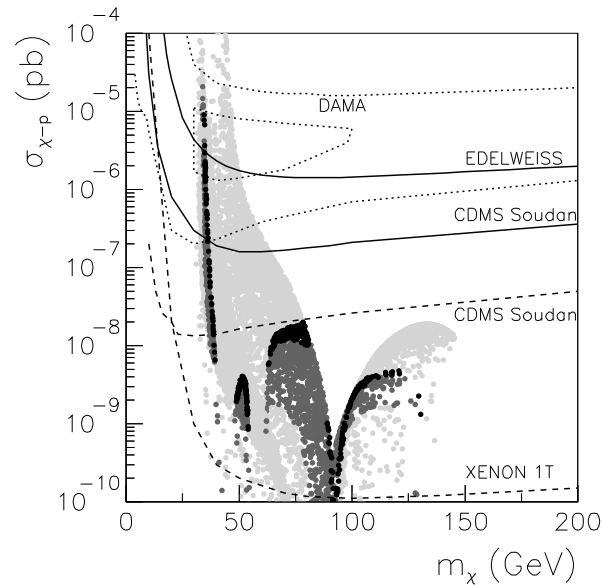
Dark Gray  $\rightarrow$  In addition fulfil  $0.1 \leq \Omega h^2 \leq 0.3$

Black  $\rightarrow$  Satisfies all experimental constraints including WMAP  $0.094 \lesssim \Omega h^2 \lesssim 0.129$

Large  $\sigma \rightarrow$  exchange of light singlet-like Higgs

## NMSSM DM: further examples

$$M_1 = 330 \text{ GeV}, M_2 = 660 \text{ GeV}, A_\lambda = 570 \text{ GeV}, A_\kappa = -60 \text{ GeV}, \mu = 160 \text{ GeV}, \tan \beta = 5$$



★ Green dash  $Z_{15}^2 = .5$

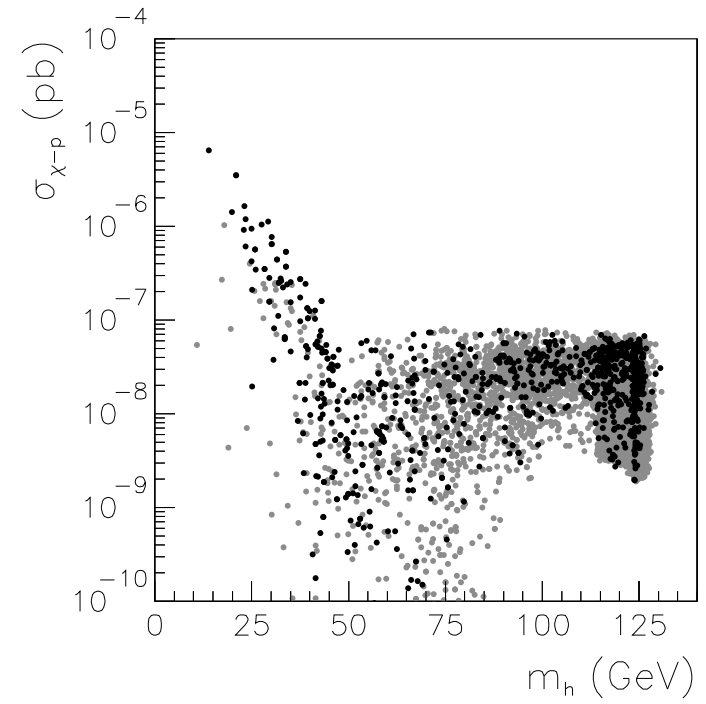
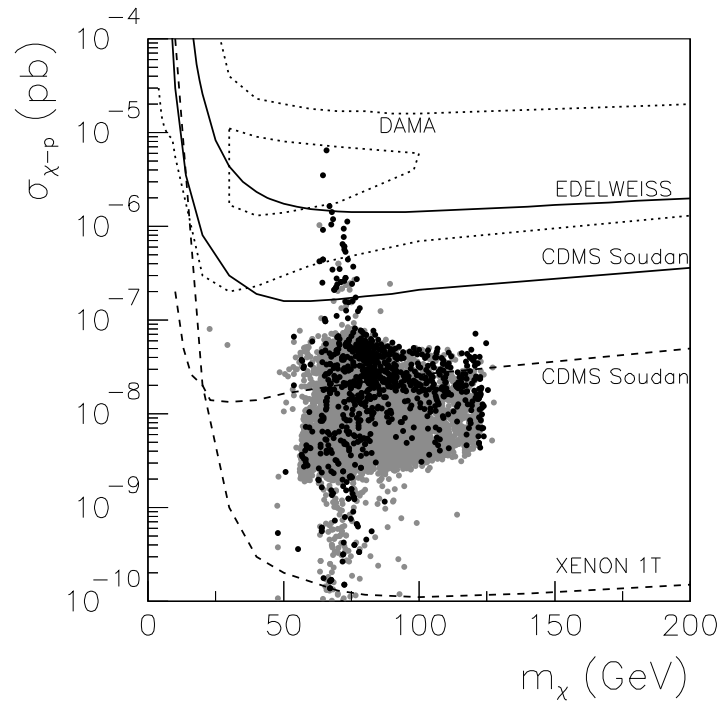
★  $a_\mu$  more than  $2\sigma$  away  $a_\mu \approx 7.2 \times 10^{-10}$

★ Compatible with  $\Omega$  and  $b \rightarrow s\gamma$  ( $2\sigma$ )

★ Within CDMS-Soudan range:  $\tilde{\chi}_1^0$  singlino-like and  $h_1^0$  singlet like.



## NMSSM DM



$$110 \lesssim M_2 \lesssim 430 \text{ GeV}, \quad -800 \lesssim A_\lambda \lesssim 800 \text{ GeV}, \quad -300 \lesssim A_\kappa \lesssim 300 \text{ GeV},$$

$$100 \lesssim \mu \lesssim 300 \text{ GeV}, \quad \tan \beta = 5$$

## Conclusions

### ① Systematic analysis of the NMSSM parameter space

Taken into account LEP constraints

$\text{BR}(b \rightarrow s \gamma)$  bounds (as well as others)

WMAP data on  $\Omega$

Investigated prospects for direct detection of DM

### ② In the NMSSM, large $\sigma_{\tilde{\chi}_1^0-p}$ can be obtained

Associated to  $t$ -channel exchange of very light Higgs ( $m_{h_1^0} \lesssim 70$  GeV),  
large singlet component (escapes detection)

NMSSM nature is further evidenced in having a singlino-Higgsino LSP

### ③ Impact of $\Omega$ and $\text{BR}(b \rightarrow s \gamma)$

$\Omega$  often relies on the same light-Higgs exchange that gives large  $\sigma$

large  $\sigma_{\tilde{\chi}_1^0-p} \leftrightarrow$  excessive annihilation

$\text{BR}(b \rightarrow s \gamma)$  typically larger in regions where DM is WMAP-compatible & within  
range of present detectors